Self-Adjusting Networks

Stefan Schmid

"We cannot direct the wind, but we can adjust the sails."

(Folklore)

Acknowledgements:





Trend

Data-Centric Applications

Datacenters ("hyper-scale")

Interconnecting networks:
a critical infrastructure
of our digital society.

Traffic Growth

Trend

~

and "

î -

NETFLIX

Data-Centric Applications

Datacenters ("hyper-scale")



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a critical infrastructure
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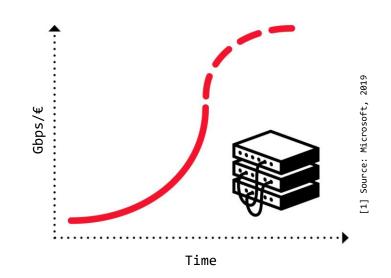


Credits: Marco Chiesa1

The Problem

Huge Infrastructure, Inefficient Use

- Network equipment reaching capacity limits
 - \rightarrow Transistor density rates stalling
 - \rightarrow "End of Moore's Law in networking" [1]
- Hence: more equipment, larger networks
- Resource intensive and:
 inefficient

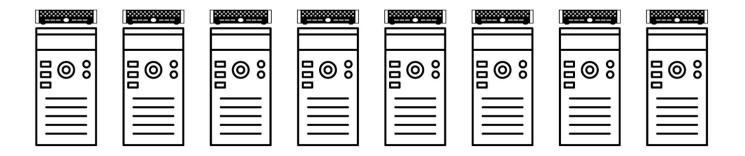


Annoying for companies, opportunity for researchers

Root Cause

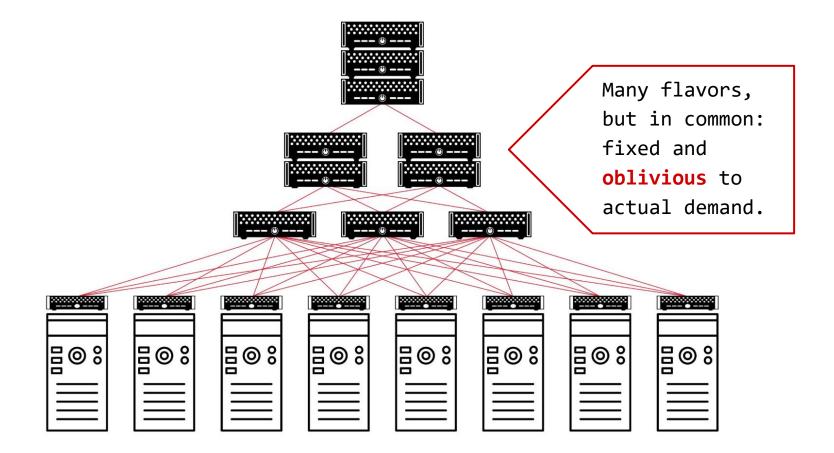
Fixed and Demand-Oblivious Topology

How to interconnect?



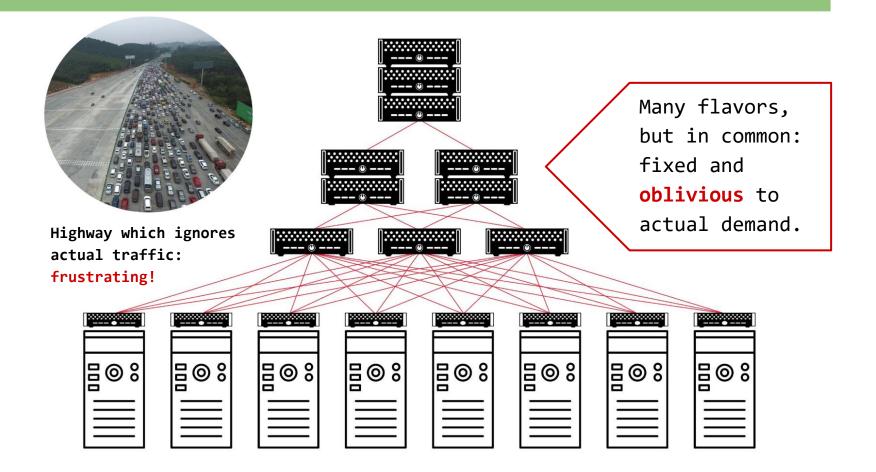
Root Cause

Fixed and Demand-Oblivious Topology

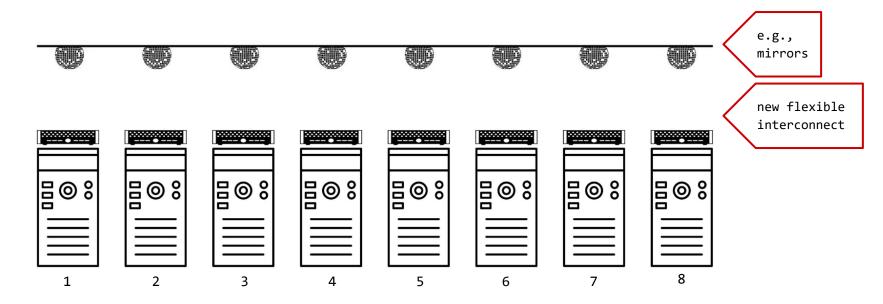


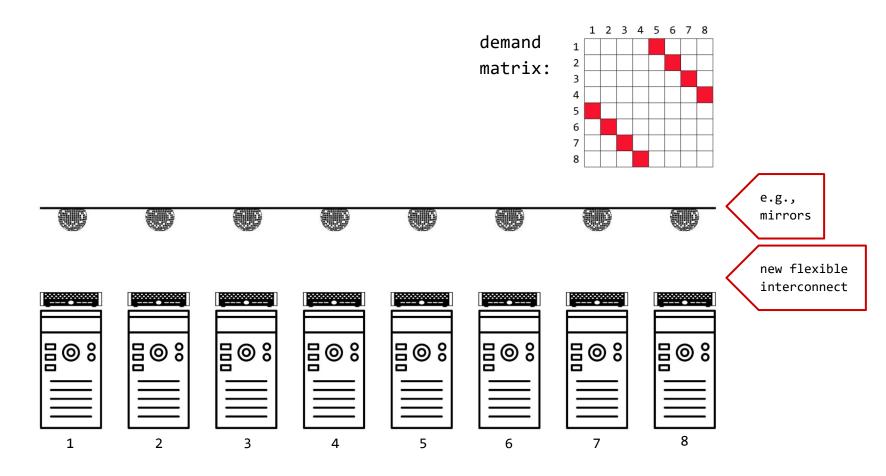
Root Cause

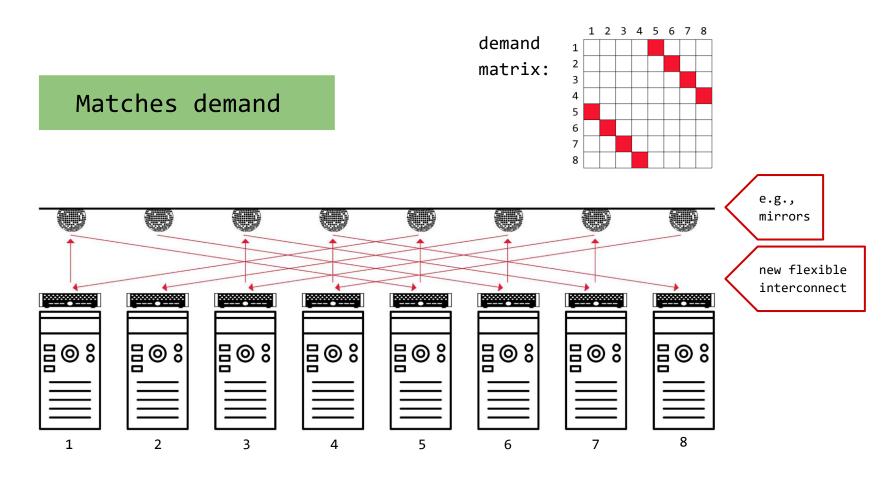
Fixed and Demand-Oblivious Topology

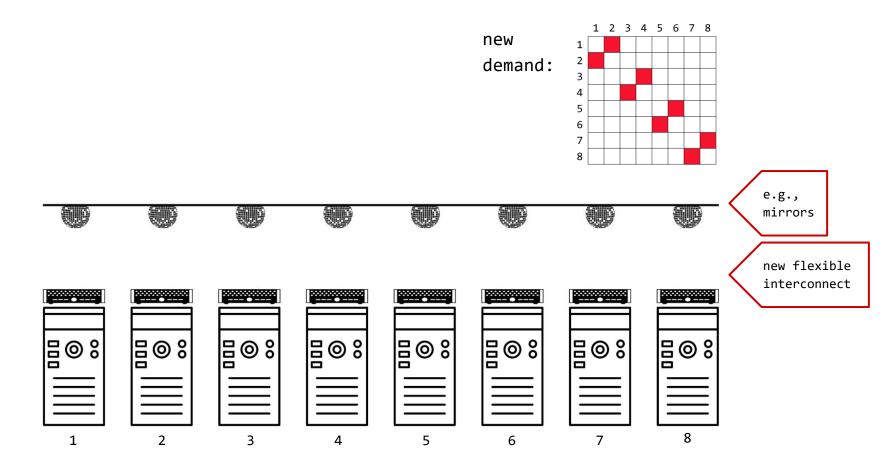


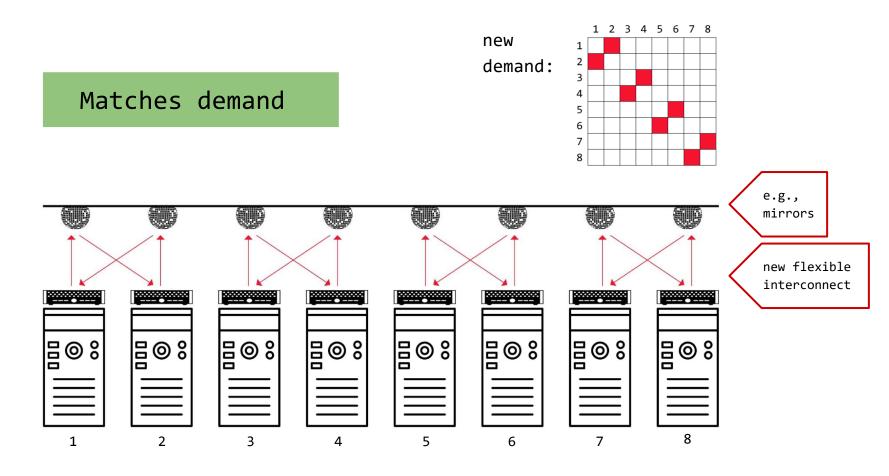
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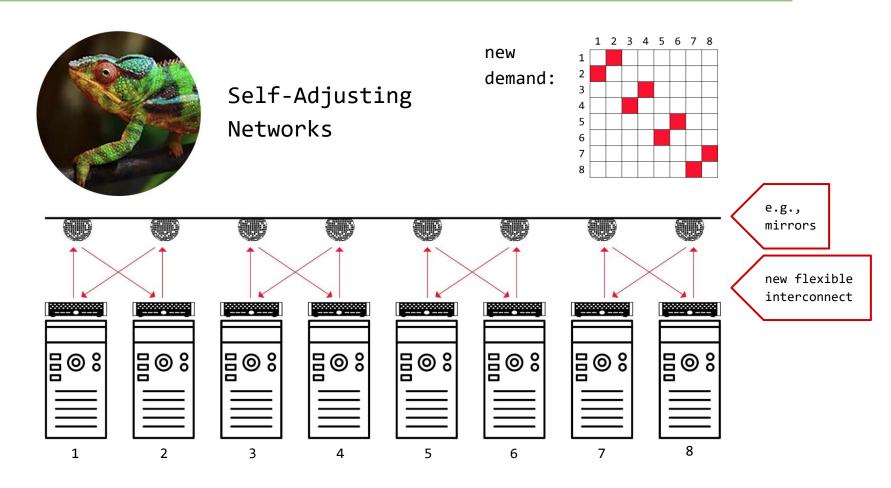










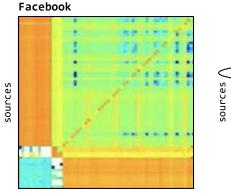


Our Motivation

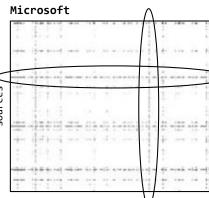
Much Structure in the Demand

Empirical studies:

traffic matrices sparse and skewed

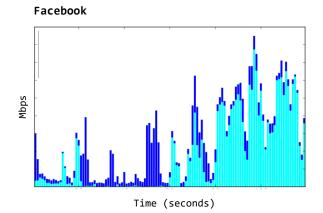


destinations



destinations

traffic bursty over time

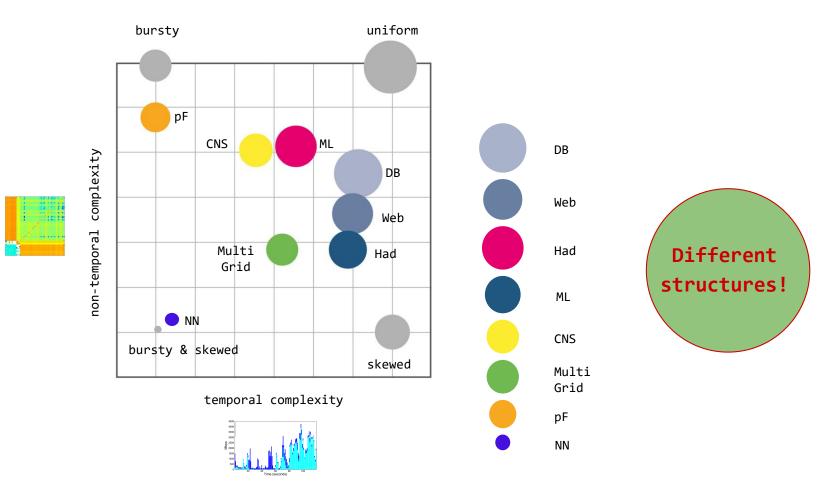


Our hypothesis: can be exploited.

