

Dynamic FIB Aggregation without Update Churn

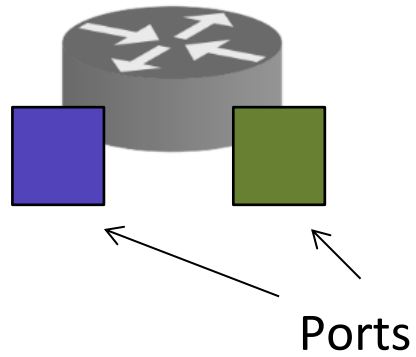
Dynamic FIB Aggregation without Update Churn



Marcin Bienkowski
Nadi Sarrar
Stefan Schmid
Steve Uhlig

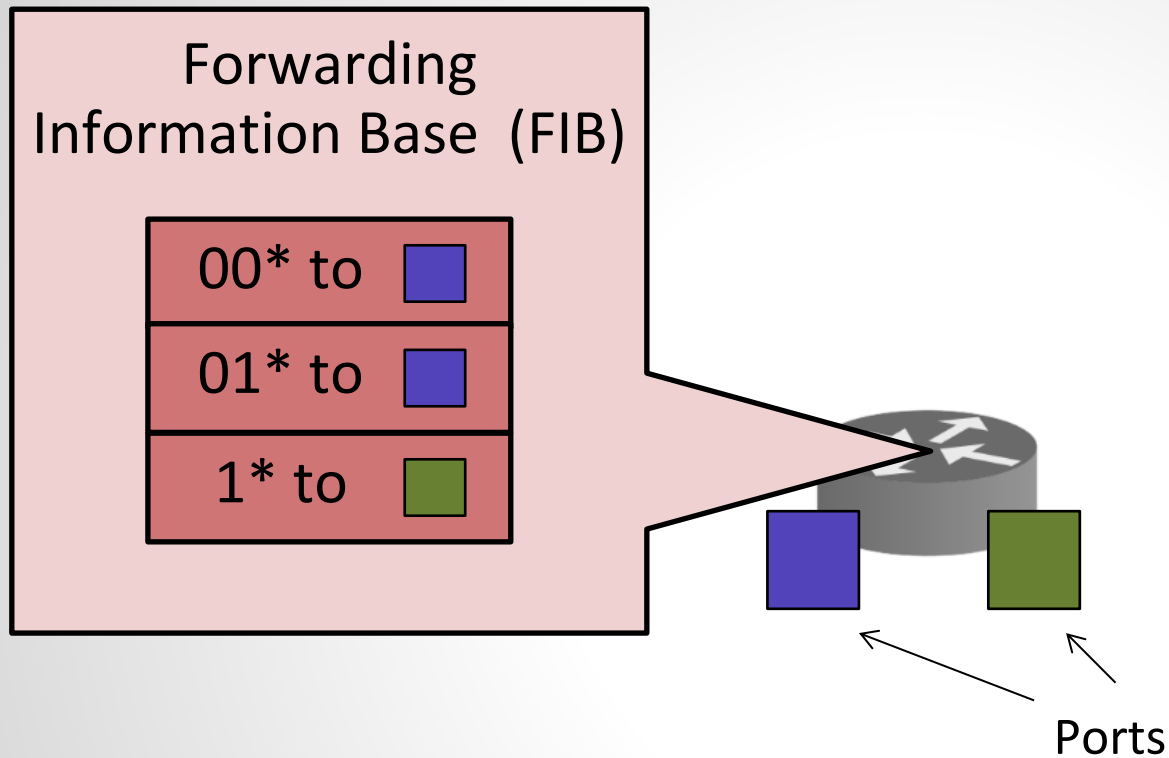
Poor Routers!

Key Functionality: Forwarding



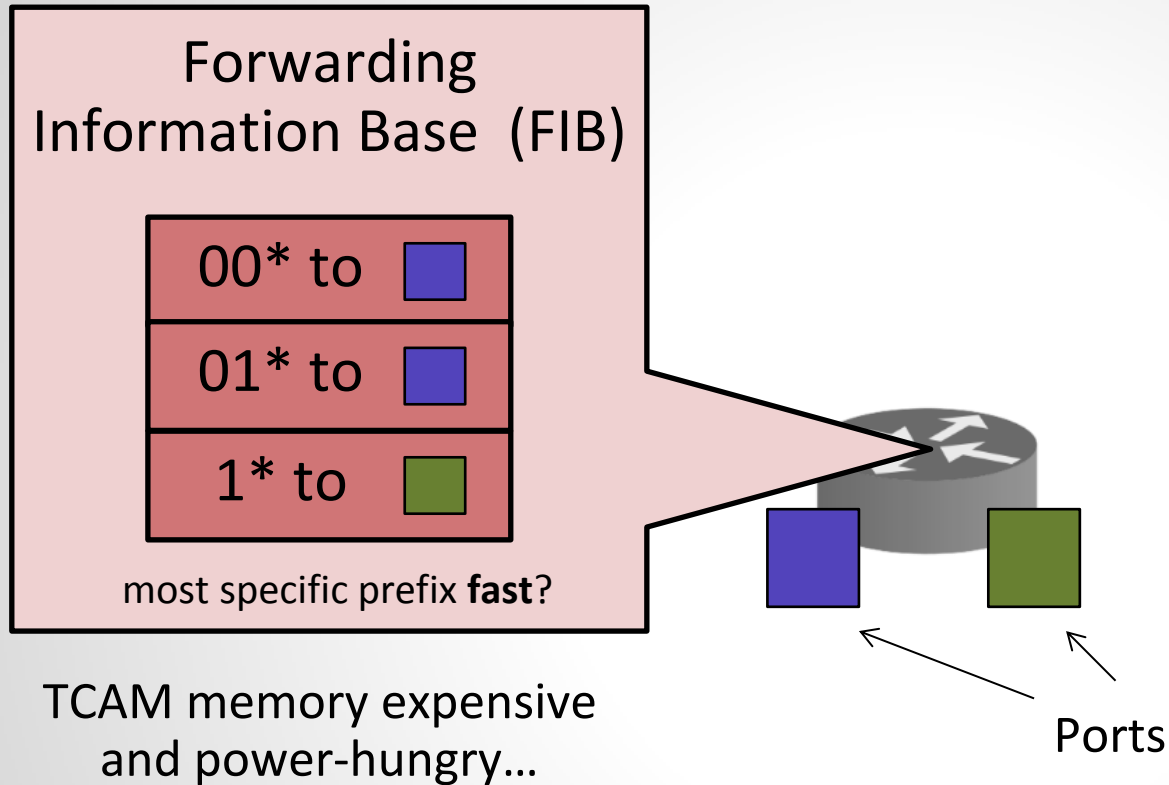
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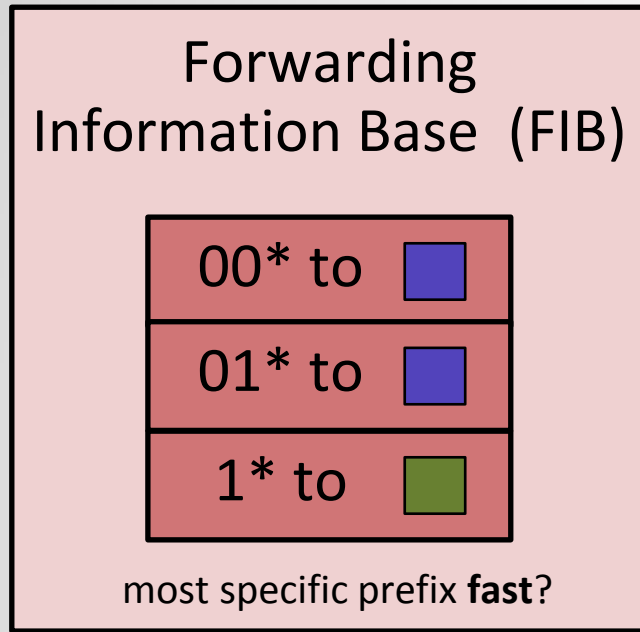
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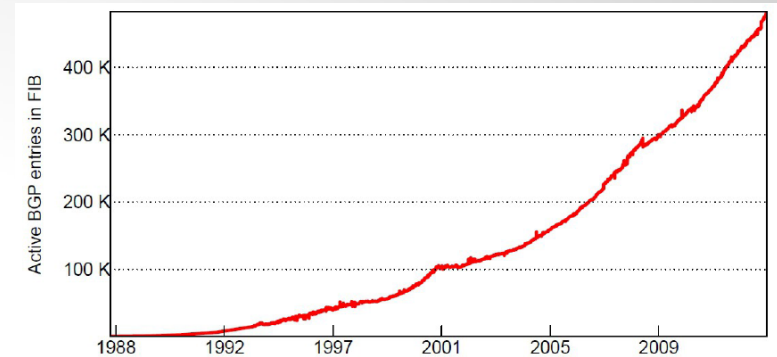


Poor Routers!

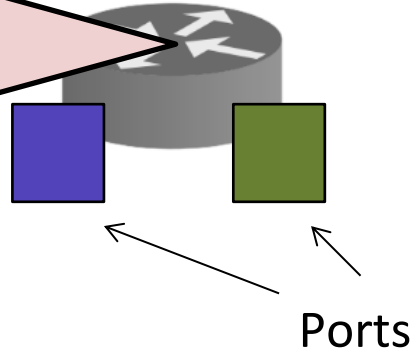
Key Functionality: Forwarding



TCAM memory expensive
and power-hungry...

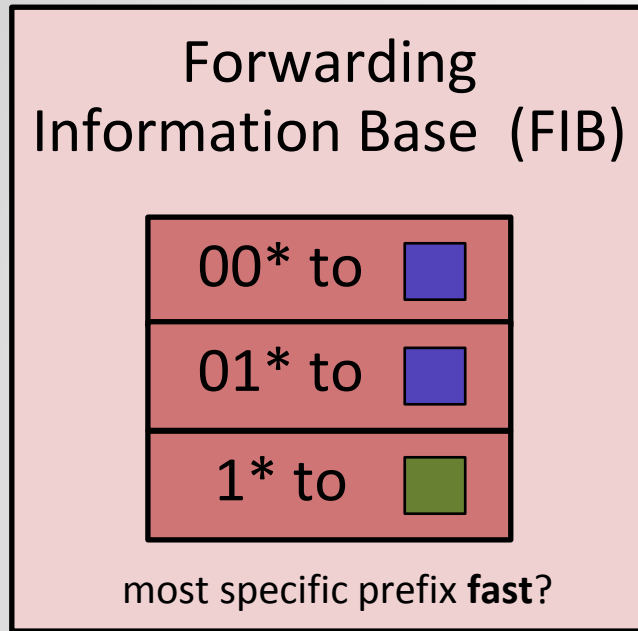


... and requirements grow
quickly (e.g., virtualization).
IPv6 does not help.

