

# Self-Adjusting Networks

Stefan Schmid @ IIT Bhubaneswar

“We cannot direct the wind,  
but we can adjust the sails.”

(Folklore)

Acknowledgements:

# Trend

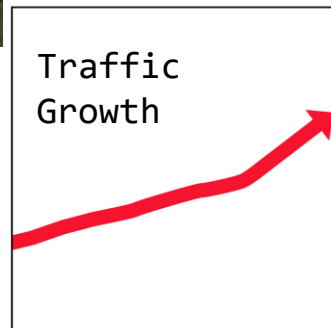
## Data-Centric Applications



Datacenters (“hyper-scale”)



Interconnecting networks:  
a **critical infrastructure**  
of our digital society.

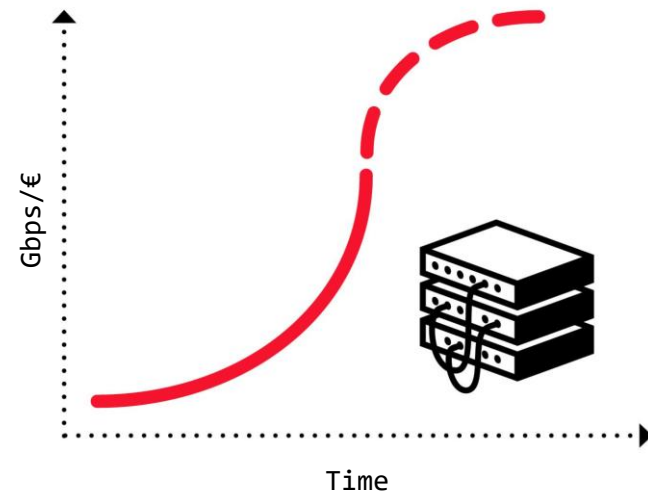


Source: Facebook

# The Problem

## Huge Infrastructure, Inefficient Use

- Network equipment reaching capacity limits
  - Transistor density rates stalling
  - “End of **Moore’s Law** in networking” [1]
- Hence: more equipment, larger networks
- Resource intensive and: **inefficient**