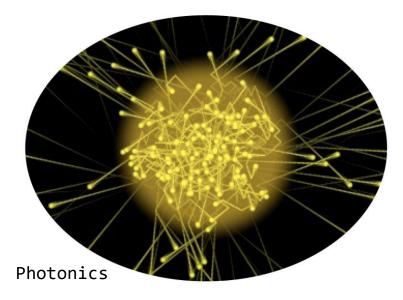
Recent Representation of Trace Structure: Complexity Map



Recent Representation of Trace Structure: Complexity Map



Sounds Crazy? Emerging Enabling Technology.



H2020:

"Photonics one of only five key enabling technologies for future prosperity."

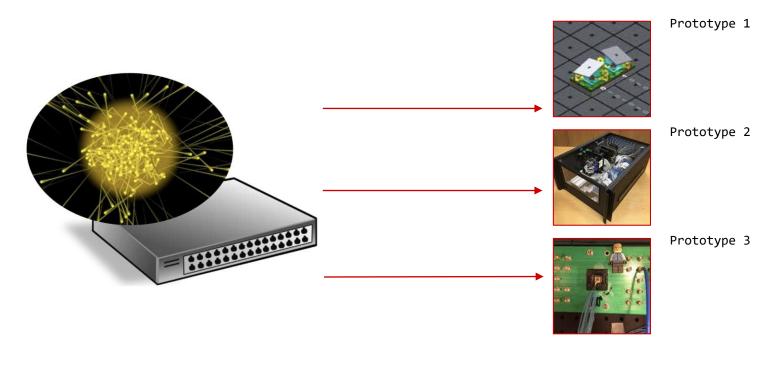
US National Research Council: "Photons are the new Electrons."

Enabler

Novel Reconfigurable Optical Switches

---> **Spectrum** of prototypes

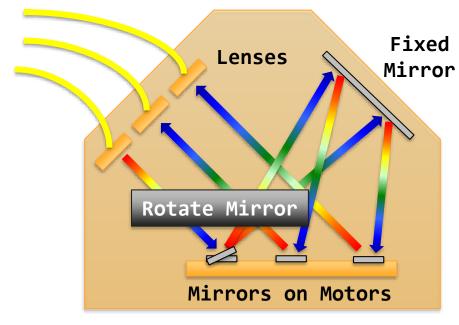
- \rightarrow Different sizes, different reconfiguration times
- → From our last year's ACM **SIGCOMM** workshop OptSys



Example

Optical Circuit Switch

---> Optical Circuit Switch rapid adaption of physical layer

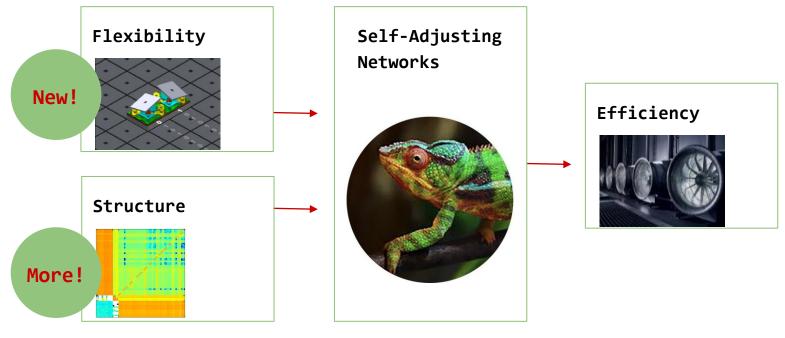


\rightarrow Based on rotating mirrors

Optical Circuit Switch

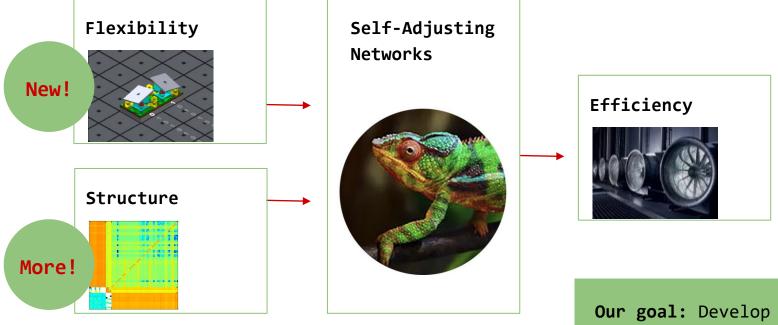
By Nathan Farrington, SIGCOMM 2010

The Big Picture



Now is the time!

The Big Picture

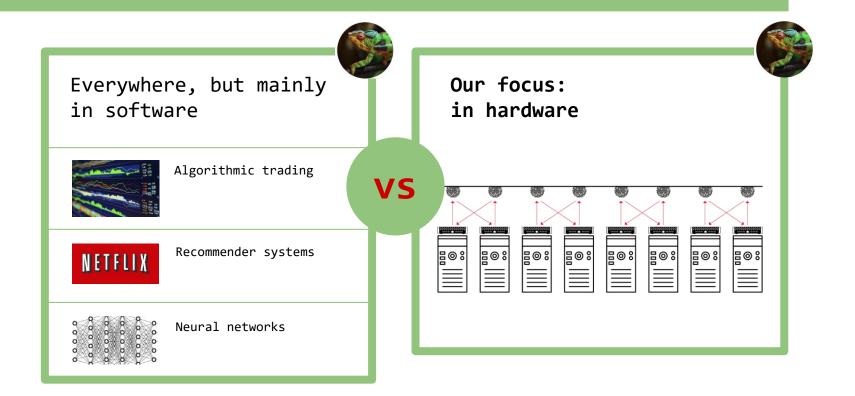


Now is the time!

Our goal: Develop the theoretical foundations of demand-aware, self-adjusting networks.

Unique Position

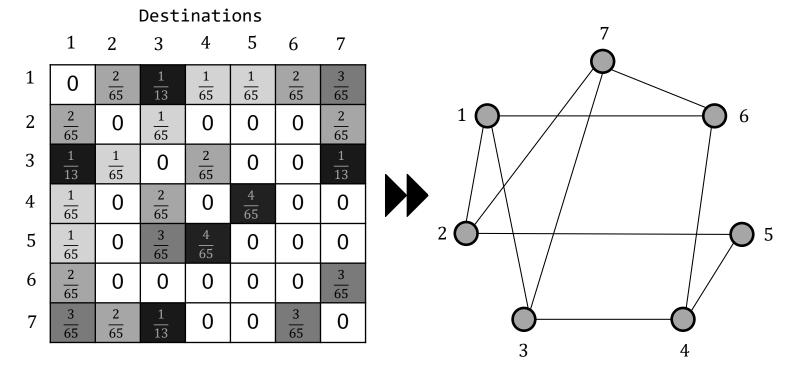
Demand-Aware, Self-Adjusting Systems



The Natural Question:

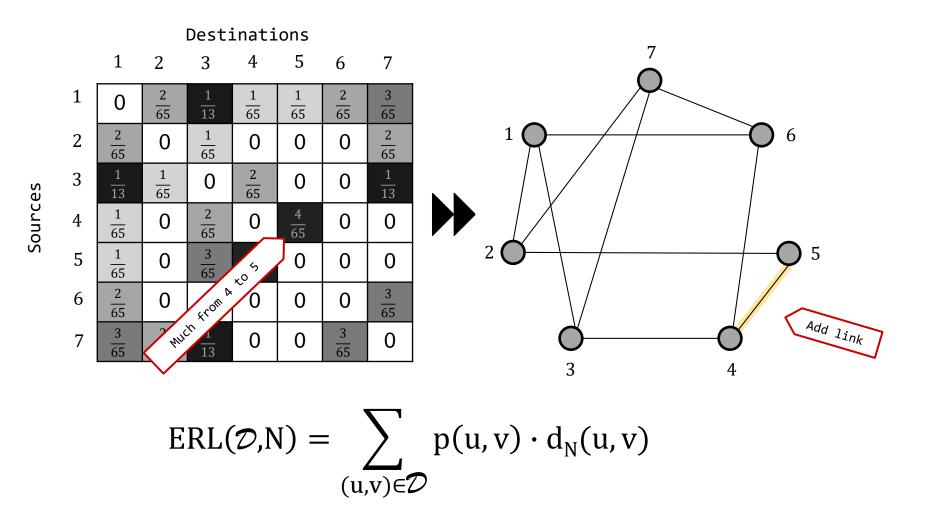
Given This Structure, What Can Be Achieved? Metrics and Algorithms?

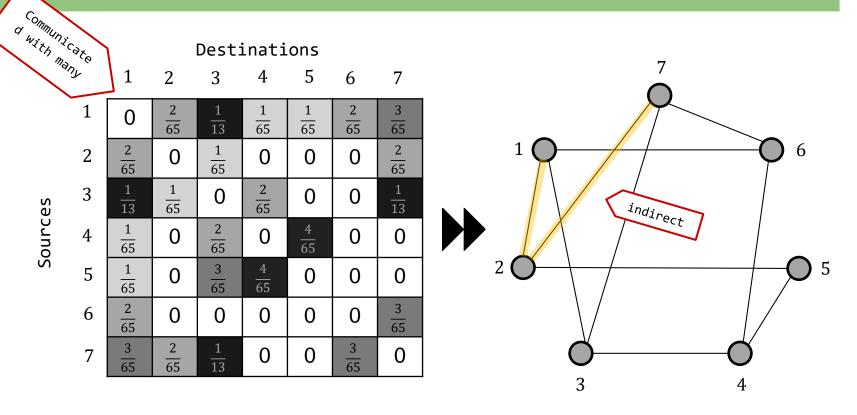
A first insight: entropy of the demand.