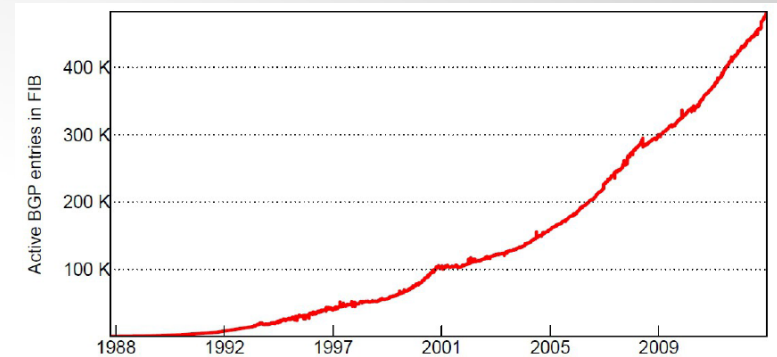
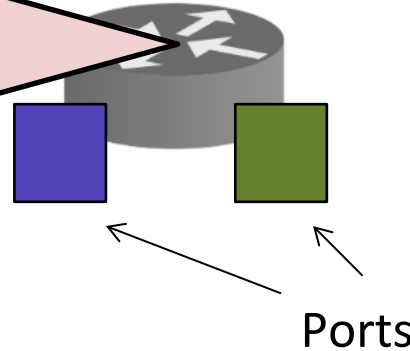


Poor Routers!

Key Functionality: Forwarding



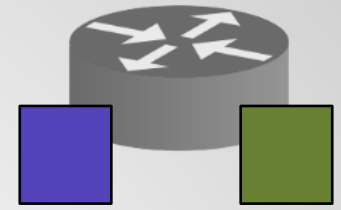
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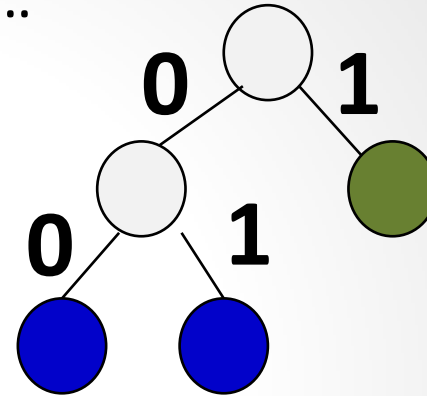
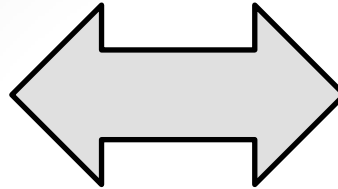
Idea to prolong the router lifetime:
Compress the FIB!

Idea: Compress the FIB

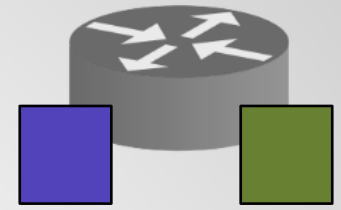


00* to	
01* to	
1* to	

represent as trie...

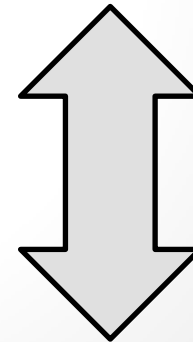
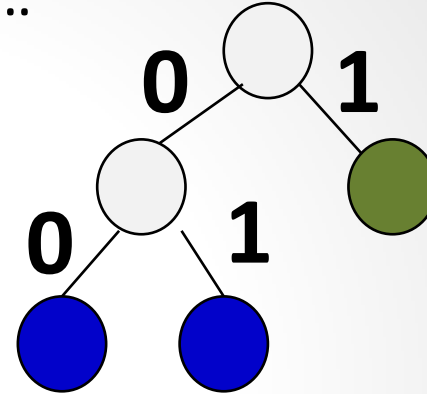
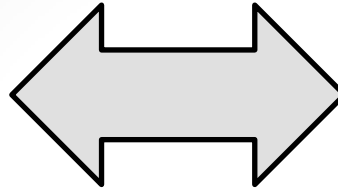


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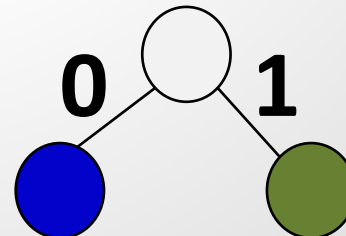


00* to	
01* to	
1* to	

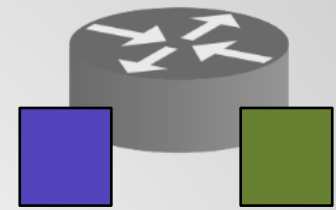
represent as trie...



... and compress it!

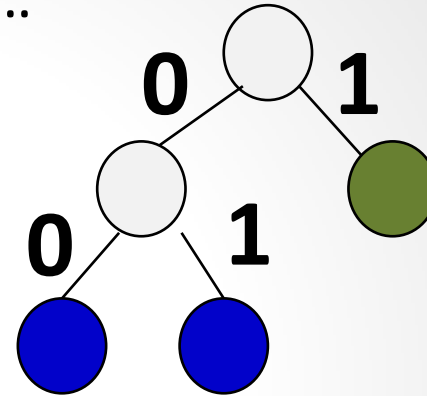
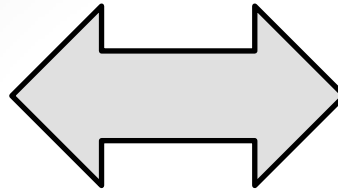


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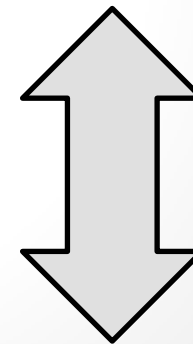
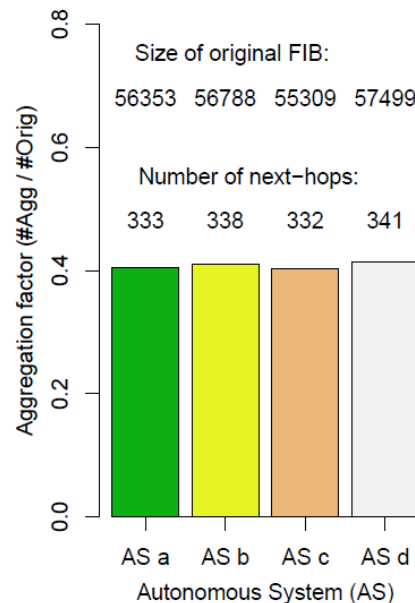
00* to	
01* to	
1* to	

represent as trie...

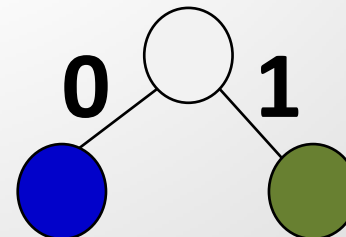


**Good
Potential:**

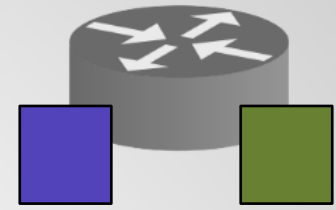
Down to 40%
(RouteView), depending
on # ports.



... and compress it!

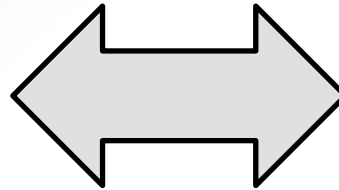


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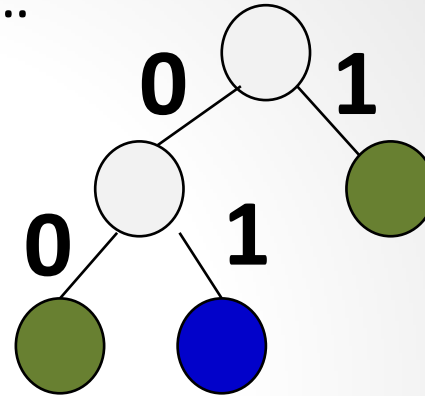


00* to	
01* to	
1* to	

represent as trie...

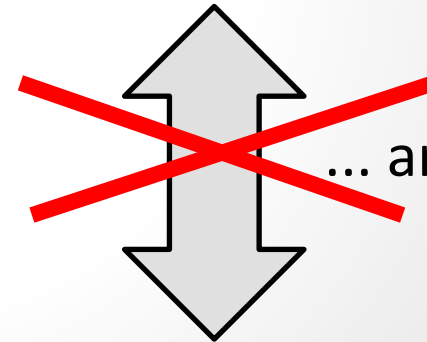


BGP event!

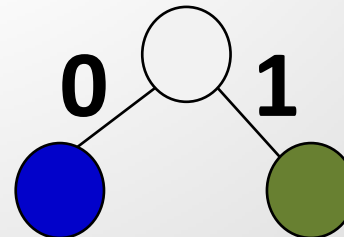


**But: May introduce
churn!**

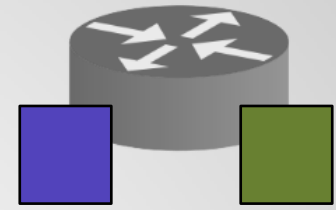
**Deaggregate upon
route change.**



... and compress it!

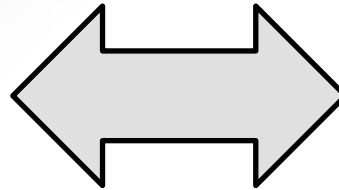


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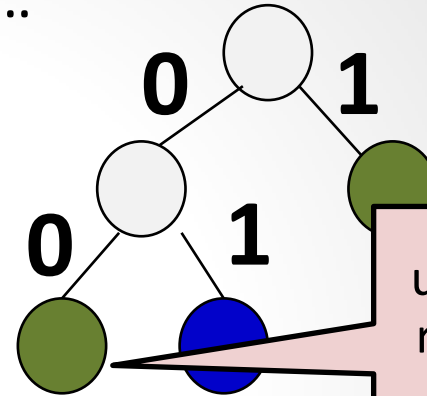


00* to	
01* to	
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represent as trie...