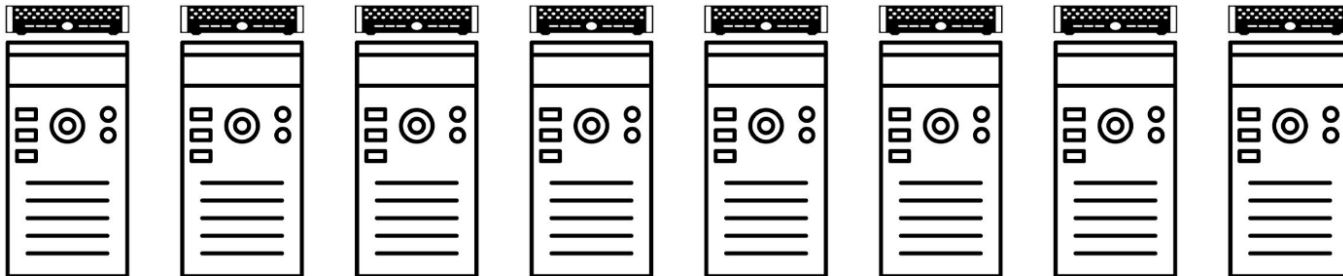
[1] Source: Microsoft, 2019

Annoying for companies,  
**opportunity** for researchers

# Root Cause

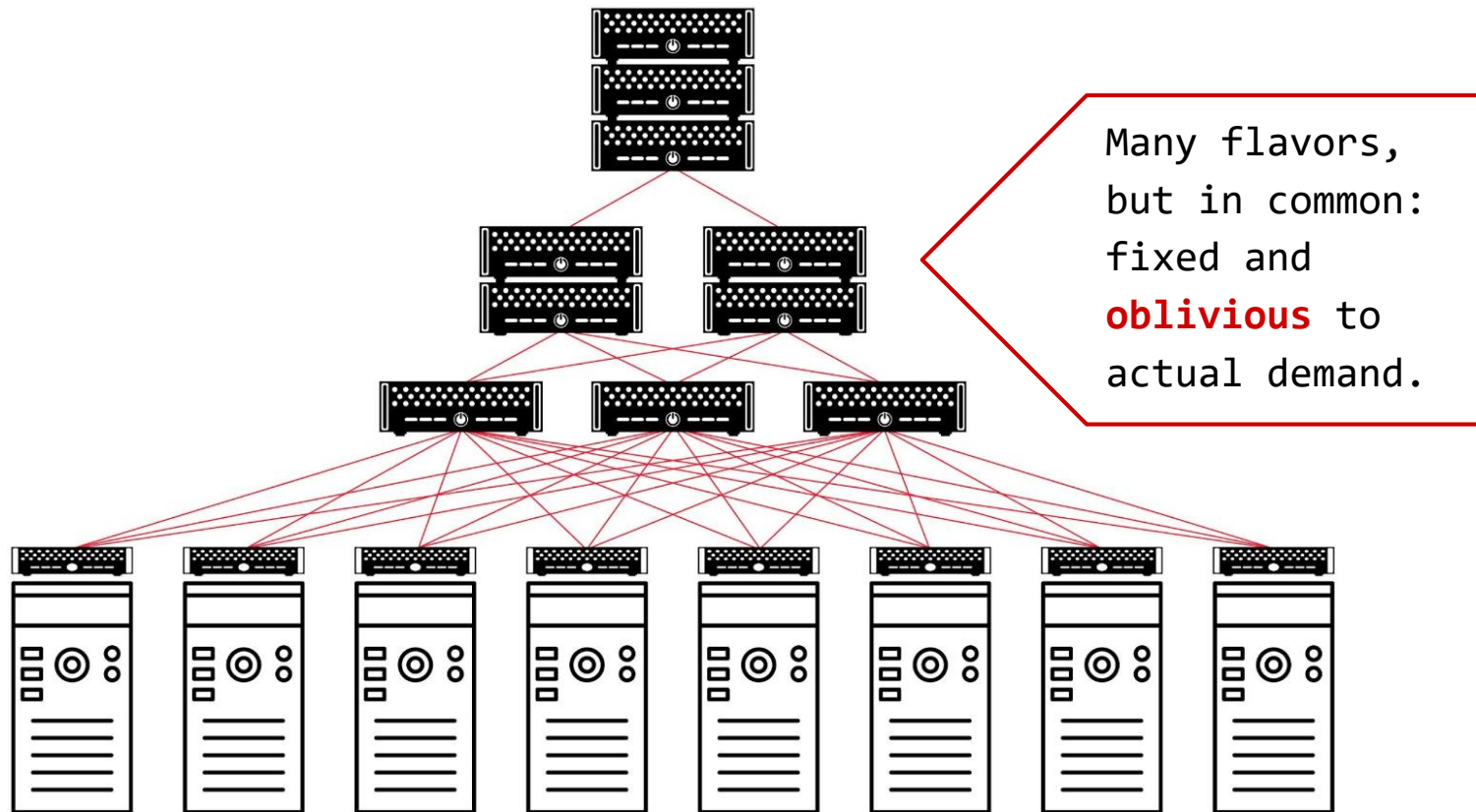
Fixed and Demand-Oblivious Topology

How to interconnect?