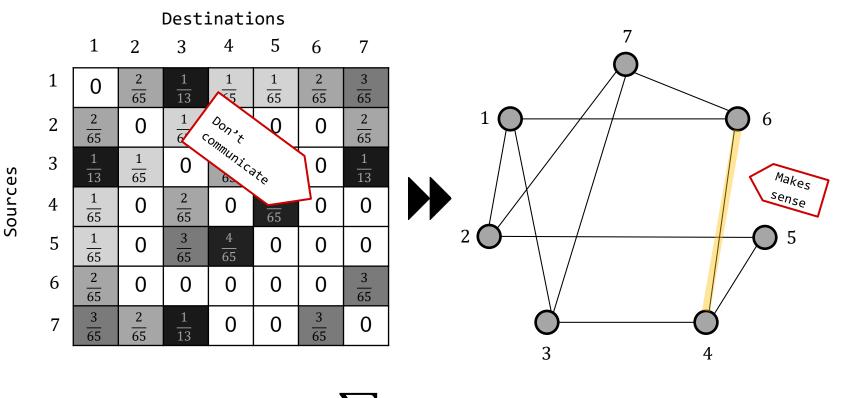
 $ERL(\mathcal{D},N) = \sum_{(u,v)\in\mathcal{D}} p(u,v) \cdot d_N(u,v)$

Sources



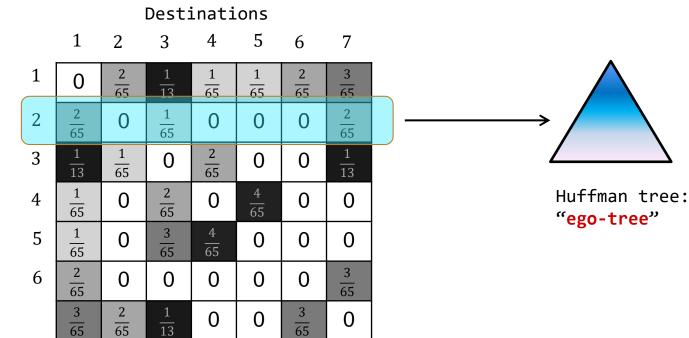


$$ERL(\mathcal{D},N) = \sum_{(u,v)\in\mathcal{D}} p(u,v) \cdot d_N(u,v)$$



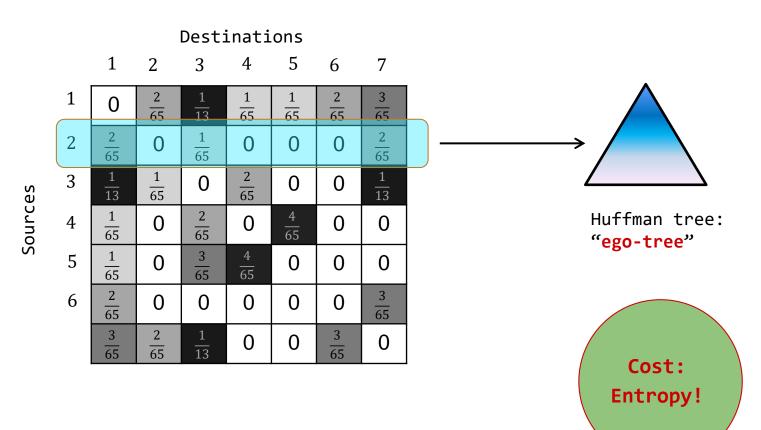
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Algorithm: Idea

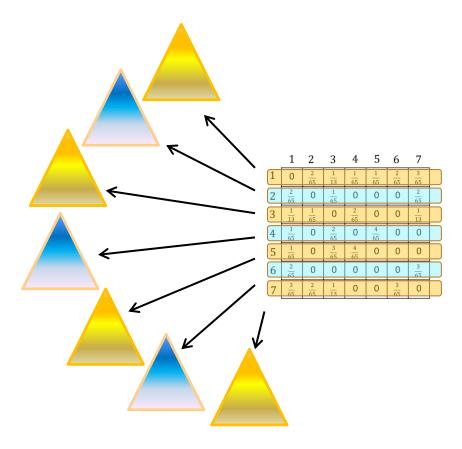


Sources

Algorithm: Idea

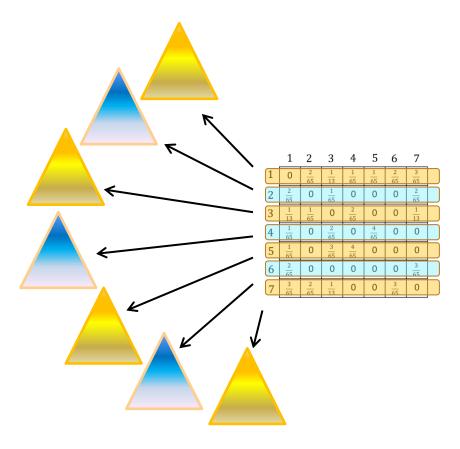


→ Idea for algorithm: → Union of trees

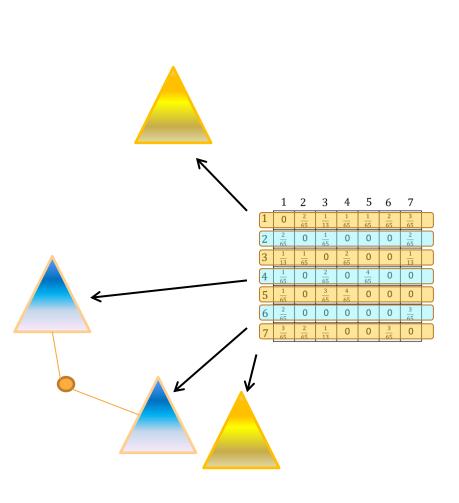


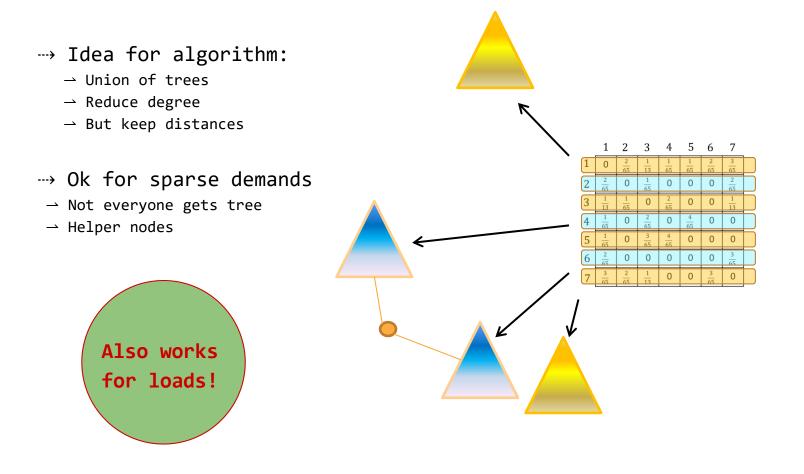
---> Idea for algorithm:

- \rightarrow Union of trees
- \rightarrow Reduce degree
- → But keep distances



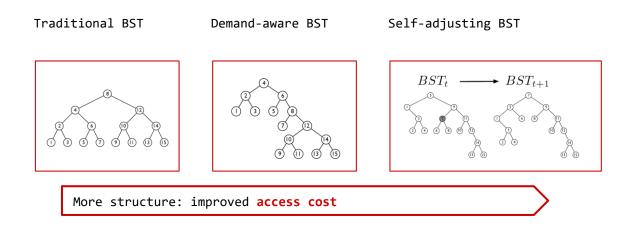
- ---> Idea for algorithm:
 - \rightarrow Union of trees
 - \rightarrow Reduce degree
 - → But keep distances
- ---> Ok for sparse demands
- \rightarrow Not everyone gets tree
- \rightarrow Helper nodes





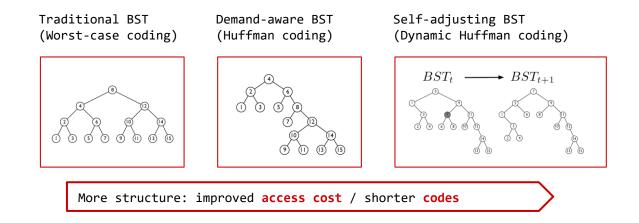
Our Insight:

Connection to Datastructures



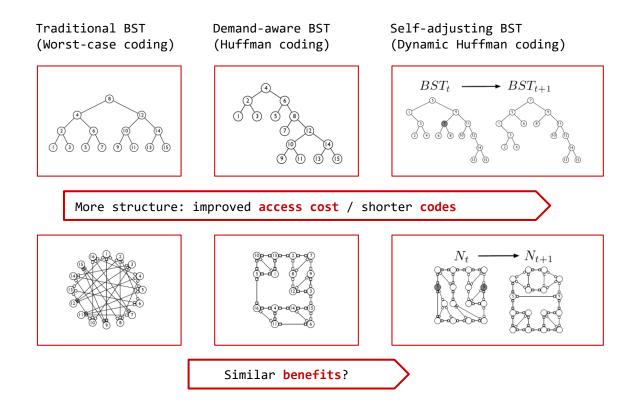
Our Insight:

Connection to Datastructures & Coding



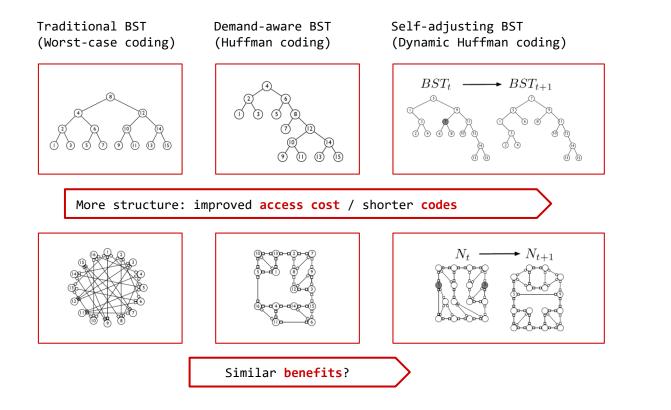
Our Insight:

Connection to Datastructures & Coding



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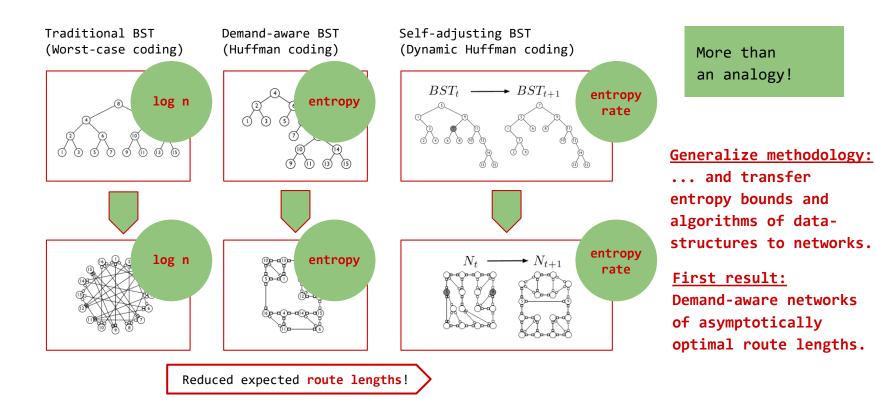
Connection to Datastructures & Coding



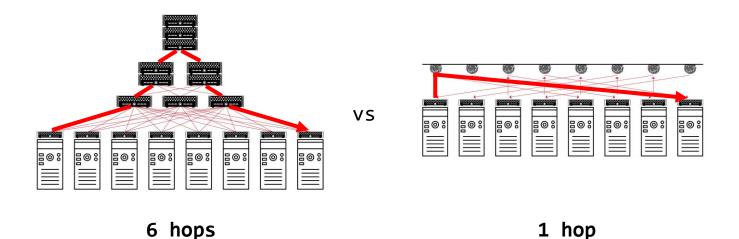
More than an analogy!

Our Insight:

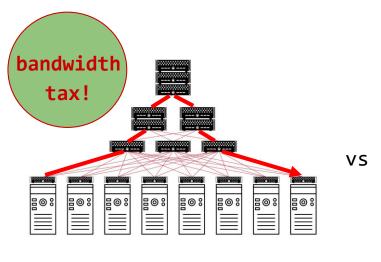
Connection to Datastructures & Coding

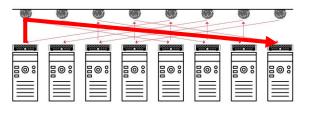


→ Self-adjusting networks may be really useful to serve large flows (elephant flows): avoiding multi-hop routing



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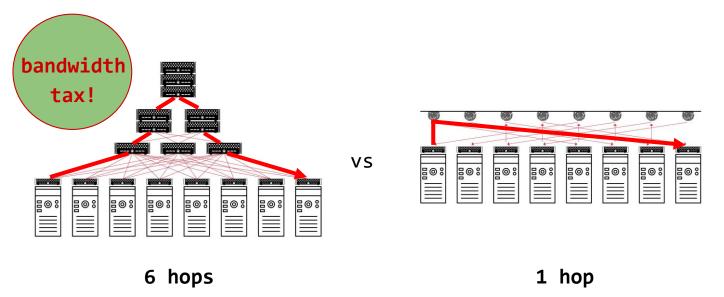




6 hops

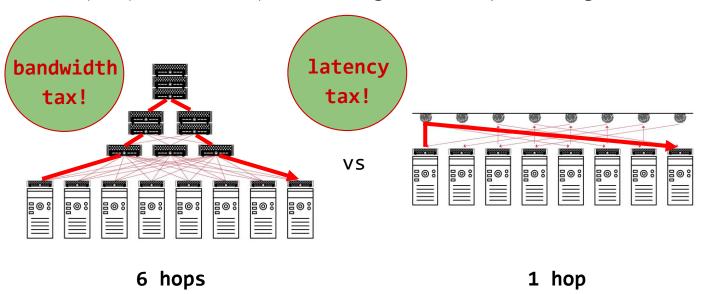
1 hop

→ Self-adjusting networks may be really useful to serve large flows (elephant flows): avoiding multi-hop routing