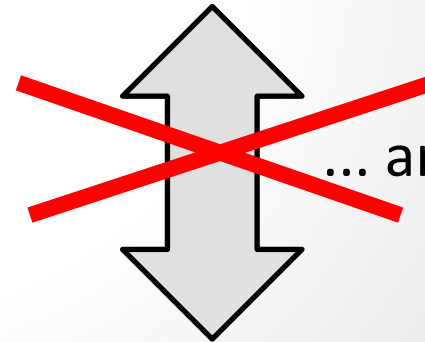
BGP event!



update cost 2:
remove + add

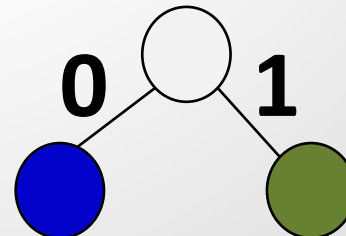
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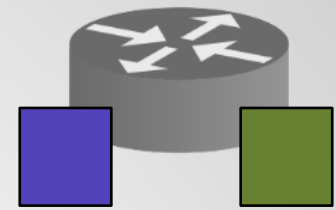


... and compress it!

update cost 3:
remove + add
subtree

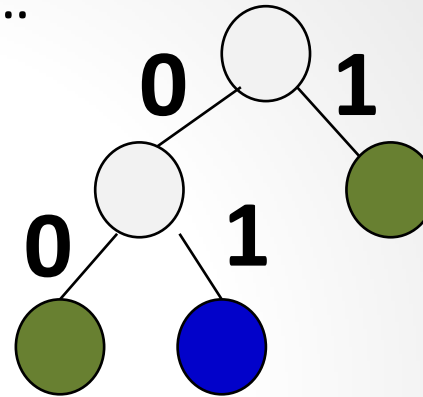
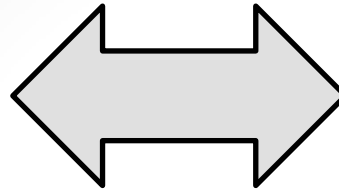


Idea: Compress the FIB



00* to	
01* to	
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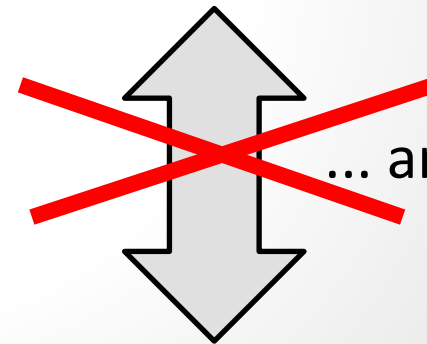
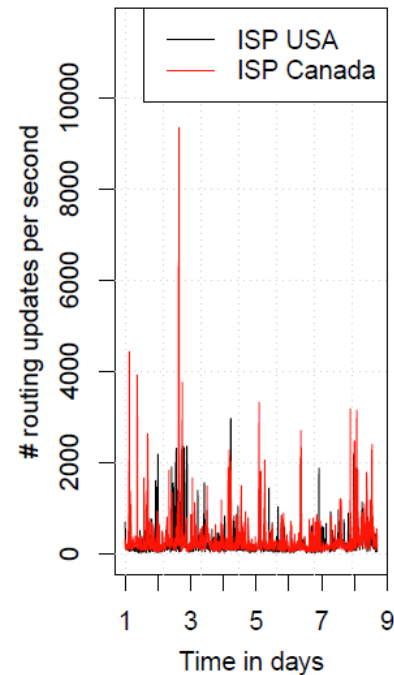
represent as trie...



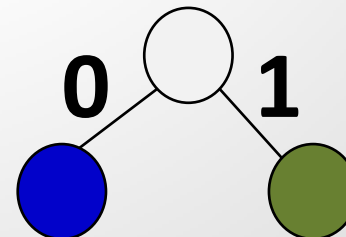
BGP event!

**But: May introduce
churn!
Deaggregate upon
route change.**

Already without
churn: 1000s/sec
updates in BGP!



... and compress it!



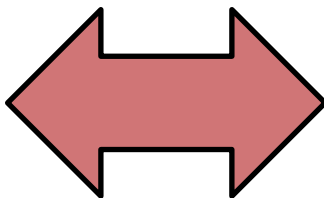
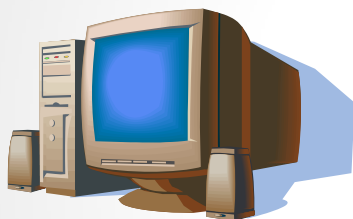
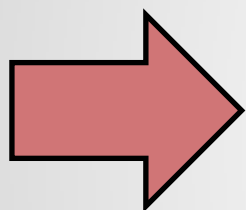
An Optimization Problem

Route Processor
or SDN Controller

FIB or SDN Switch

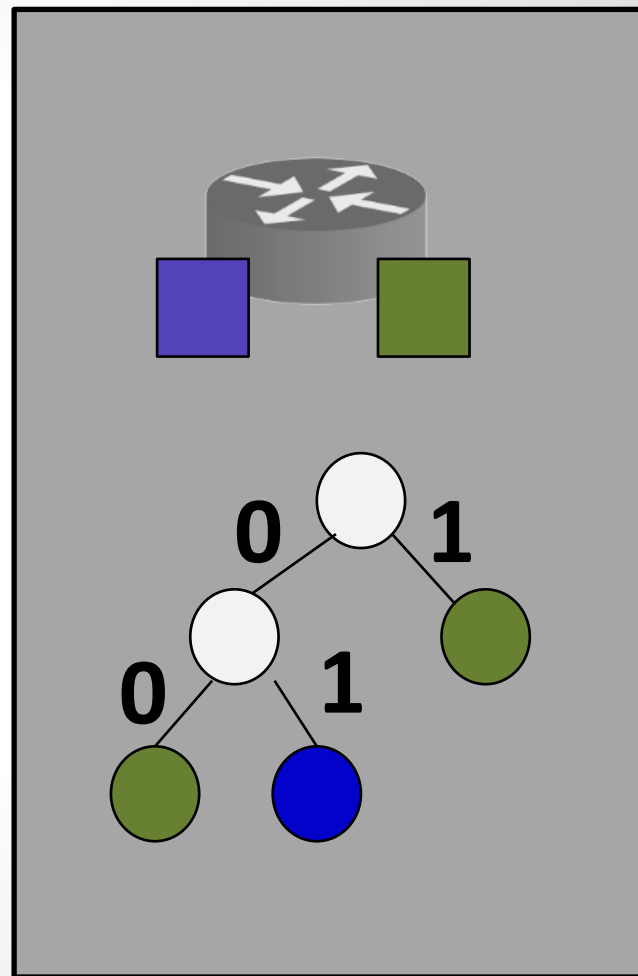
BGP
Events

update!



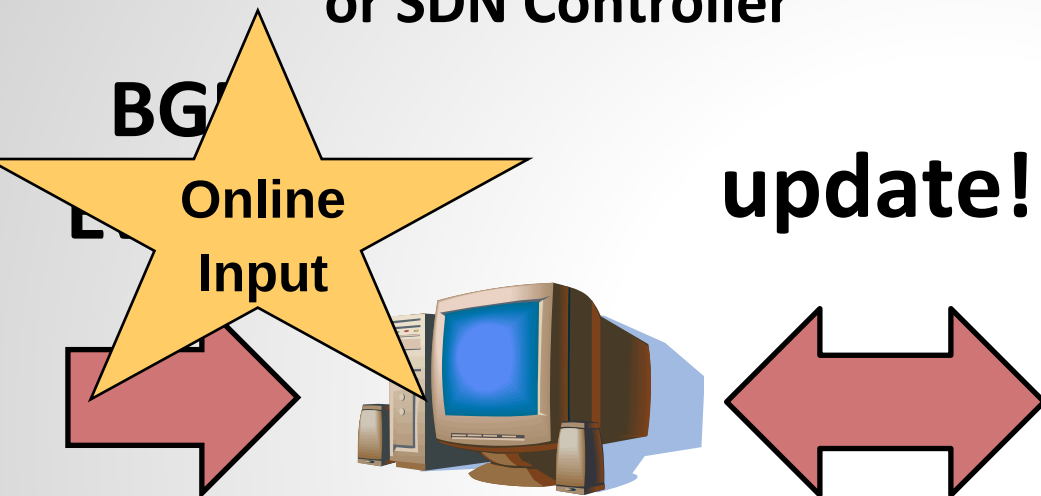
An online problem:

1. Forwarding must always be correct (equivalent)
2. Minimize update cost and memory size

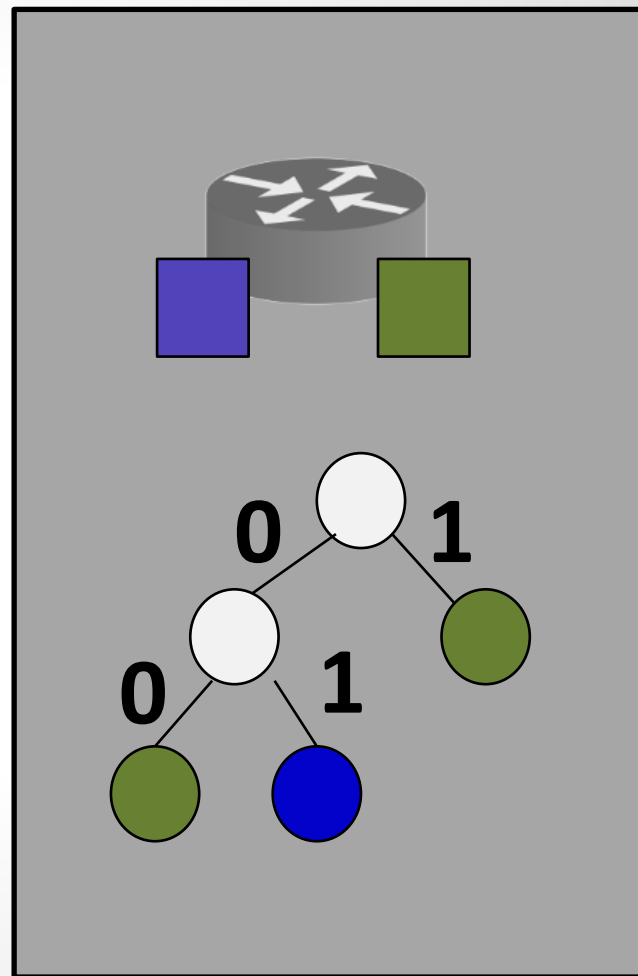


An Optimization Problem

Route Processor
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FIB or SDN Switch