# Root Cause

## Fixed and Demand-Oblivious Topology

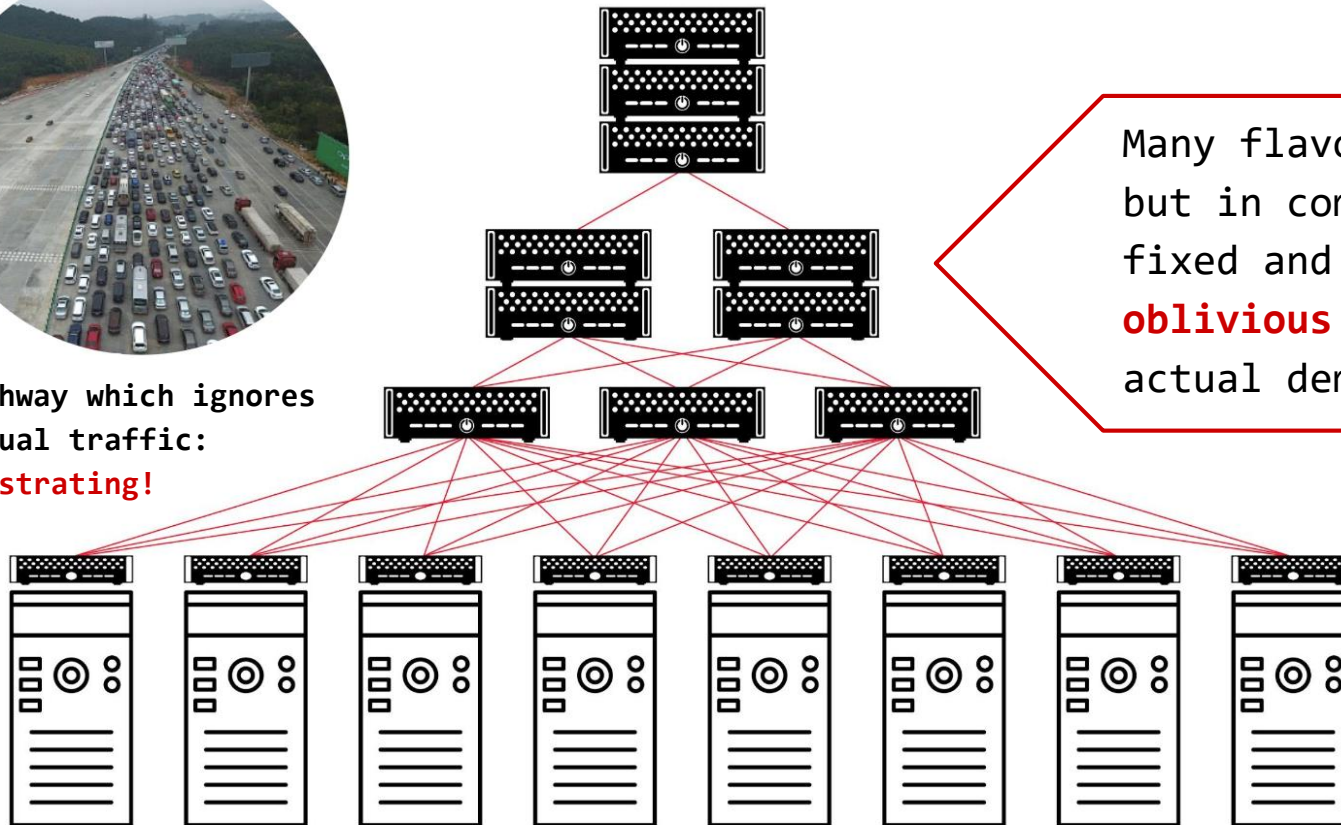


# Root Cause

## Fixed and Demand-Oblivious Topology



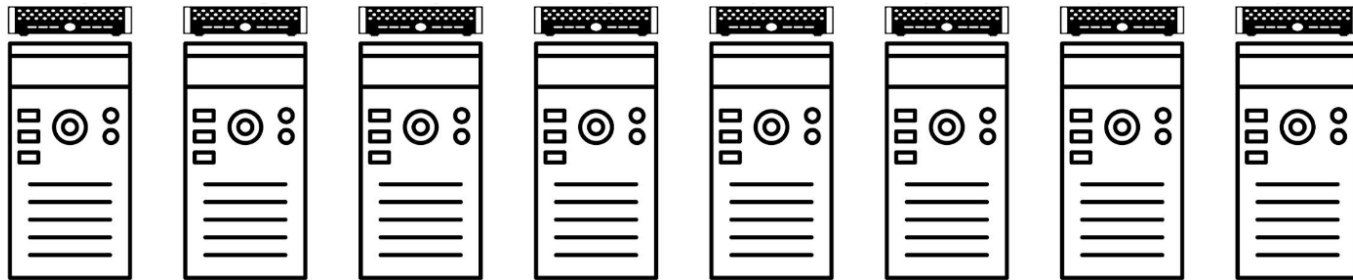
Highway which ignores  
actual traffic:  
**frustrating!**



Many flavors,  
but in common:  
fixed and  
**oblivious** to  
actual demand.