 \rightarrow However, requires optimization and adaption, which takes time

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Indeed, it is more complicated than that... Challenge: Traffic Diversity

Diverse patterns:

- → Shuffling/Hadoop: all-to-all
- → All-reduce/ML: ring or tree traffic patterns → Elephant flows
- → Query traffic: skewed → Mice flows
- → Control traffic: does not evolve but has non-temporal structure

Diverse requirements:

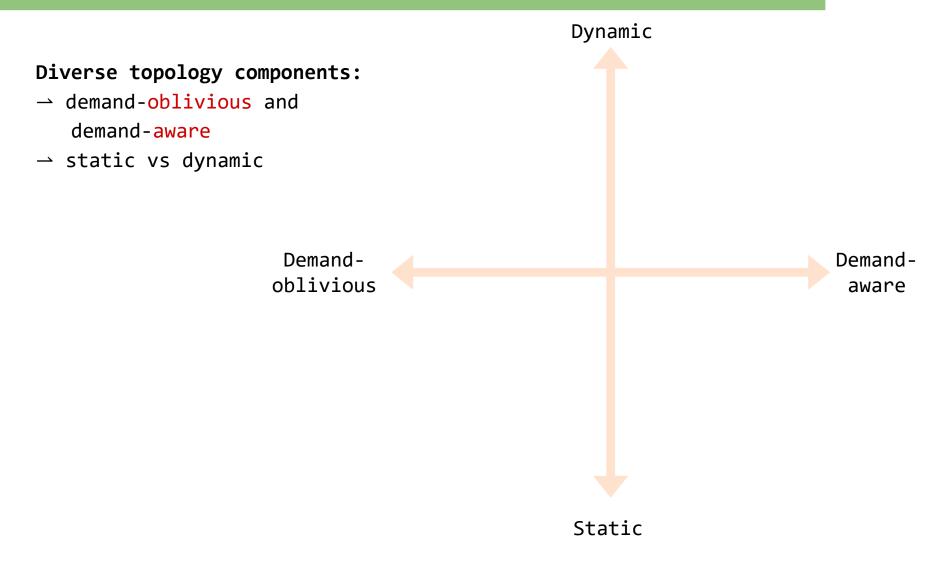
→ ML is bandwidth hungry, small flows are latencysensitive

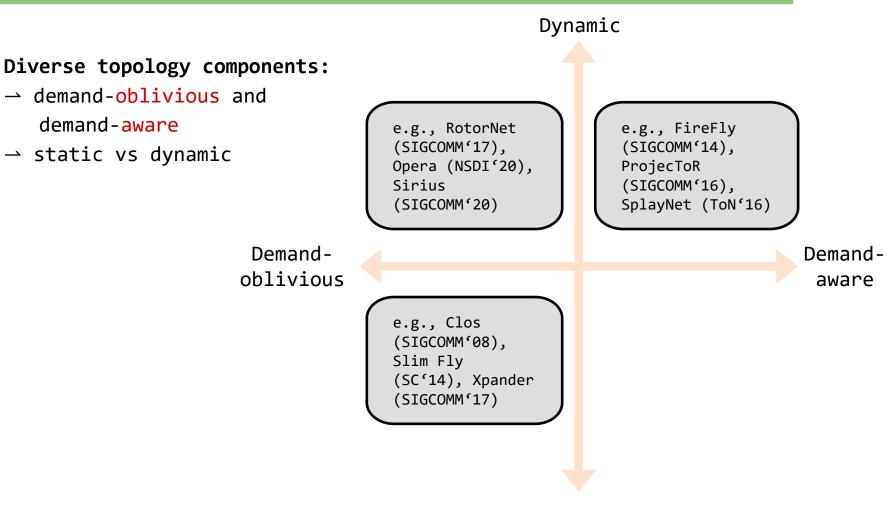


Diverse topology components:

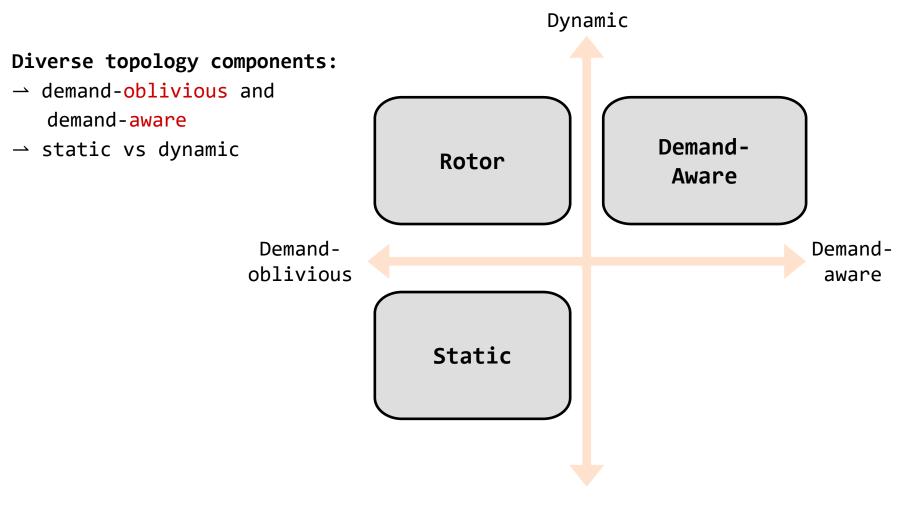
→ demand-oblivious and demand-aware

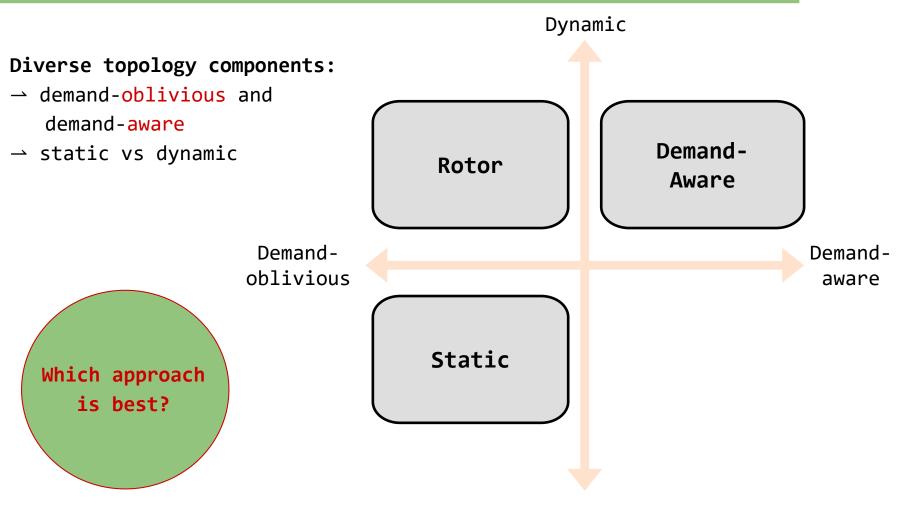
> Demandoblivious Demandaware

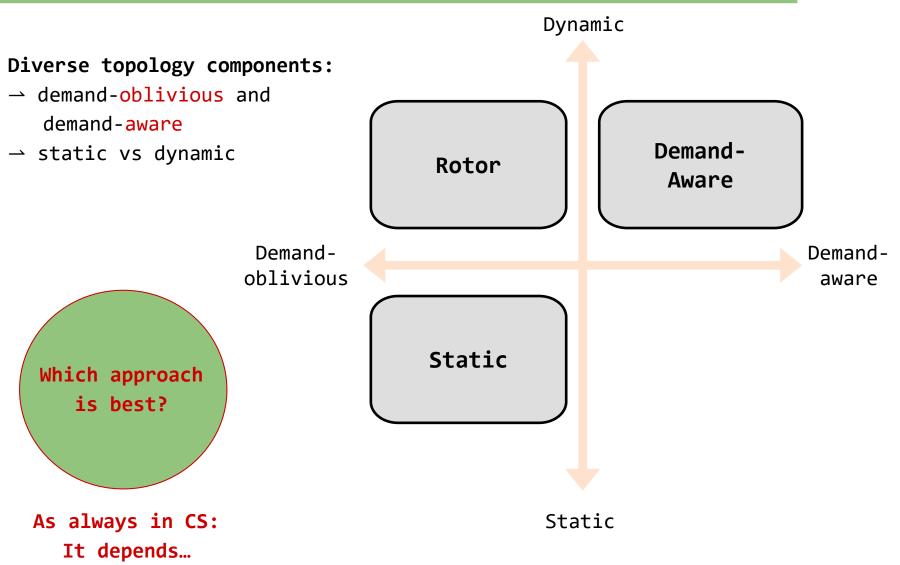




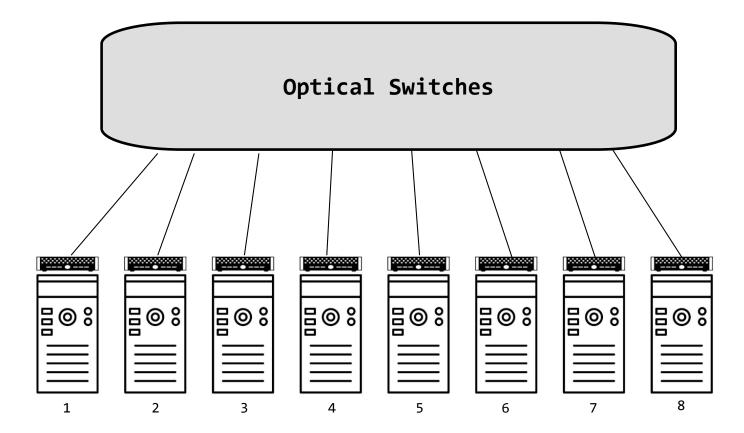
Static





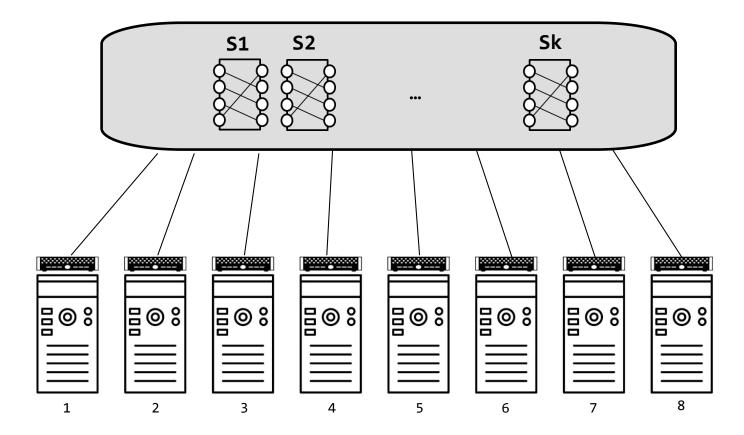


Rack Interconnect



Typical rack internconnect: ToR-Matching-ToR (TMT) model

Rack Interconnect

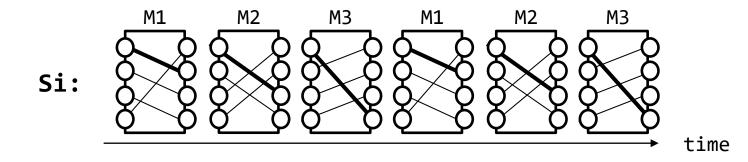


Typical rack internconnect: ToR-Matching-ToR (TMT) model

Details: Switch Types

Periodic Switch (aka Rotor Switch)

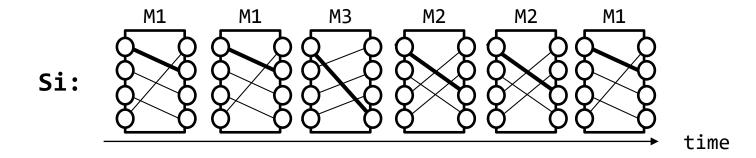
Rotor switch: periodic matchings (demand-oblivious)



Details: Switch Types

Demand-Aware Switch

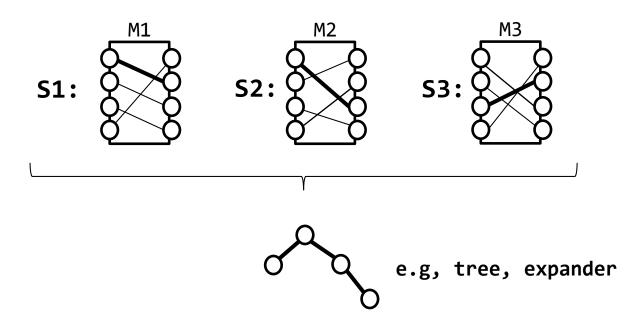
Demand-aware switch: optimized matchings



Details: Switch Types

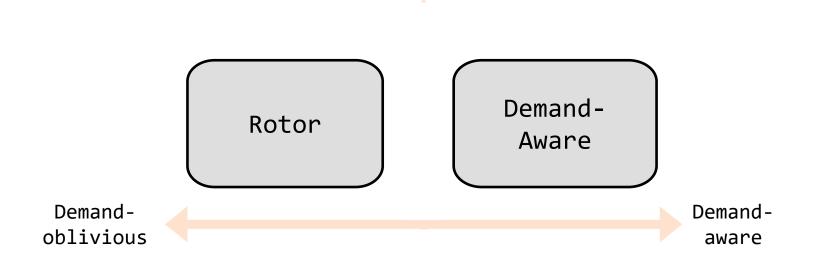
Static Switch

Static switches: combine for optimized static topology



Design Tradeoffs (1)

The "Awareness-Dimension"



Good for all-to-all traffic!