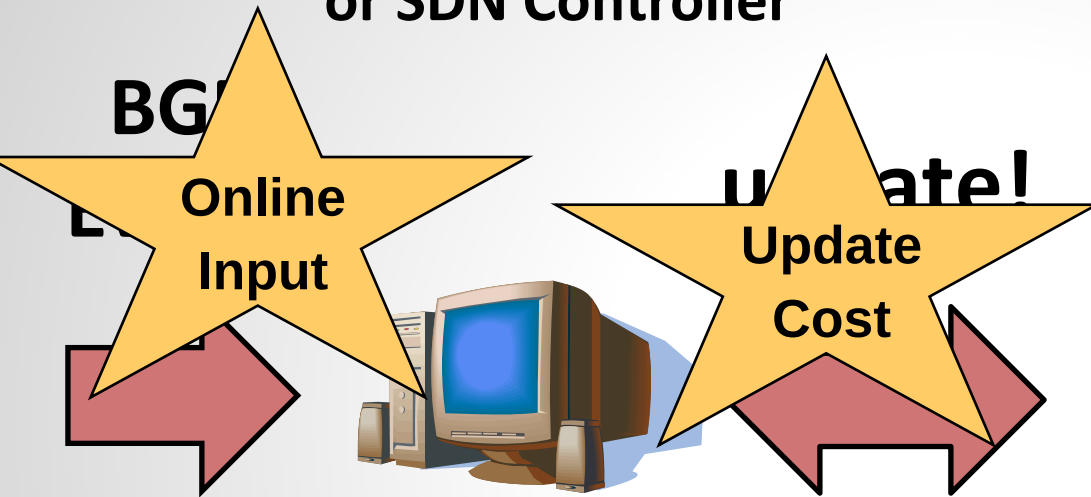


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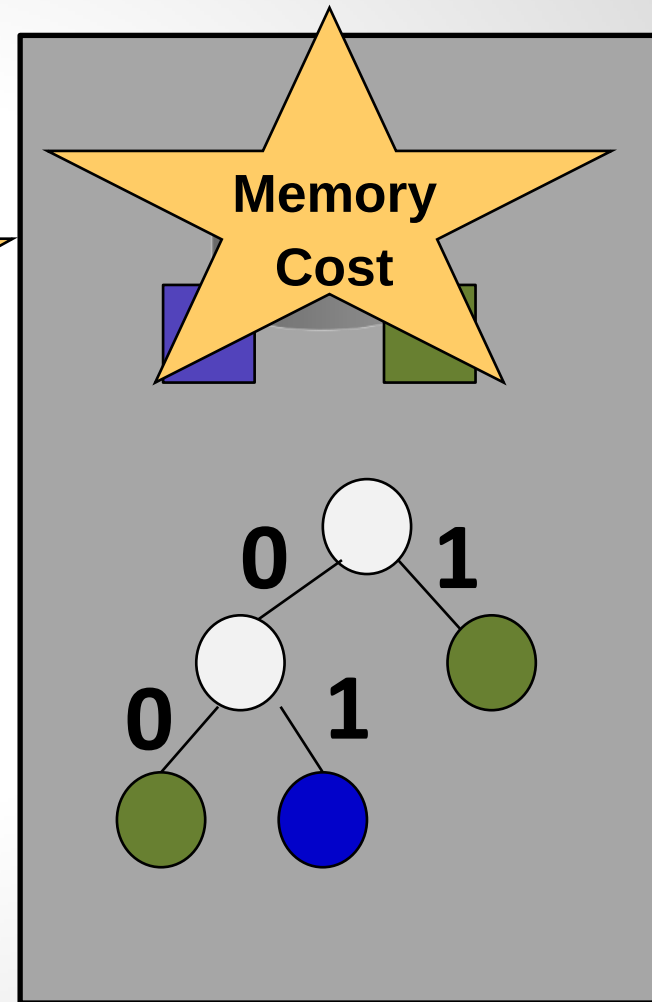
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An Optimization Problem

Route Processor
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FIB or SDN Switch



An online problem:

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An

Joint Optimization:

Route Pro
or SDN Co

$$\text{Cost} = \alpha (\# \text{ updates}) + \int_t \text{FIB size} \text{ tch}$$

BGP

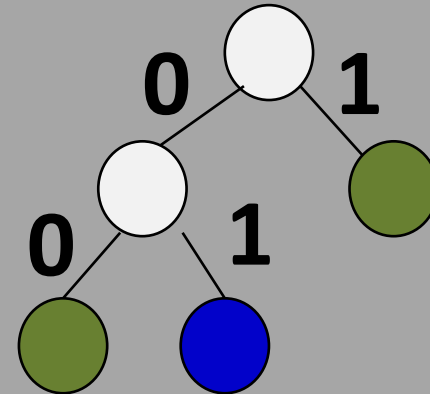
Online
Input

Update!
Update
Cost

Memory
Cost

An online problem:

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An

Joint Optimization:

Route Pro
or SDN Co

$$\text{Cost} = \alpha (\# \text{ updates}) + \int_t \text{FIB size} \text{ tch}$$

BGP

Online
Input

Update!
Update
Cost

Memory
Cost

Realm of Online Algorithms and Competitive Analysis!

$$\text{Competitive Ratio} = \max \text{Cost(ON)}/\text{Cost(OFF)}$$

- 1.
2. Minimize update cost and memory size

What Was Known So Far?

Static Compression

E.g., ORTC (INFOCOM'99): dynamic programming algorithm to compute optimally compressed FIB

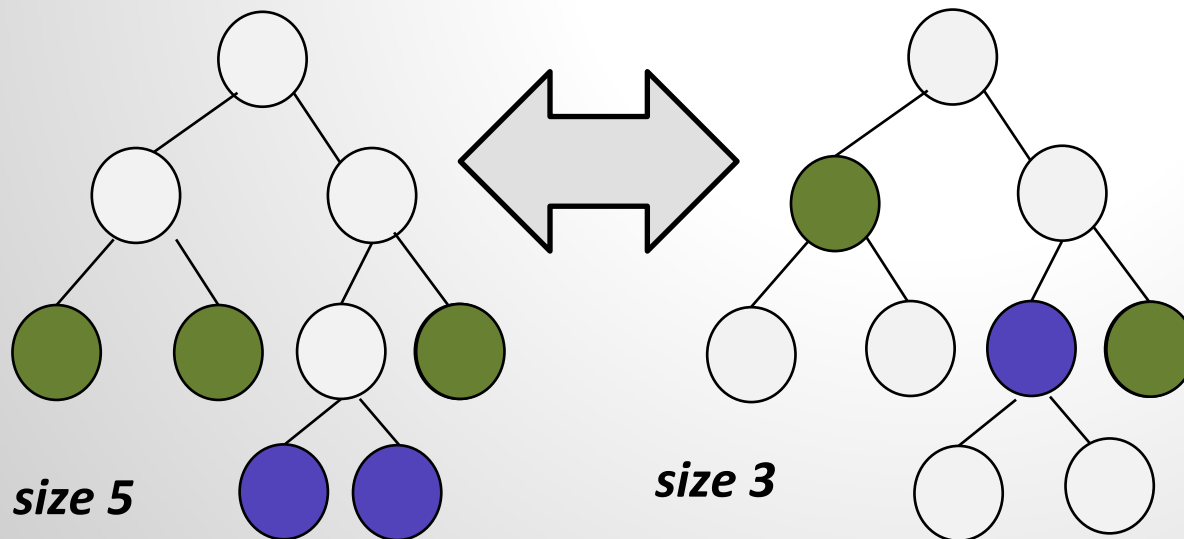
Dynamic Compression

No free lunch! (But can also *reduce* churn!)

Lots of work over the last 15 years (since Lulea) to find better tradeoffs between memory and updates. Often implicitly though. Heuristics: SMALTA (CoNEXT'11), FIFA (INFOCOM'13)

Online algorithm BLOCK for «independent prefixes»

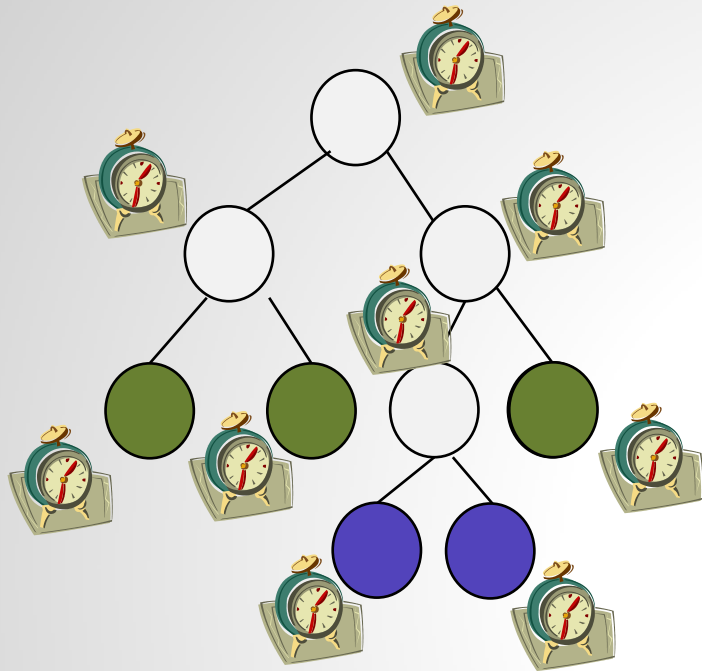
a.k.a. without exceptions (SIROCCO 2013)



BLOCK is 3.603-competitive.