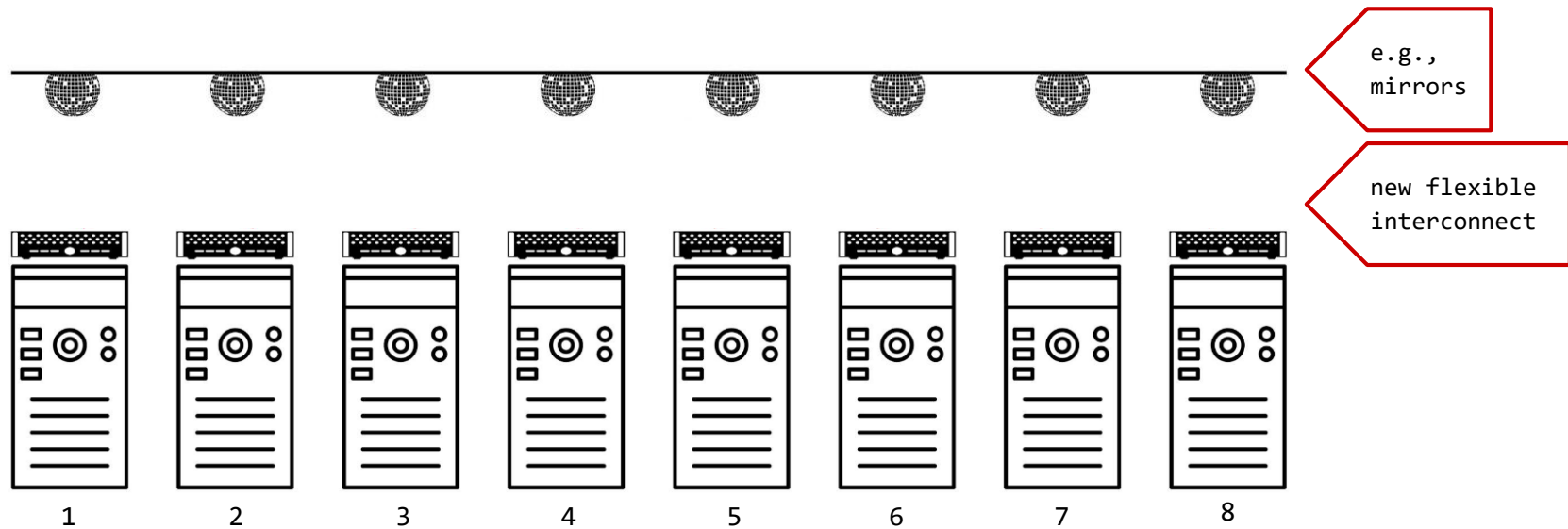
# Our Vision

Flexible and Demand-Aware Topologies



# Our Vision

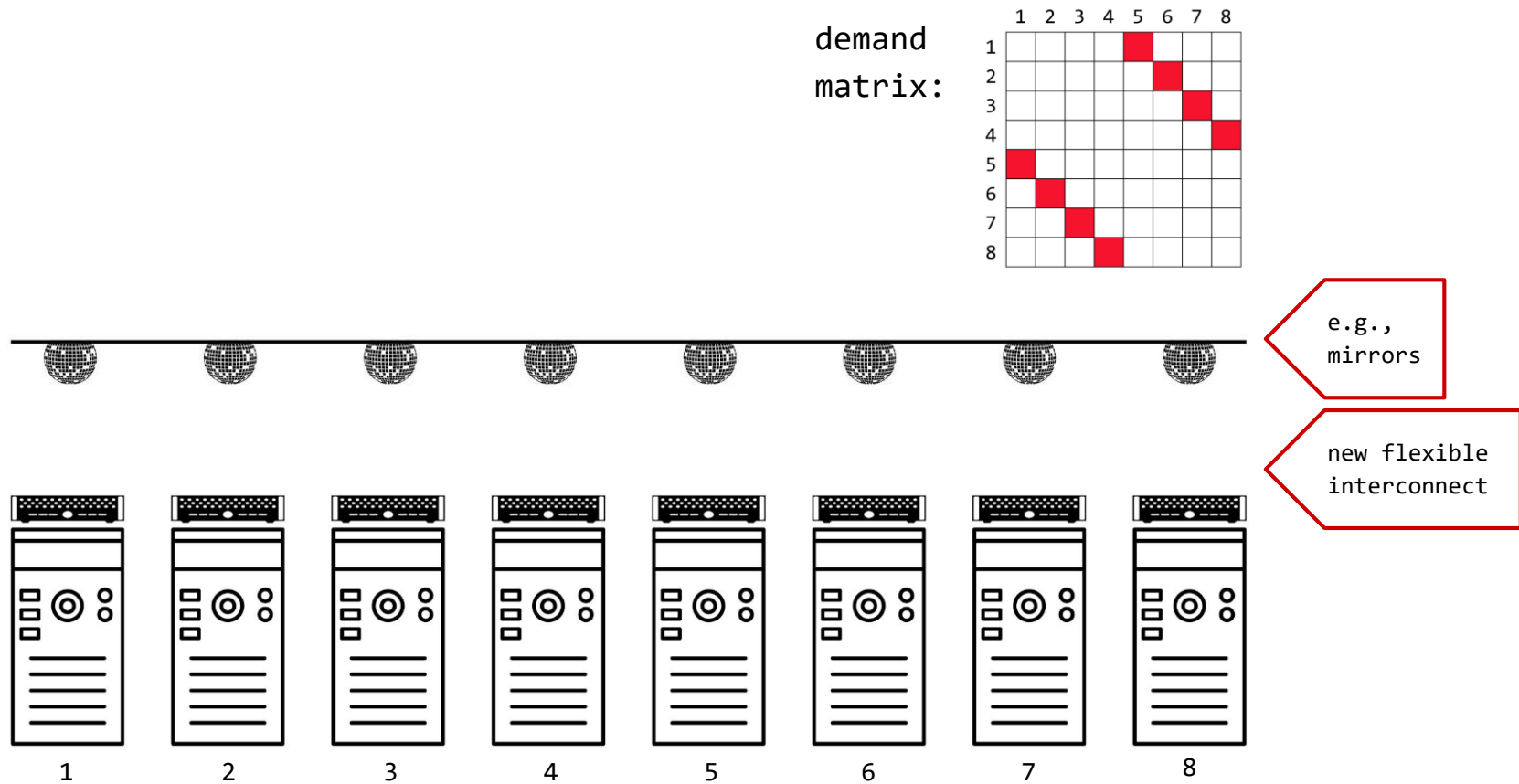