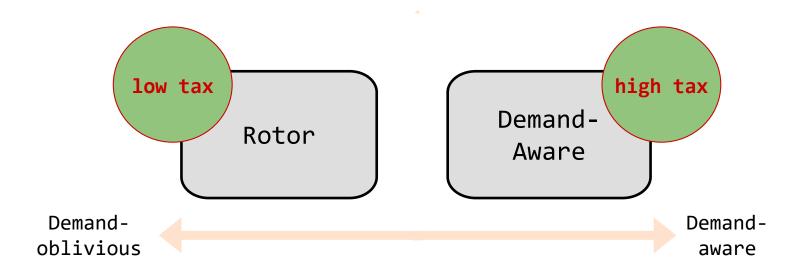
- → oblivious: very fast
 - periodic <mark>direct</mark> connectivity
- \rightarrow no control plane overhead

Good for elephant flows!

- → optimizable toward traffic
- \rightarrow but slower

Design Tradeoffs (1)

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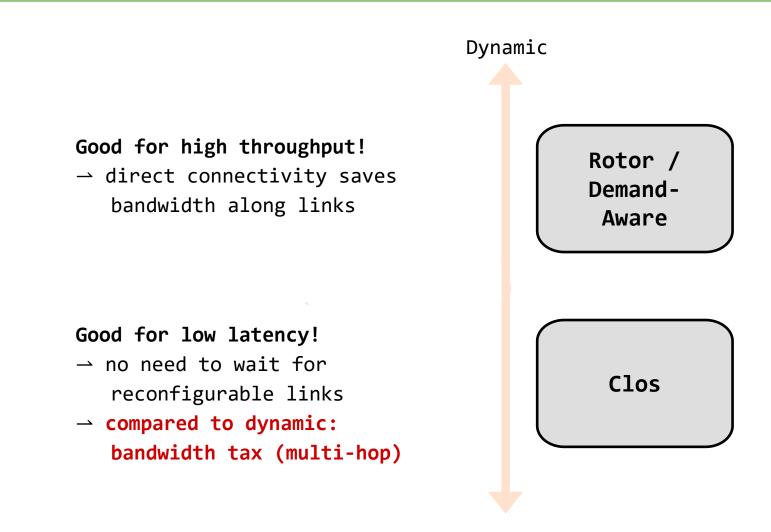
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Compared to static networks: latency tax!

Design Tradeoffs (2)

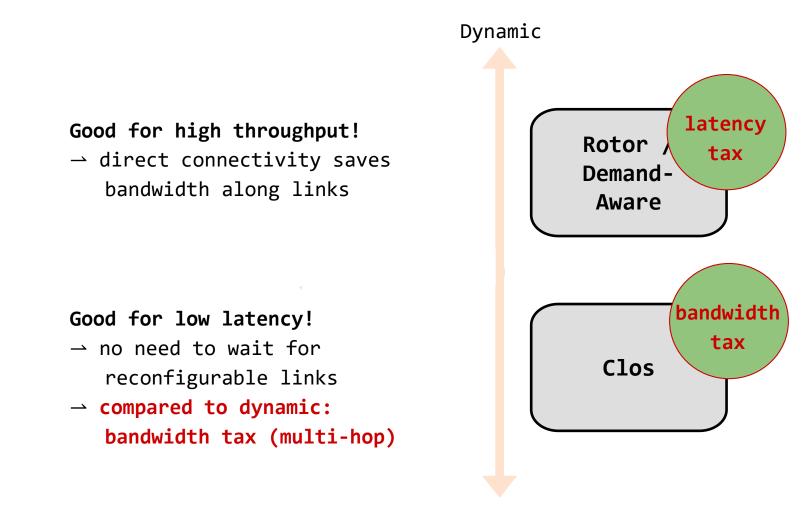
The "Flexibility-Dimension"



Static

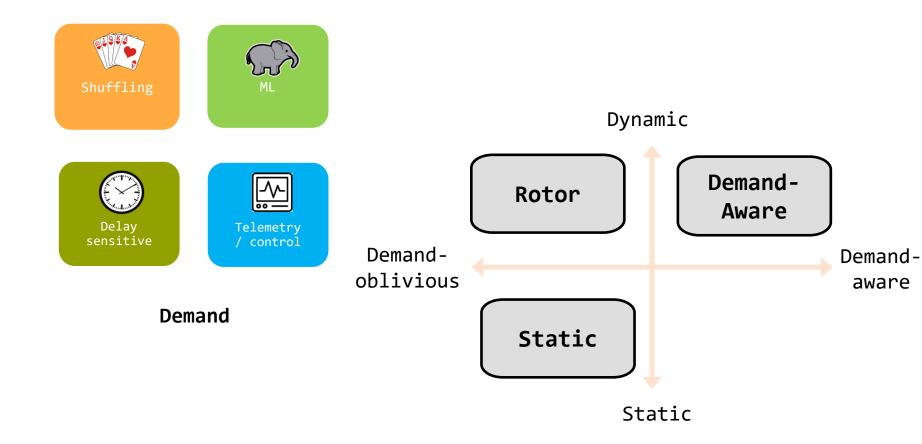
Design Tradeoffs (2)

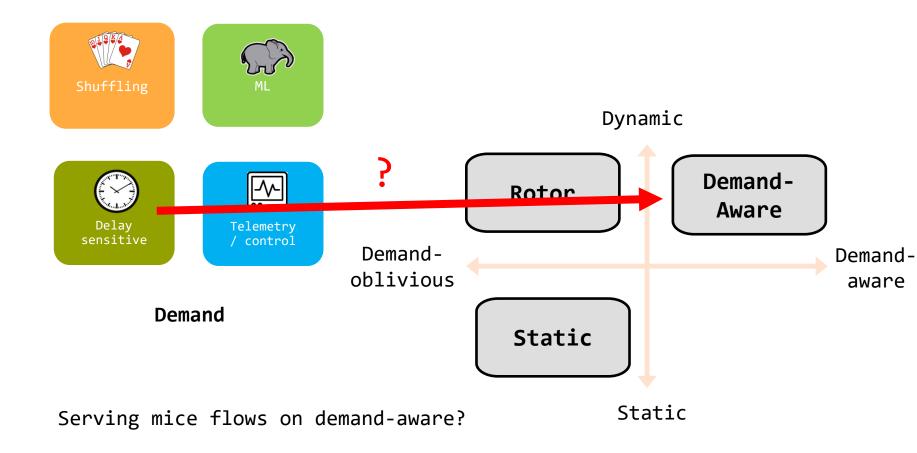
The "Flexibility-Dimension"

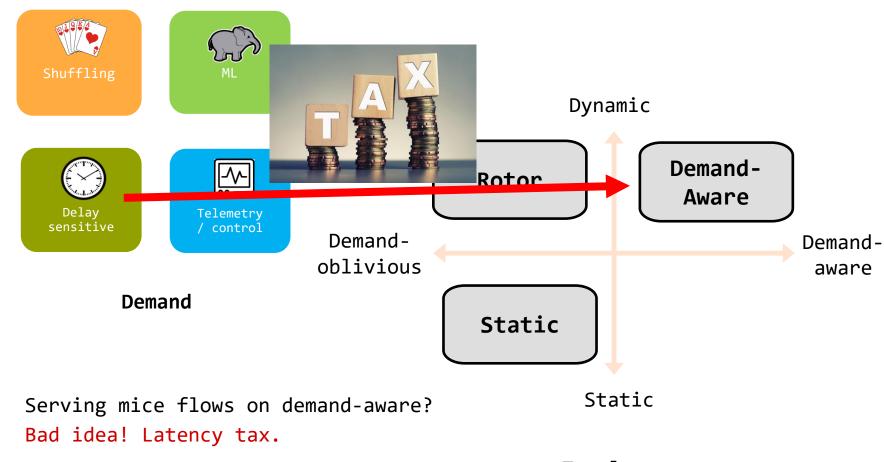


First Observations

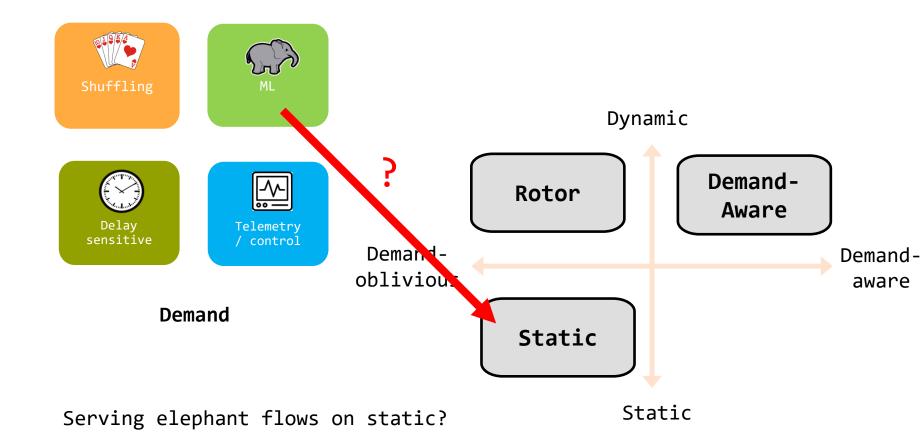
- ••• Observation 1: Different topologies provide different tradeoffs.
- ---> **Observation 2:** Different traffic requires different topology types.
- Observation 3: A mismatch of demand and topology
 can increase flow completion times.

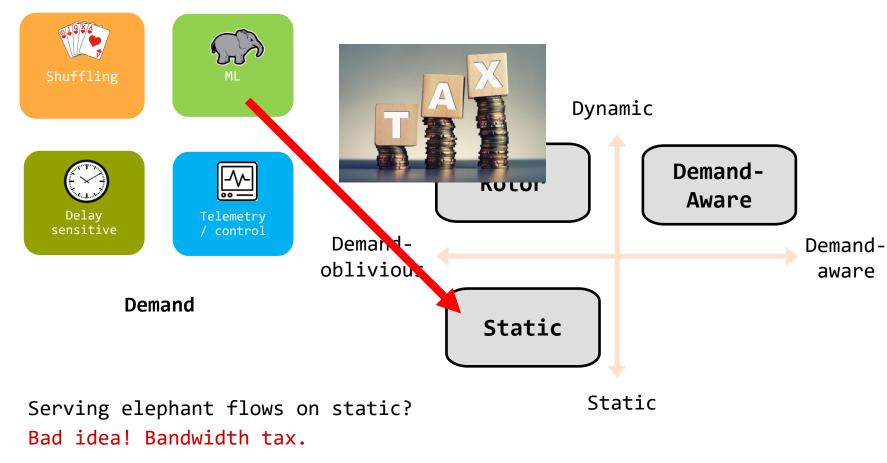






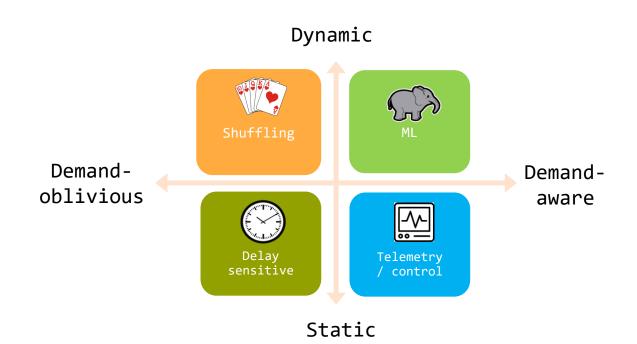
Topology





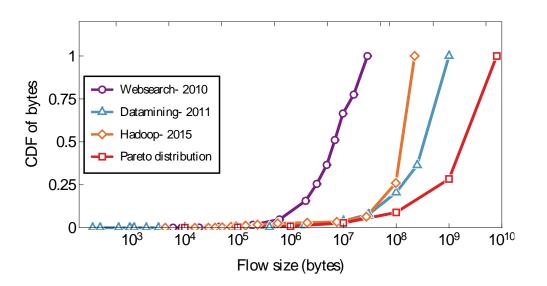
Topology

Cerberus: It's a Match!