Any online algorithm is at least 1.636-competitive. (Even if ON can use exceptions and OFF not.)

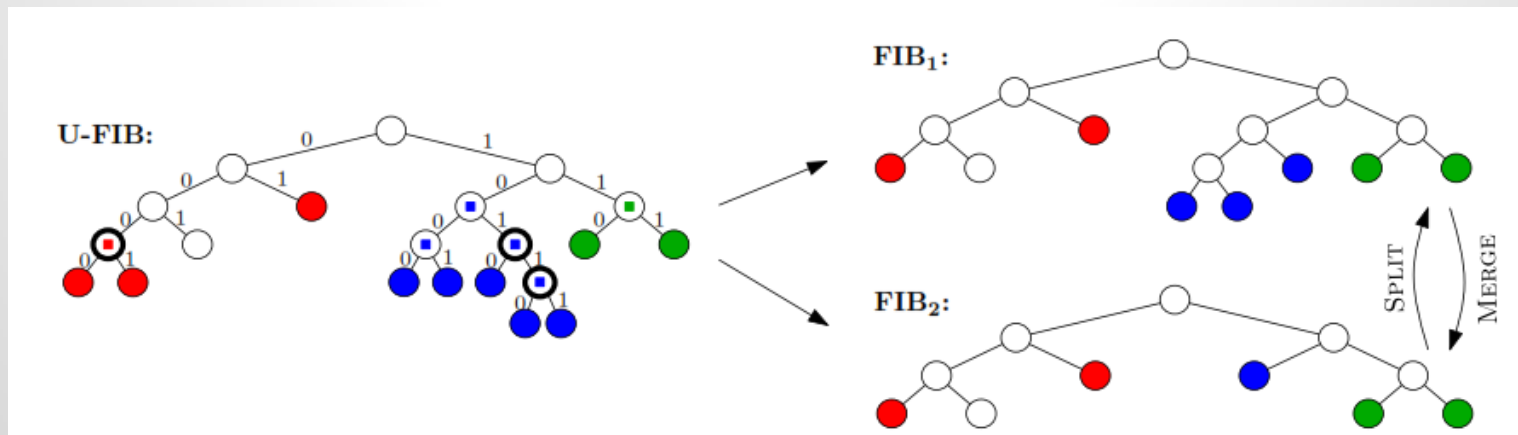
Idea of BLOCK



BLOCK(A,B) operates on trie:

1. balances memory and update costs
2. exploits possibility to merge multiple tree nodes simultaneously at lower price (thresholds A and B)

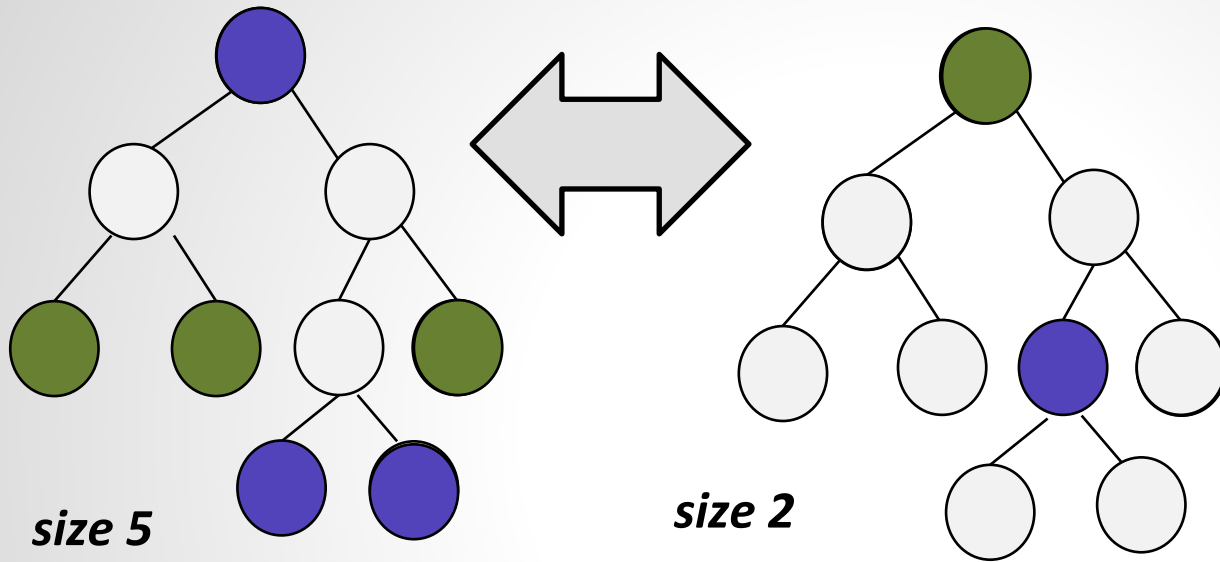
- Timers/counters for each trie node
- Wait before aggregating to save update costs
- Thresholds A and B for amortization ($A \geq B$) of update costs
- Definition: internal node v is **c-mergeable** if subtree $T(v)$ only contains color c leaves
- Trie node v monitors: how long was subtree $T(v)$ c-mergeable without interruption? Counter $C(v)$.
- If $C(v) \geq A$, then aggregate entire tree $T(u)$ where u is furthest ancestor of v with $C(u) \geq B$.
- Split lazily: only when forced.



Nodes with square inside: mergeable.

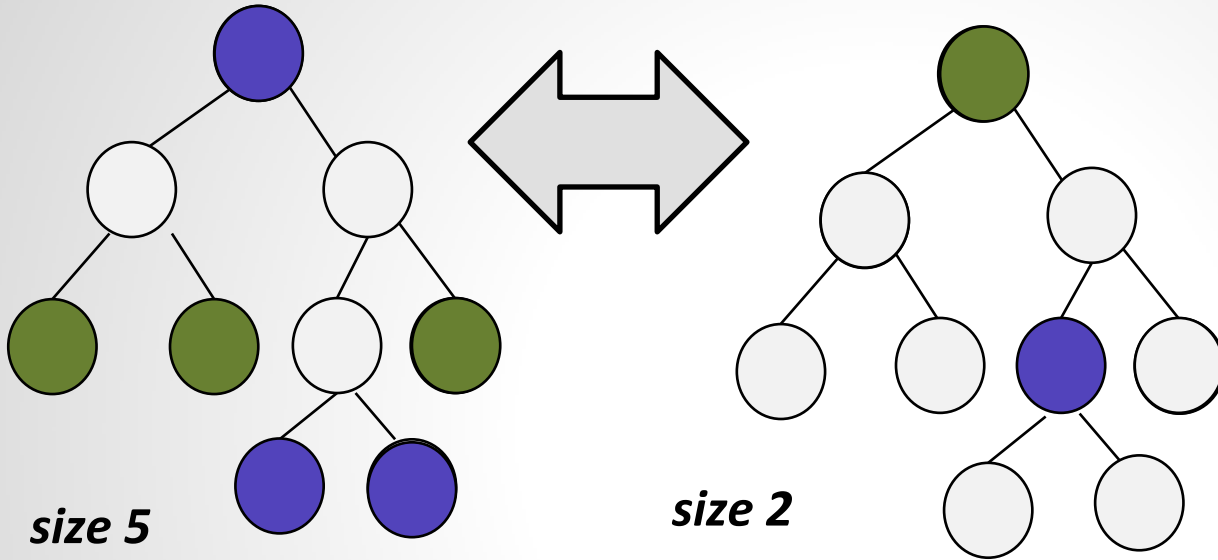
Our Contribution:

Competitive Compression for Dependent Prefixes



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Competitive Compression for Dependent Prefixes



**UFIB: Uncompressed trie
with exceptions**

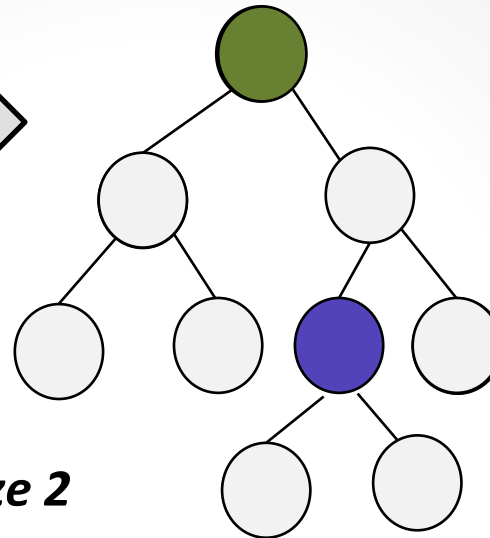
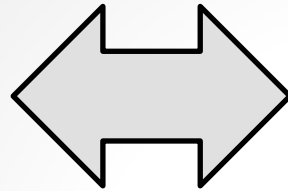
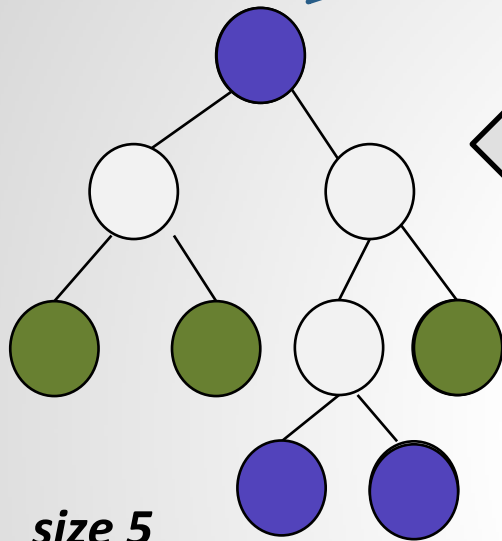
FIB: Compressed equivalent trie

Always stored in controller!

Comp

Invisible Node

Contribution: Compression for Dependent Prefixes



**UFIB: Uncompressed trie
with exceptions**

FIB: Compressed equivalent trie

Always stored in controller!