## Flexible and Demand-Aware Topologies





# Our Vision

## Flexible and Demand-Aware Topologies



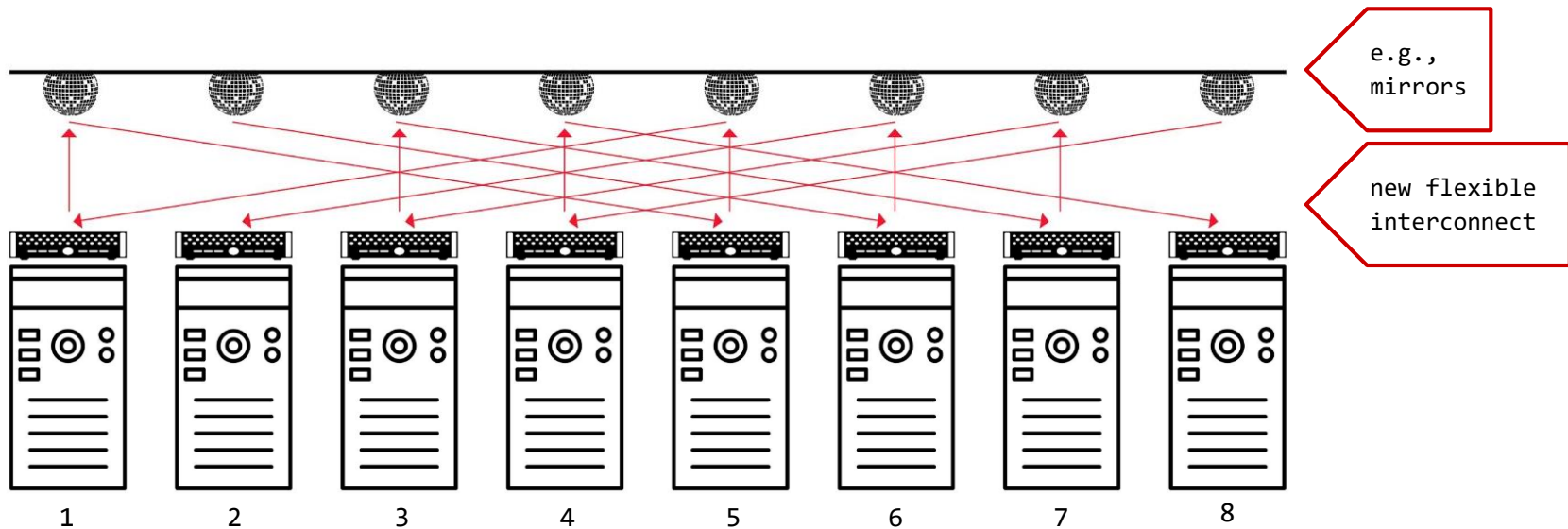