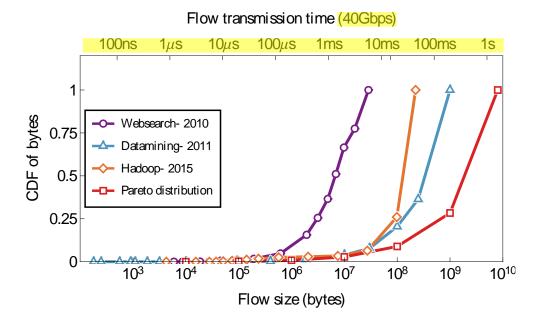


Our system Cerberus* serves traffic on the "best topology"!

* Griner et al., ACM SIGMETRICS 2022

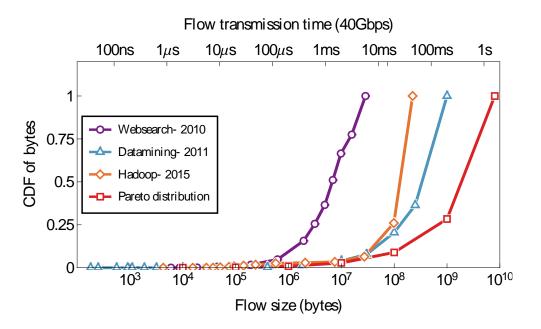


----> Observation 1: Different apps have different flow size distributions.

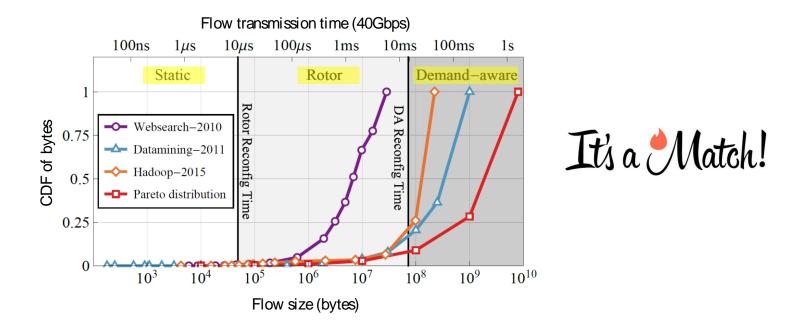


---> Observation 1: Different apps have different flow size distributions.

---- Observation 2: The transmission time of a flow depends on its size.



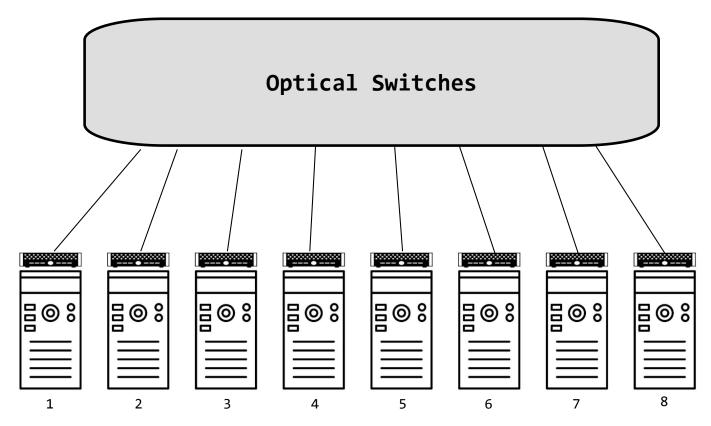
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- ••• Observation 3: For small flows, flow completion time suffers if network needs to be reconfigured first.
- ---> Observation 4: For large flows, reconfiguration time may amortize.



- ---> **Observation 1:** Different apps have different flow size distributions.
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- ••• Observation 3: For small flows, flow completion time suffers if network needs to be reconfigured first.
- ---> Observation 4: For large flows, reconfiguration time may amortize.

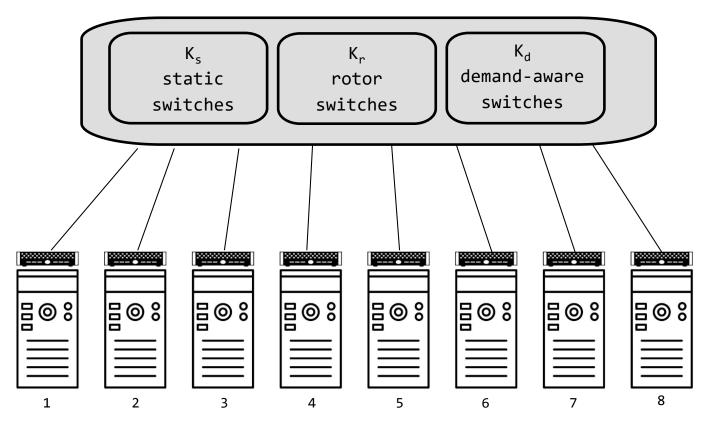






Cerberus

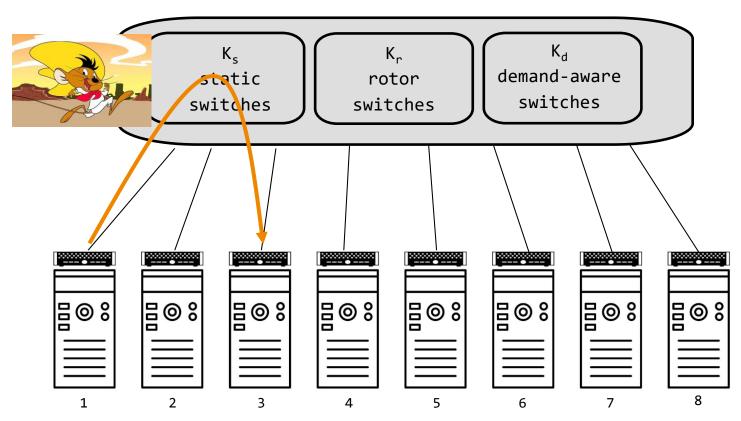




26

Cerberus

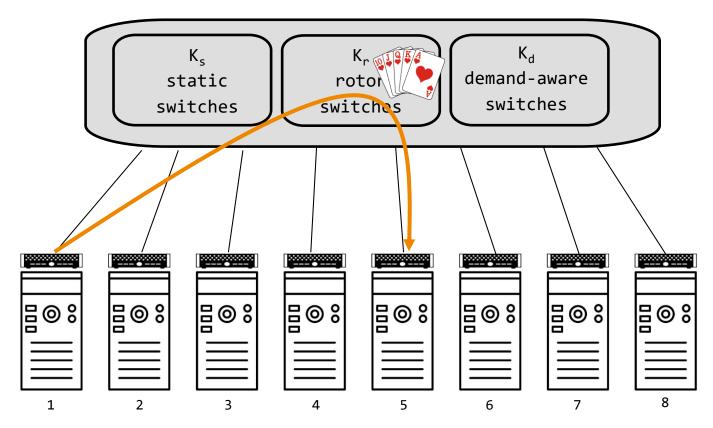




Scheduling: Small flows go via static switches...

Cerberus

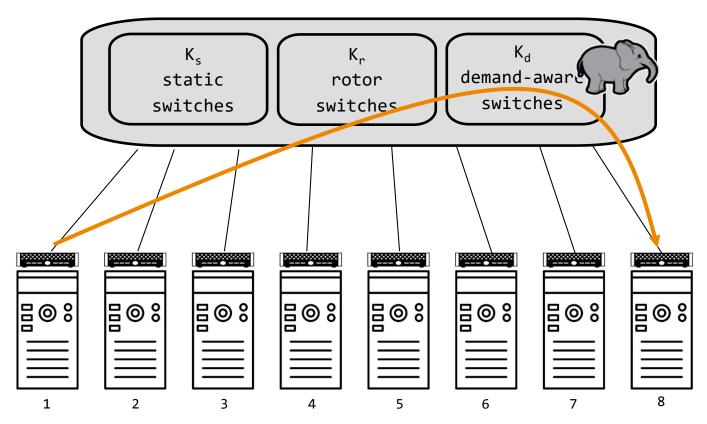




Scheduling: ... medium flows via rotor switches...

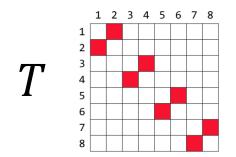
Cerberus





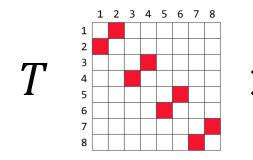
Scheduling: ... and large flows via demand-aware switches (if one available, otherwise via rotor).

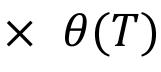
Demand Matrix



Metric: throughput of a demand matrix...

Demand Matrix

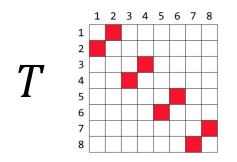




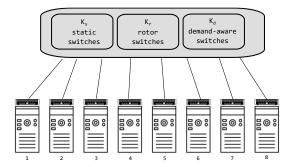
Metric:			throughput	
of	а	der	nand	matrix

... is the maximal scale down factor by which traffic is feasible.

Demand Matrix



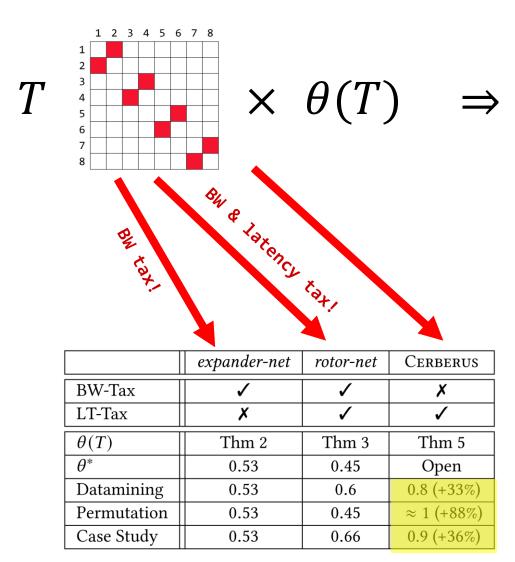
 $\times \theta(T) =$

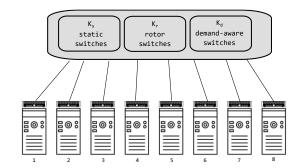


Metric: throughput of a demand matrix... ... is the maximal scale down factor by which traffic is feasible.

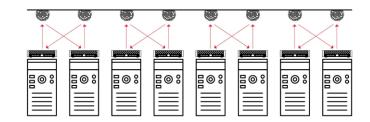
Throughput of network θ^* : worst case T

Demand Matrix





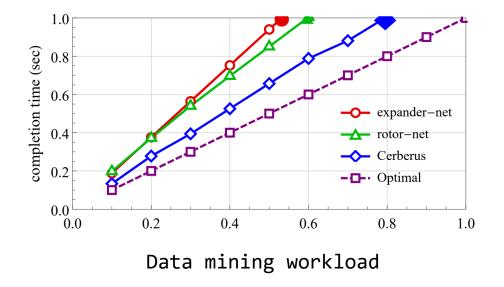
Worst demand matrix for static and rotor: permutation. Best case for demand-aware!





Completion Time

Demand completion time: How long does
it take to serve a demand matrix?



Also useful in analysis: throughput can be computed more easily via demand completion time.

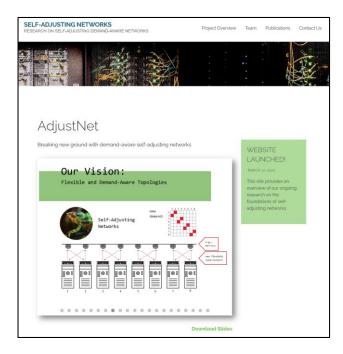
Conclusion

- Diverse traffic requires diverse technologies
- → Cerberus aims to assign traffic to its best topology → Depending on flow size
- ---> Many challenges
 - \rightharpoonup Impact on routing and congestion control
 - → Sensitivity analysis
 - → Prototyping



Thank you!

Websites



http://self-adjusting.net/ Project website



https://trace-collection.net/ Trace collection website

Further Reading

Static DAN

Demand-Aware Network Designs of Bounded Degree

Chen Avin Kaushik Mondal Stefan Schmid

Abstract Traditionally, networks such as datacenter 1 Introduction nterconnects are designed to optimize worst-case p formance under arbitrary traffic patterns. Such network signs can however be far from optimal when considering the actual workloads and traffic patterns which they serve. This insight led to the development of demandsare datacenter interconnects which can be reconfigured depending on the workload.