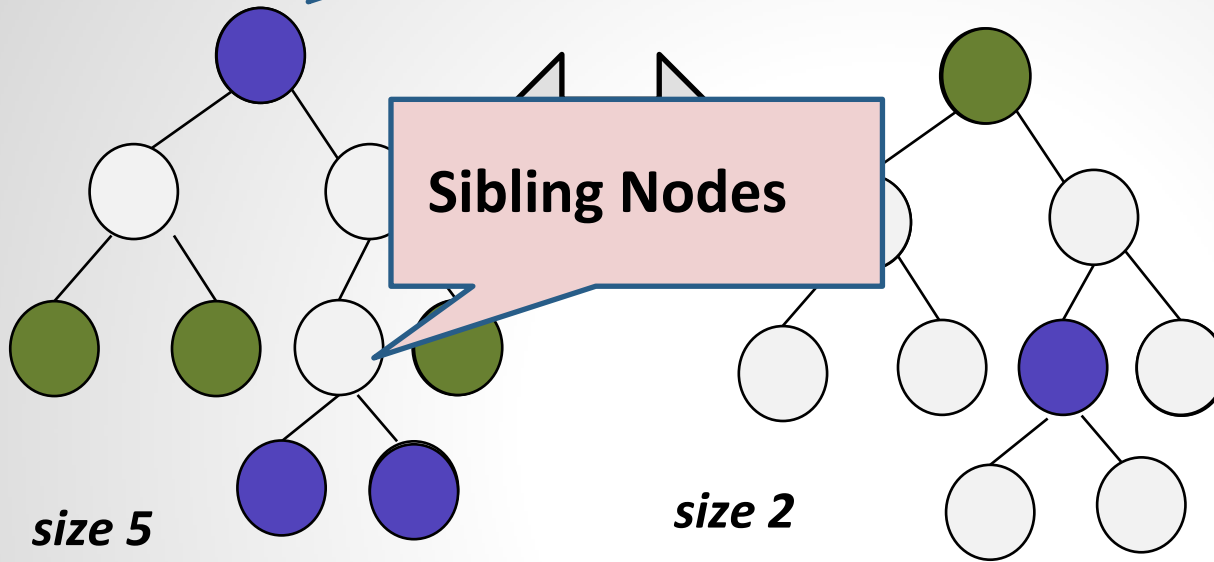
Contribution:

Comp

Invisible Node

sion for Dependent Prefixes

Sibling Nodes



UFIB: Uncompressed trie
with exceptions

FIB: Compressed equivalent trie

Always stored in controller!

Comp

Invisible Node

Contribution:
sion for Dependent Prefixes

Sibling Nodes

Theorem 1: HIMS

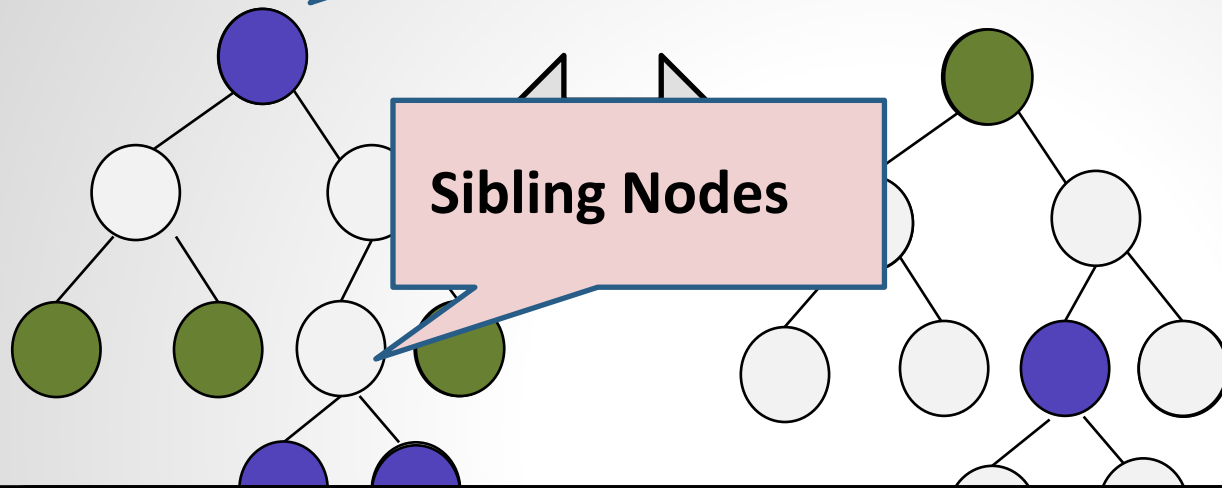
HIMS («Hide Invisible Merge Siblings») is $O(w)$ -competitive, where w is prefix length. HIMS is deterministic.

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Comp

Invisible Node

sion for Dependent Prefixes



Theorem 1: HIMS

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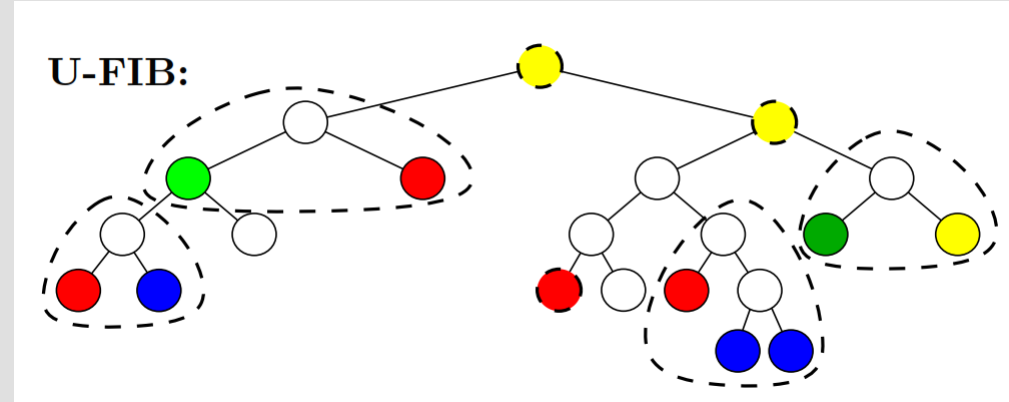
Theorem 2: Lower Bound

This is optimal for a large class of online and offline algorithms.

Ideas of HIMS.

Concept of Sticks: (on UFIB!)

Maximal subtrees of UFIB with colored leaves and blank internal nodes.

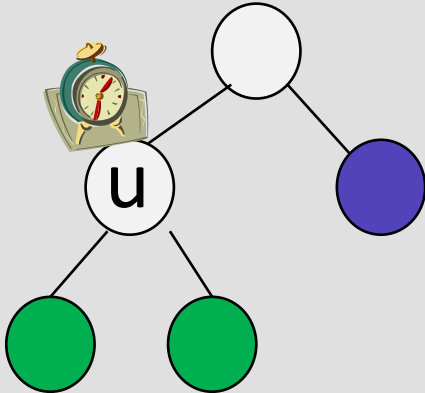


Idea: if all leaves in stick have same color, they would become mergeable.

Ideas of HIMS.

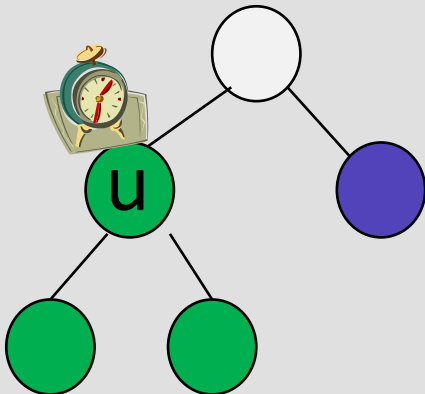
Two counters at nodes:

Merge Sibling Counter $C(u)$



$C(u)$ = time since stick descendants are unicolor

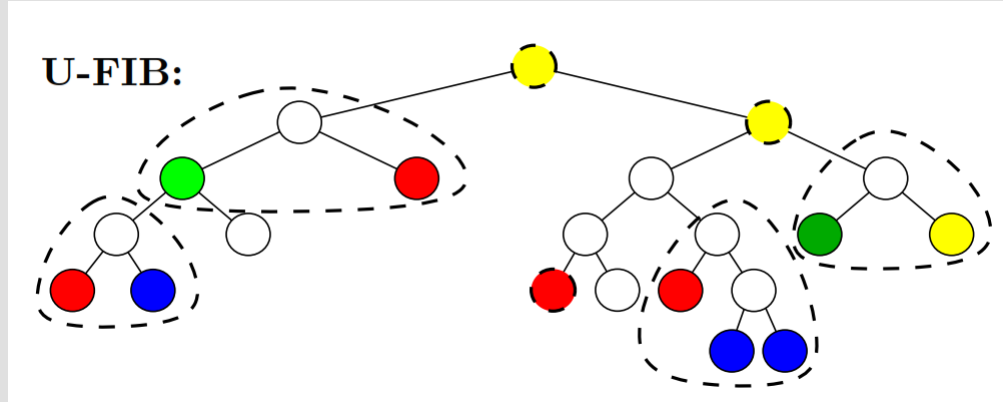
Hide Invisible Counter $H(u)$



$H(u)$ = how long do nodes have same color as the least colored ancestor in UFIB?

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Maximal subtrees of UFIB with colored leaves and blank internal nodes.