Motivated by these trends, this paper initiates the deorithmic study of demand-aware networks (DANs). and in particular the design of bounded-degree networks. The inputs to the network design problem are a liscrete communication request distribution, D, defined ver communicating pairs from the node set V, and a bound, Δ , on the maximum degree. In turn, our obective is to design an (undirected) demand-aware network N = (V, E) of bounded-degree Δ , which provides short routing paths between frequently communicating nodes distributed across N. In particular, the designed network should minimize the expected path length on Nwith respect to D, which is a basic measure of the

The problem studied in this paper is motivated by the advent of more flexible datacenter interconnects, such as ProjecToR [29,31]. These interconnects aim to overcome a fundamental drawback of traditional datacenter network designs: the fact that network designers must decide in advance on how much capacity to provision between electrical packet switches, e.g., between Topof-Rack (ToR) switches in datacenters. This leads to an undesirable tradeoff [42]: either capacity is overprovisioned and therefore the interconnect expe-(e.g., a fat-tree provides full-bisection bandwidth), or one may risk congestion, resulting in a poor cloud appli cation performance. Accordingly, systems such as ProjecToR provide a reconfigurable interconnect, allowing to establish links flexibly and in a demand-aware manner. For example, direct links or at least short commu nication paths can be established between frequently communicating ToR switches. Such links can be implemented using a bounded number of lasers, mirrors

Robust DAN

rDAN: Toward Robust Demand-Aware Network Designs

Chen Avin¹ Alexandr Hercules¹ Andreas Loukas² Stefan Schmid³ ¹ Ben-Gurion University, IL ² EPFL, CH ³ University of Vienna, AT & TU Berlin, DE

Abstract

We currently witness the emergence of interesting new network topologies optimized towards the traffic matrices they serve, such as demand-aware datacenter interconnects (e.g., ProjecToR) and demand-aware peer-to-peer overlay networks (e.g., SplayNets). This paper introduces a format framework and approach to reason about and design robust demand-aware networks (DAN). In particular, we establish a connection between the communication frequency of two nodes and the path length between them in the network, and show that this relationship depends on the entropy of the communication matrix. Our main contribution is a novel robust, yet sparse, family of networks, short rDANs, which guarantee an expected path length that is proportional to the entropy of the communication patterns

Overview: Models

Toward Demand-Aware Networking: A Theory for Self-Adjusting Networks

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This article is an editorial note submitted to CCR. It has NOT been peer reviewed. The authors take full responsibility for this article's technical content. Comments can be posted through CCR Online

ABSTRACT

The physical topology is emerging as the next frontier in an ongoing effort to render communication networks more flexible. While first empirical results indicate that these flexibilities can be exploited to reconfigure and optimize the network toward the workload it serves and, e.g., providing the same bandwidth at lower infrastructure cost, only little is known today about the fundamental algorithmic problems underlying the design of reconfigurable networks. This paper initiates the study of the theory of demand-aware, self-adjusting networks. Our main position is that self-adjusting networks should be seen through the lense of self-adjusting datastructures. Accordingly, we present a taxonomy classifying the different algorithmic models of demand-oblivious, fixed demand-aware, and reconfigurable demand-aware networks, introduce a formal model, and identify objectives and evaluaon metrics. We also demonstrate, by examples, the inheren



Figure 1: Taxonomy of topology optimization

design of efficient datacenter networks has received much attention over the last years. The topologies underlying modern datacenter networks range from trees [7, 8] over hypercubes [9, 10] to expander networks [11] and provide high connectivity at low cost [1]. Until now, these networks also have in common that their topology is *fixed* and *oblivious* to the actual demand (i.e.,

Dynamic DAN

SplayNet: Towards Locally Self-Adjusting Networks

Stefan Schmid*, Chen Avin*, Christian Scheideler, Michael Borokhovich, Bernhard Haeupler, Zvi Lotker

Abstract—This paper initiates the study of bacily self: toward static metrics, such as the diameter or the length of igniting networks three topology adapts dynamically in the longest route; the self-adjusting paradigm has not spilled and in a decentralized manner, to the communication pattern σ . Or vision can be seen as a distributed generalization of the distributed networks yet. Our vision can be seen as a distributed generalization of the distributed networks yet. The initial the study of a distributed generalization of the distributed networks yet. In this paper, initiate the study of a distributed generalization of the distributed interview. This is a non-trivial network was the distributed parameter of the distributed of experiment of the distributed distributed generalization of the distributed is non-trivial study of a distributed dis lookup costs from a single node (namely the tree root), we seek to minimize the routing cost between arbitrary communication pairs in the network.

pairs in the network. As a first step, we study distributed binary search trees (BSTs), which are attractive for their support of greedy routing, We introduce a simple model which captures the fundamental tradeoff between the benefits and costs of self-adjusting networks, We present the SplayNet algorithm and formally analyze its we present the spany-ter augorithm and normany analyze its performance, and prove its optimility in specific case studies. We also introduce lower bound techniques based on interval cuts and edge expansion, to study the limitations of any demand-optimized network. Finally, we extend our study to multi-tree networks, and highlight an intriguing difference between classic and distributed splay trees.

I. INTRODUCTION

In the 1980s, Sleator and Tarjan [22] proposed an appealing new paradigm to design efficient Binary Search Tree (BST) datastructures: rather than optimizing traditional metrics such

generalization of the classic splay tree concept: While in classic BSTs, a lookup request always originates from the same node, the tree root, distributed datastructures and networks

such as skip graphs [2], [13] have to support routing requests between arbitrary pairs (or peers) of communicating nodes; in other words, both the source as well as the destination of the requests become variable. Figure 1 illustrates the difference between classic and distributed binary search trees. In this paper, we ask: Can we reap similar benefits from self-

adjusting entire networks, by adaptively reducing the distance between frequently communicating nodes?

As a first step, we explore fully decentralized and self-adjusting Binary Search Tree networks: in these networks, nodes are arranged in a binary tree which respects node identifiers. A BST topology is attractive as it supports greedy routing: a node can decide locally to which port to forward a request given its destination address

Static Optimality

ReNets: Toward Statically Optimal Self-Adjusting Networks

Chen Avin¹ Stefan Schmid² ¹ Ben Gurion University, Israel ² University of Vienna, Austria

Abstract

This paper studies the design of *self-adjusting* networks whose topology dynamically adapts to the workload, in an online and demand-aware manner. This problem is motivated by emerging optical technologies which allow to reconfigure the datacenter topology at runtime. Our main contribution is *ReNet*, a self-adjusting network which maintains a balance between the benefits and costs of reconfigurations. In particular, we show that ReNets are statically optimal for arbitrary sparse communication demands, i.e., perform at least as good as any fixed demand-aware network designed with a perfect knowledge of the future demand. Furthermore, ReNets provide compact and local routing, by leveraging ideas from self-adjusting datastructures.

1 Introduction

Modern datacenter networks rely on efficient network topologies (based on fat-trees [1], hypercubes [2, 3], or expander [4] graphs) to provide a high connectivity at low cost [5]. These datacenter networks have in common that their topology is fixed and oblivious to the actual demand (i.e., workload or communication pattern) they currently serve. Rather, they are designed for all-to-all communication patterns, by ensuring properties such as full bisection bandwidth or $O(\log n)$ route lengths between any node pair in a constant-degree n-node network. However, demand-oblivious networks can be inefficient for more *specific* demand patterns, as they usually arise in

Concurrent DANs

CBNet: Minimizing Adjustments in Concurrent Demand-Aware Tree Networks

Otavio Augusto de Oliveira Sonza¹ Olga Goussevskaja¹ Stefan Schmid² Universidade Federal de Minas Gerais, Brazil ² University of Vienna, Austria

Advance—This paper studies the datage of denames servers thereas the pledge servers, the ad streamest shared the merrors toward the denamed they currently international single fiberations that denamest servers in the pledge streamest servers that denamest servers international single fiberations that denamest servers international single fiberations that denamest servers international single fiberations that constructions are server at the servers international single fiberations att constructions, a constrained constrainer of used nations att constructions, a constrained constrainer of used nations processes a biological single single

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SplayNet: Towards Locally Self-Adjusting Networks

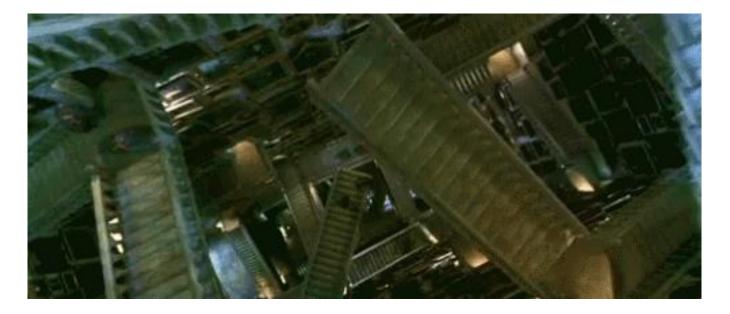
Stefan Schmid, Chen Avin, Christian Scheideler, Michael Borokhovich, Bernhard Haeupler, and Zvi Lotker.

IEEE/ACM Transactions on Networking (TON), Volume 24, Issue 3, 2016. Early version: IEEE IPDPS 2013.

Characterizing the Algorithmic Complexity of Reconfigurable Data Center Architectures Klaus-Tycho Foerster, Monia Ghobadi, and Stefan Schmid.

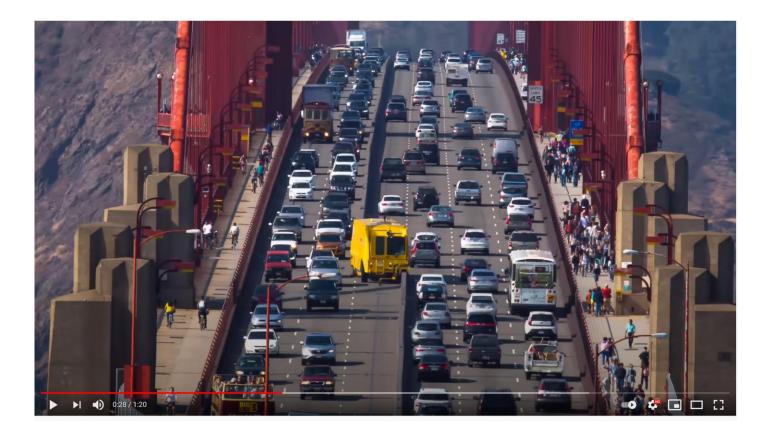
ACM/IEEE Symposium on Architectures for Networking and Communications Systems (ANCS), Ithaca, New York, USA, July 2018.

Bonus Material



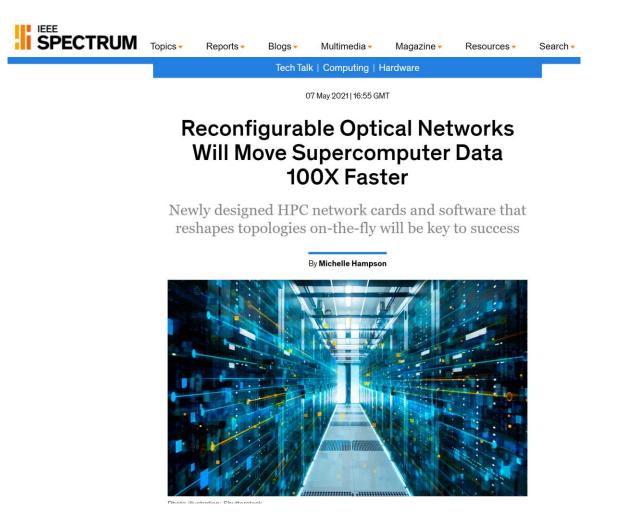
Hogwarts Stair

Bonus Material



Golden Gate Zipper

Bonus Material



In HPC

Question:

How to Quantify such "Structure" in the Demand?

Which demand has more structure?

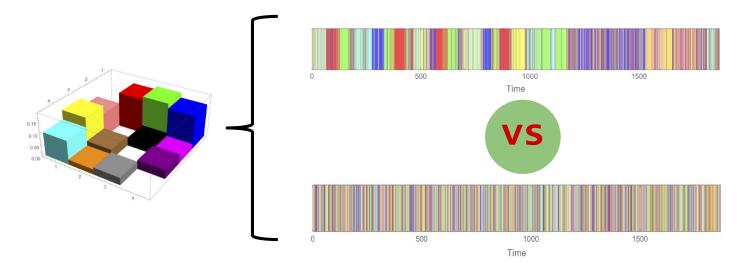
Which demand has more structure?

More uniform

More structure

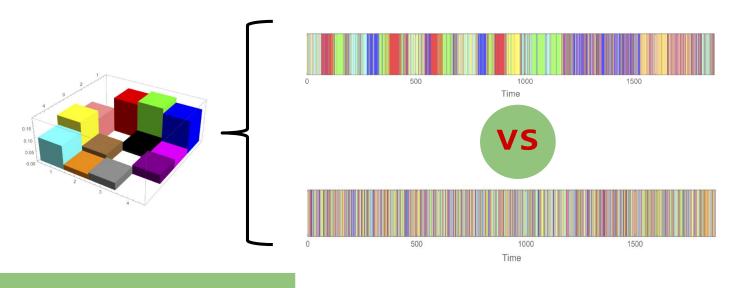
Spatial vs temporal structure

- ---> Two different ways to generate same traffic matrix:
 - \rightarrow Same non-temporal structure
- ---> Which one has more structure?

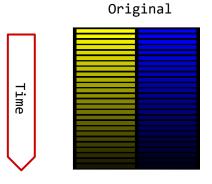


Spatial vs temporal structure

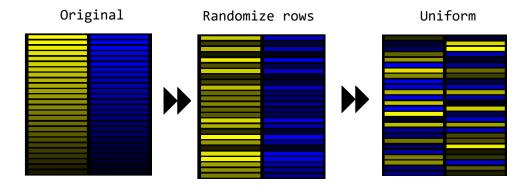
- ---> Two different ways to generate same traffic matrix:
 - \rightarrow Same non-temporal structure
- ---> Which one has more structure?



Systematically?

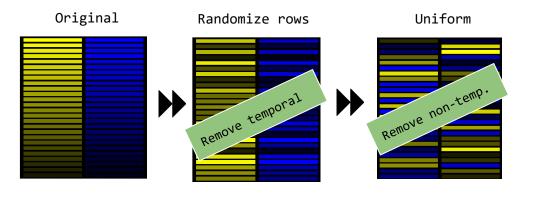


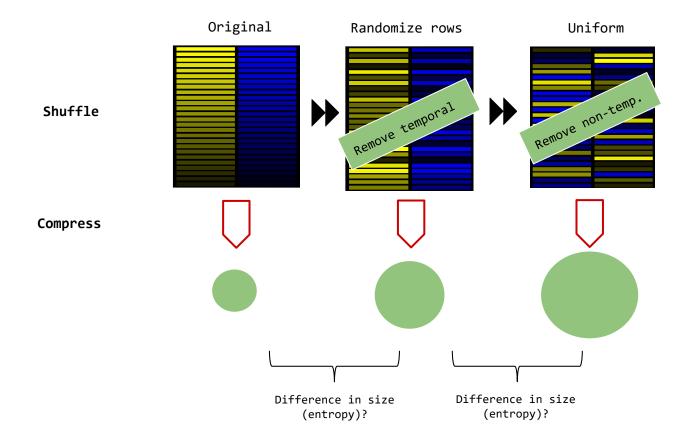
Information-Theoretic Approach
"Shuffle&Compress"

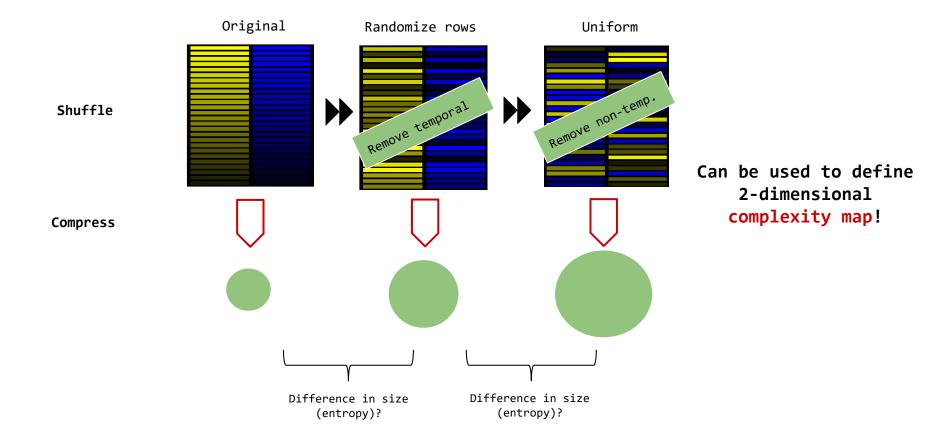


Increasing complexity (systematically randomized)

More structure (compresses better)

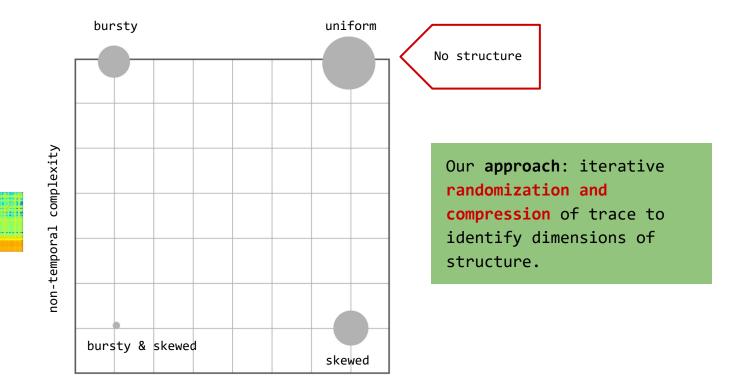




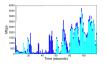


Our Methodology

Complexity Map

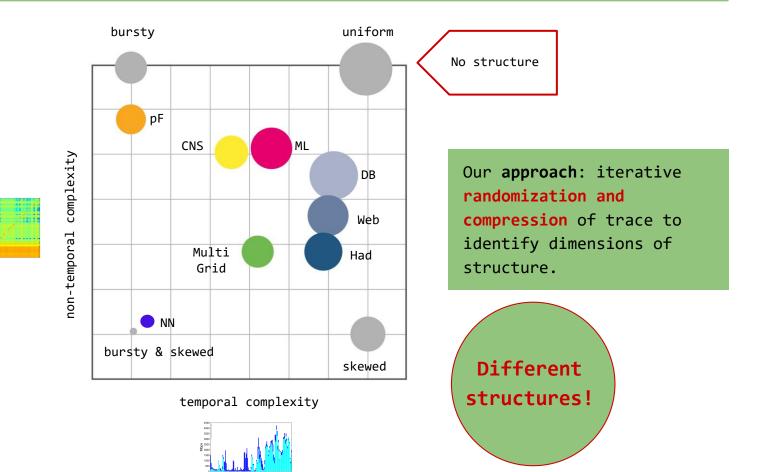


temporal complexity



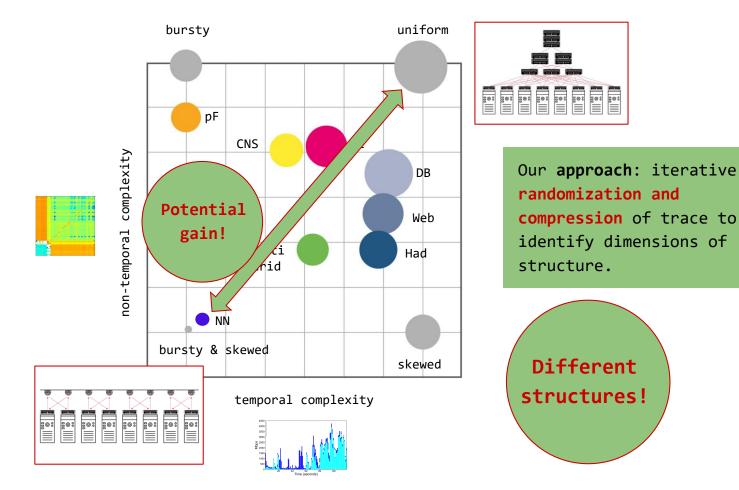
Our Methodology

Complexity Map



Our Methodology

Complexity Map



Further Reading

ACM SIGMETRICS 2020

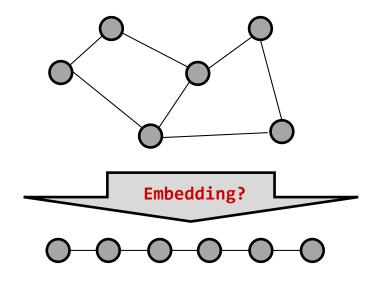
On the Complexity of Traffic Traces and Implications CHEN AVIN, School of Electrical and Computer Engineering, Ben Gurion University of the Negev, Israel MANYA GHOBADI, Computer Science and Artificial Intelligence Laboratory, MIT, USA CHEN GRINER, School of Electrical and Computer Engineering, Ben Gurion University of the Negey, Israel STEFAN SCHMID, Faculty of Computer Science, University of Vienna, Austria This paper presents a systematic approach to identify and quantify the types of structures featured by packet traces in communication networks. Our approach leverages an information-theoretic methodology, based on iterative randomization and compression of the packet trace, which allows us to systematically remove and measure dimensions of structure in the trace. In particular, we introduce the notion of trace complexity which approximates the entropy rate of a packet trace. Considering several real-world traces, we show that trace complexity can provide unique insights into the characteristics of various applications. Based on our approach, we also propose a traffic generator model able to produce a synthetic trace that matches the complexity levels of its corresponding real-world trace. Using a case study in the context of datacenters, we show that insights into the structure of packet traces can lead to improved demand-aware network designs: datacenter topologies that are optimized for specific traffic patterns. CCS Concepts: • Networks \rightarrow Network performance evaluation; Network algorithms; Data center **networks**; • Mathematics of computing \rightarrow Information theory; Additional Key Words and Phrases: trace complexity, self-adjusting networks, entropy rate, compress, complexity map, data centers **ACM Reference Format:** Chen Avin, Manya Ghobadi, Chen Griner, and Stefan Schmid. 2020. On the Complexity of Traffic Traces and Implications. Proc. ACM Meas. Anal. Comput. Syst. 4, 1, Article 20 (March 2020), 29 pages. https://doi.org/10.

1145/3379486

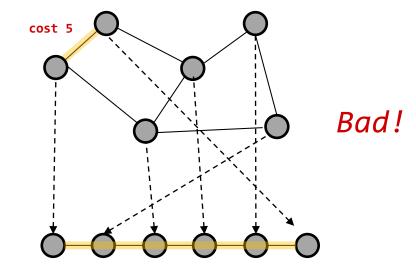
1 INTRODUCTION

Packet traces collected from networking applications, such as datacenter traffic, have been shown to feature much structure: datacenter traffic matrices are sparse and skewed [16, 39], exhibit 20

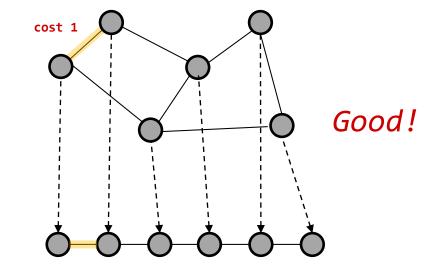
Example △=2: A Minium Linear Arrangement (MLA) Problem → Minimizes sum of virtual edges



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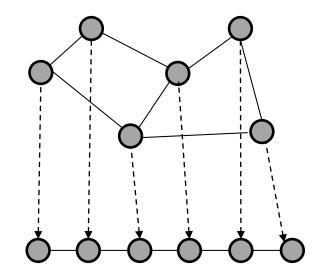


Related Problem

Virtual Network Embedding Problem (VNEP)

Example △=2: A Minium Linear Arrangement (MLA) Problem → Minimizes sum of virtual edges

MLA is NP-hard → … and so is our problem!



Example △=2: A Minium Linear Arrangement (MLA) Problem → Minimizes sum of virtual edges

MLA is **NP-hard**

 \rightarrow ... and so is our problem!

But what about $\triangle>2$?

- \rightarrow Embedding problem still hard
- → But we have a new degree of freedom!

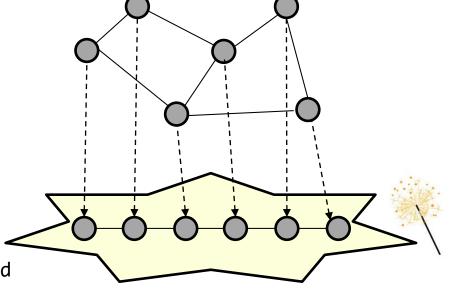
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MLA is **NP-hard**

 \rightarrow ... and so is our problem!

But what about $\triangle > 2$?

- \rightarrow Embedding problem still hard
- → But we have a new degree of freedom!



Simplifies problem?!