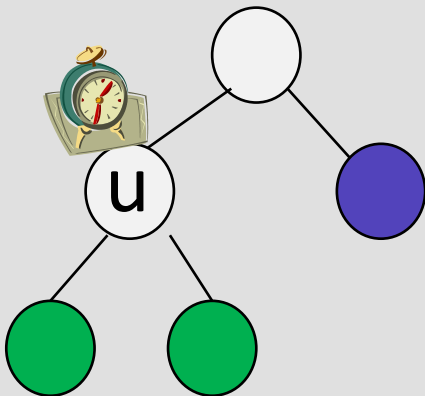


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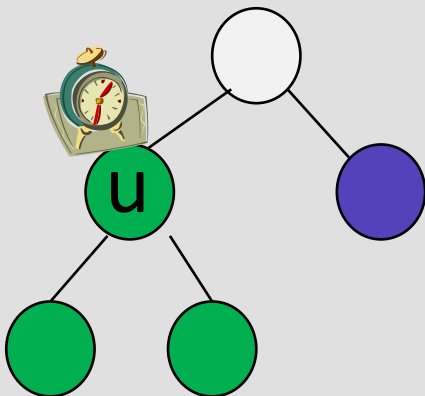
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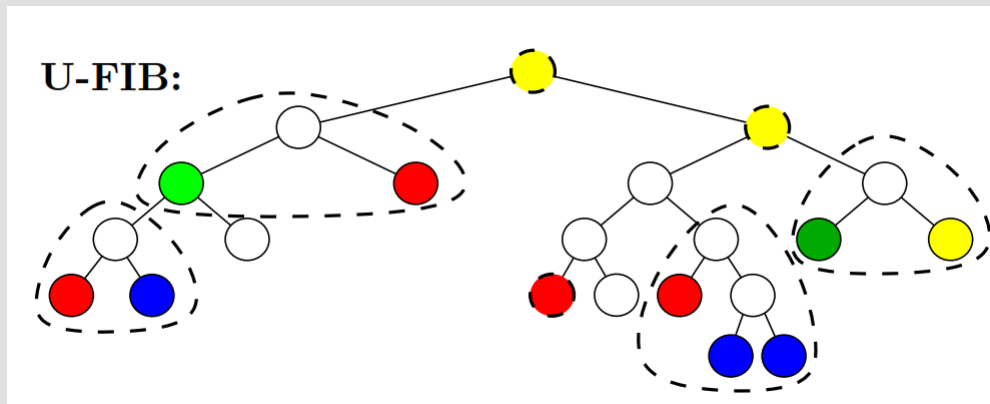
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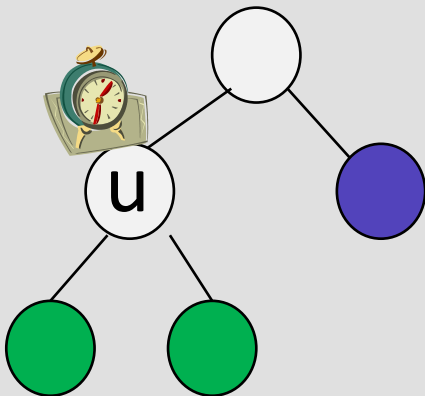
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Monotonic properties: E.g., color change of stick leaf resets all counters to root. So $C(u) \geq C(p(u))$ and $H(u) \geq H(p(u))$, and also $C(u) \geq H(u)$, as I need ancestor. Where $p()$ is parent in trie.

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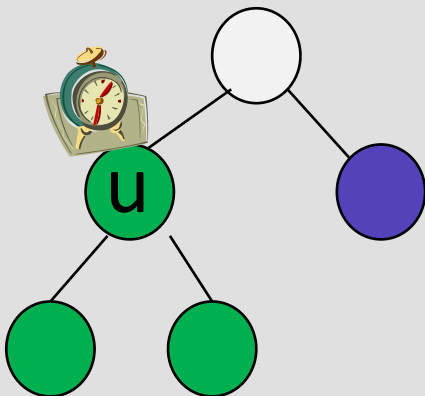
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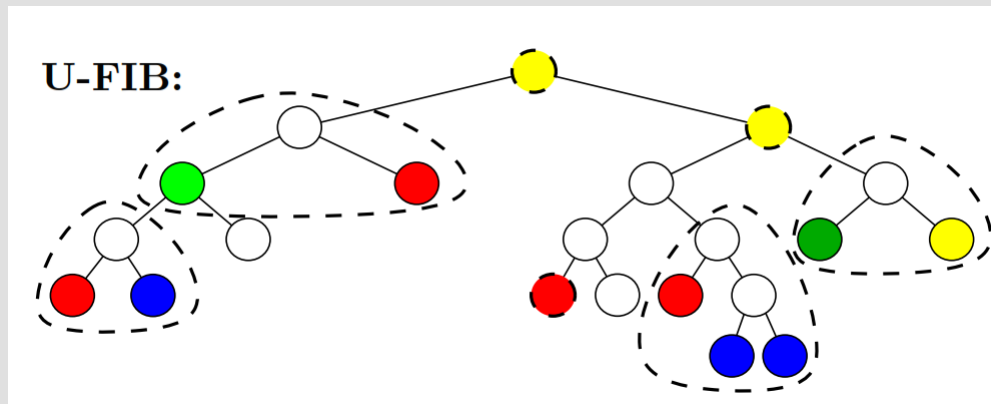
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Idea: if all leaves in stick have same color, they would become mergeable.

Monotonic properties: E.g., color change of stick leaf resets all counters to root. So $C(u) \geq C(p(u))$ and $H(u) \geq H(p(u))$, and also $C(u) \geq H(u)$, as I need ancestor. Where $p()$ is parent in trie.

HIMS Algo: Keep rule in FIB if and only if **all three** conditions hold:

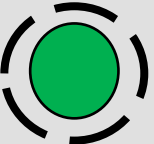
- (1) $H(u) < \alpha$ (remove if hidden for long)
- (2) $C(u) \geq \alpha$ or u is a stick leaf (always true for UFIB rule)
- (3) $C(p(u)) < \alpha$ or u is a stick root (remove if amortized parent)

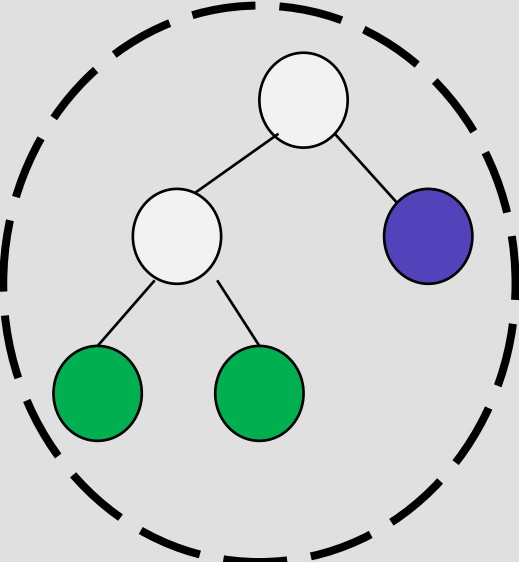
Ideas of HIMS.

Concept of Sticks: (on UFIB!)

Maximal subtrees of UFIB with colored leaves and

Example.

Ex 1.  Trivial stick: node is both root and leaf (Conditions 2+3 fulfilled). So HIMS simply waits until invisible node can be hidden.

Ex 2.  Stick without colored ancestors: $H(u)=0$ all the time (Condition 1 fulfilled). So everything depends on sibling counters inside stick. E.g., if no change for time α and unicolor leaves, only root stays (all three conditions fulfilled).

Ex 3. Inner nodes of the stick are never longer than α in the FIB. (Otherwise second condition violated.)

$H(u)$ = how long do nodes have same color as the least colored ancestor in UFIB?

- (1) $H(u) < \alpha$ (remove if hidden for long)
- (2) $C(u) \geq \alpha$ or u is a stick leaf (always true for UFIB rule)
- (3) $C(p(u)) < \alpha$ or u is a stick root (remove if amortized parent)

Upper Bound: Proof Idea

Theorem:

HIMS is $O(w)$ -competitive.

Proof idea:

- In the absence of further BGP updates
 - (1) HIMS does not introduce any changes **after time α**
 - (2) After time α , the memory cost is at most an factor **$O(w)$ off**
- In general: for any snapshot at time t , either HIMS already started aggregating or changes are quite new
- Lower bound for OFF: Concept of rainbow points and line coloring useful.



- A rainbow point is a “witness” for a FIB rule.
- Many different rainbow points over time give lower bound.

Lower Bound: Proof Idea

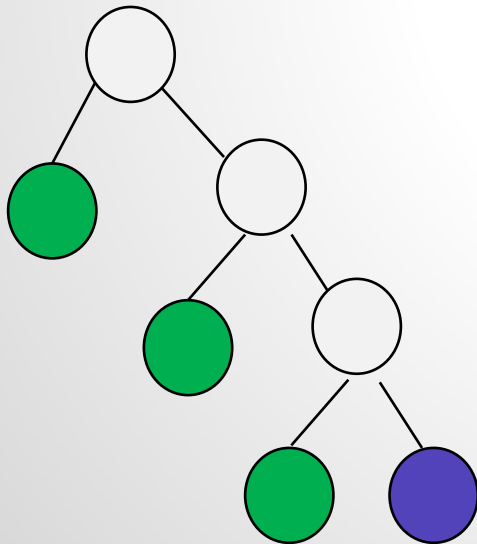
Theorem:

Any (online or offline) Stick-based algo is $\Omega(w)$ -competitive.

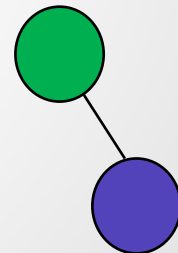
Proof idea:

- Stick-based:
- (1) never keep a node outside a stick
 - (2) inside a stick, for any pair u, v in ancestor-descendant relation, only keep one

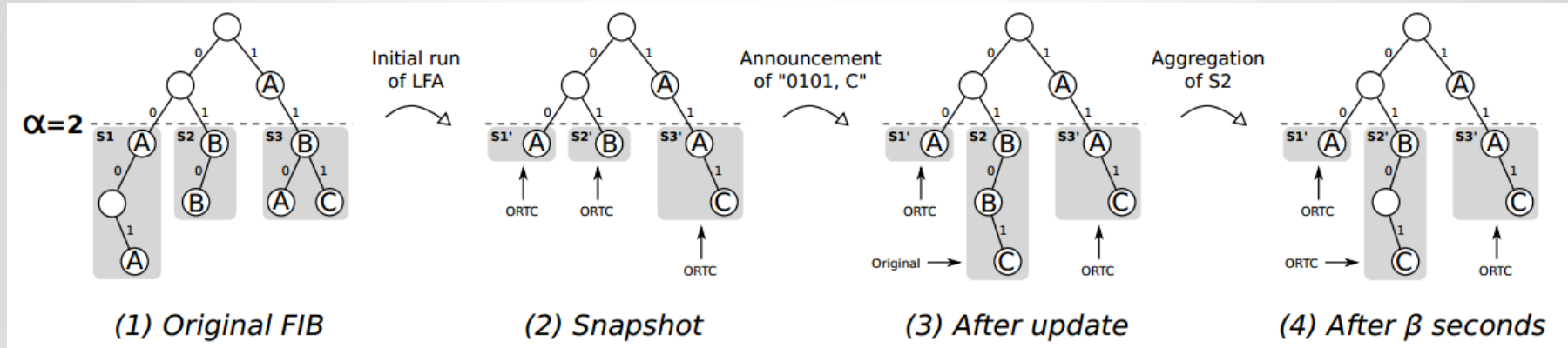
Consider single stick: prefixes representing lengths $2^{w-1}, 2^{w-2}, \dots, 2^1, 2^0, 2^0$



Cannot aggregate stick!
But OPT could do that:



QED



Conclusion

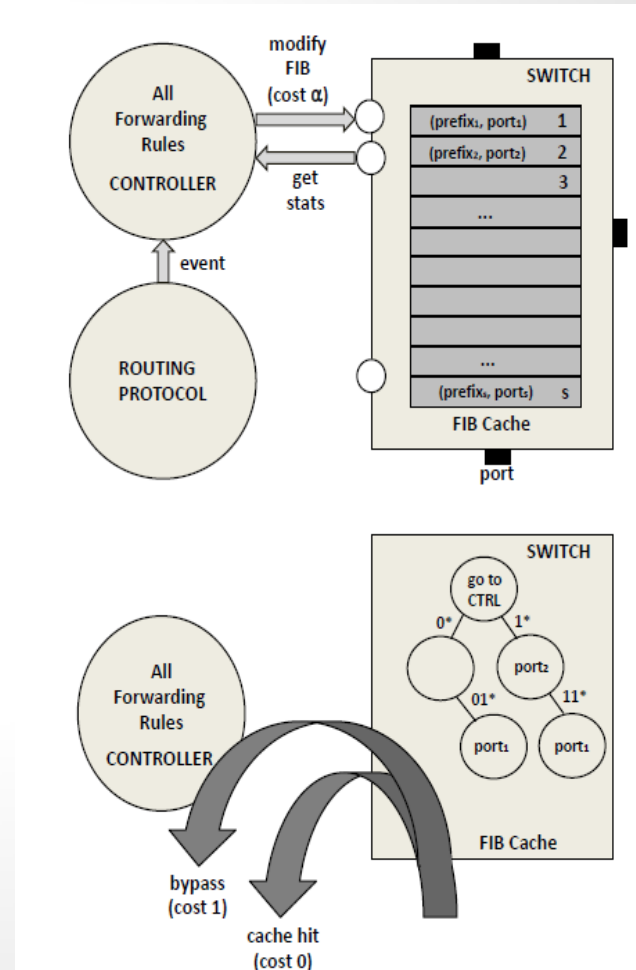
- Without exceptions in input and output: BLOCK is constant competitive
- With exceptions in input and output: HIMS is $O(w)$ -competitive
- Note on offline variant: fixed parameter tractable, runtime of dynamic program in $f(\alpha) n^{O(1)}$

Thank you! Questions?

Why Aggregation in Worst Case?

With fixed switch size and sum over time?

- Start to make errors late!
- Or offload rest...



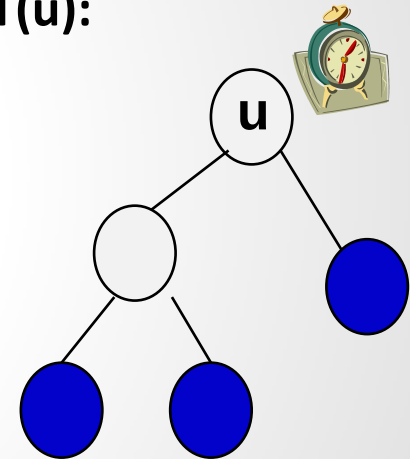
Analysis

Theorem: BLOCK(A,B) is 3.603-competitive.

Proof idea (a bit technical):

- Time events when ALG merges k nodes of $T(u)$ at u
- **Upper bound ON cost:**
 - $k+1$ counters between $B\alpha$ and $A\alpha$
 - Merging cost at most $(k+3)\alpha$: remove $k+2$ leaves, insert one root
 - Splitting cost at most $(k+1)3\alpha$: in worst case, remove-insert-remove individually
- **Lower bound OFF cost:**
 - Time period from $t-\alpha$ to t
 - If OPT does not merge anything in $T(u)$ or higher: high memory costs
 - If OPT merges ancestor of u : counter there must be smaller than $B\alpha$, memory and update costs
 - If OPT merges subtree of $T(u)$: update cost and memory cost for in- and out-subtree
- Optimal choice: $A = \sqrt{13} - 1$, $B = (2\sqrt{13})/3 - 2/3$
- Add event costs (inserts/deletes) later!

$T(u)$:



QED

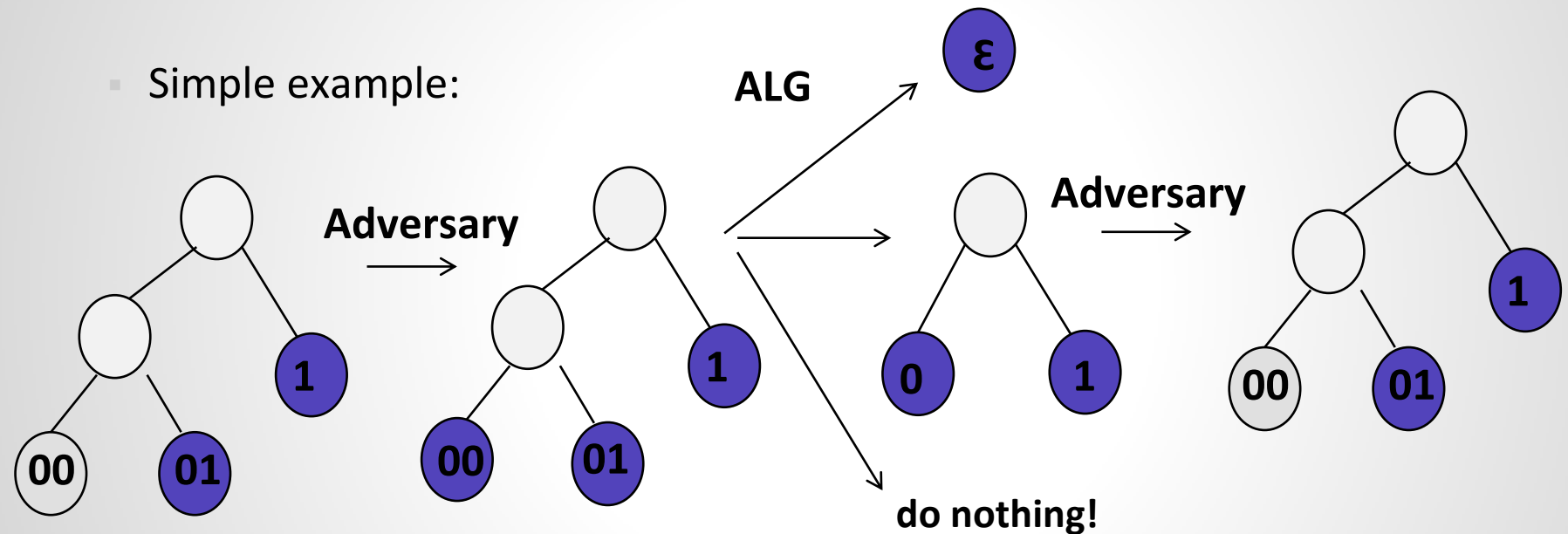
Lower Bound

Theorem:

Any online algorithm is at least 1.636-competitive.

Proof idea:

- Simple example:

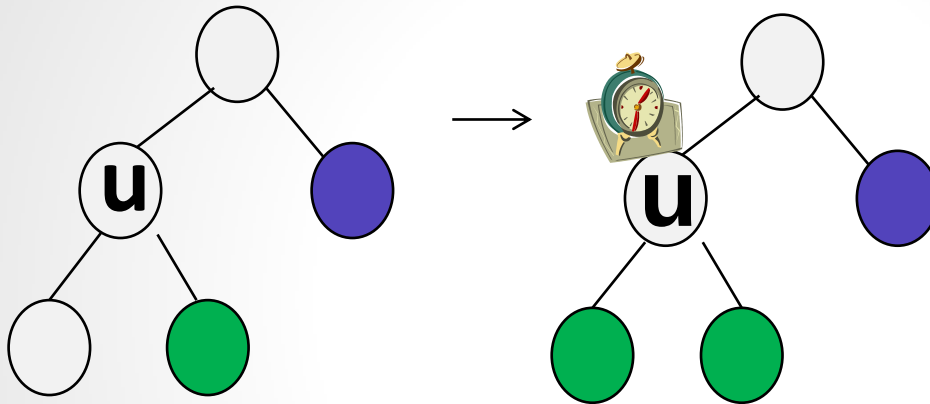


- (1) If ALG does **never** changes to single entry, competitive ratio is at least 2 (size 2 vs 1).
- (2) If ALG changes **before time α** , adversary immediately forces split back! Yields costly inserts...
- (3) If ALG changes **after time α** , the adversary resets color as soon as ALG for the first time has a single node. Waiting costs too high.

Note on Adding Insertions and Deletions

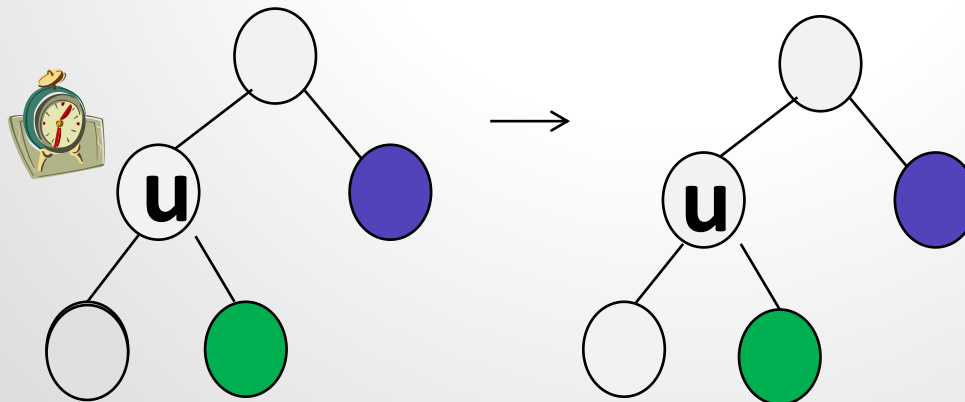
- Algorithm can be extended to insertions/deletions

Insert:



u becomes mergeable!

Delete:



u no longer mergeable!