# Our Vision

## Flexible and Demand-Aware Topologies

Matches demand

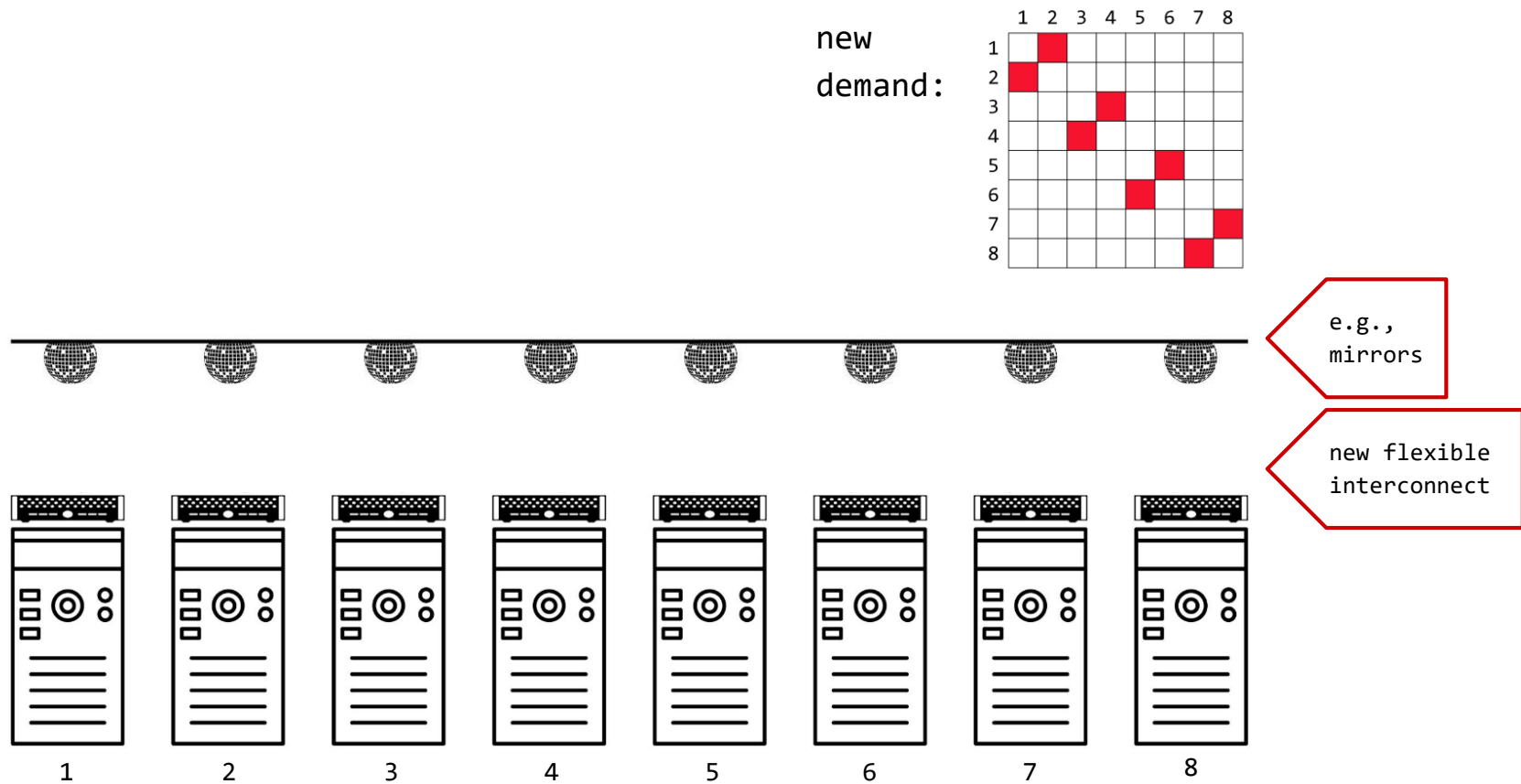
demand  
matrix:

	1	2	3	4	5	6	7	8
1					■			
2						■		
3							■	
4								■
5	■							
6		■						
7			■					
8				■				



# Our Vision

## Flexible and Demand-Aware Topologies



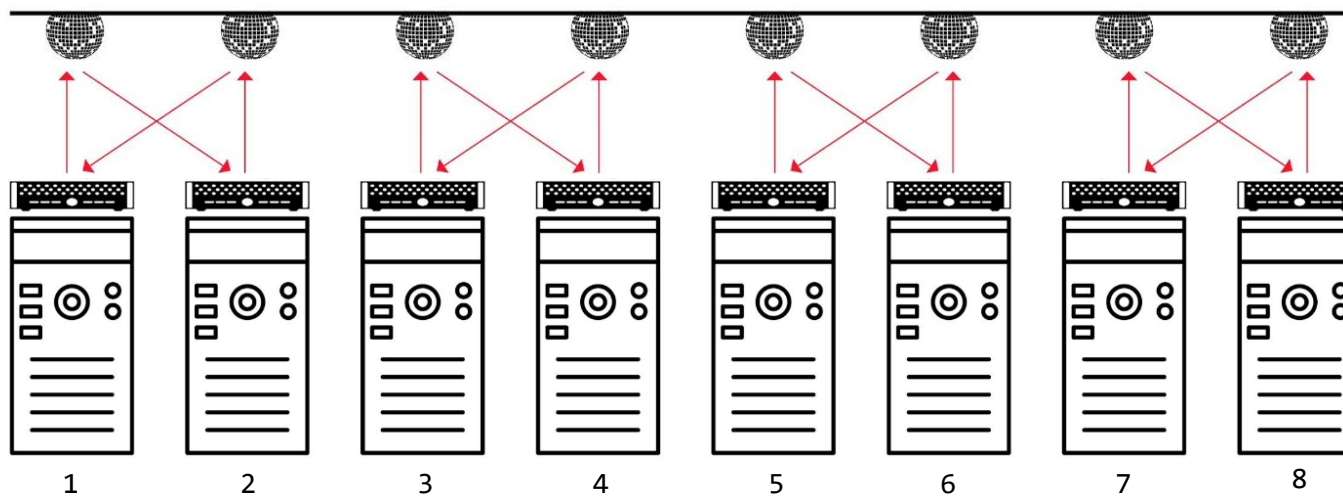
# Our Vision

## Flexible and Demand-Aware Topologies

Matches demand

new  
demand:

	1	2	3	4	5	6	7	8
1								
2								
3								
4								
5								
6								
7								
8								



e.g.,  
mirrors

new flexible  
interconnect

# Our Vision

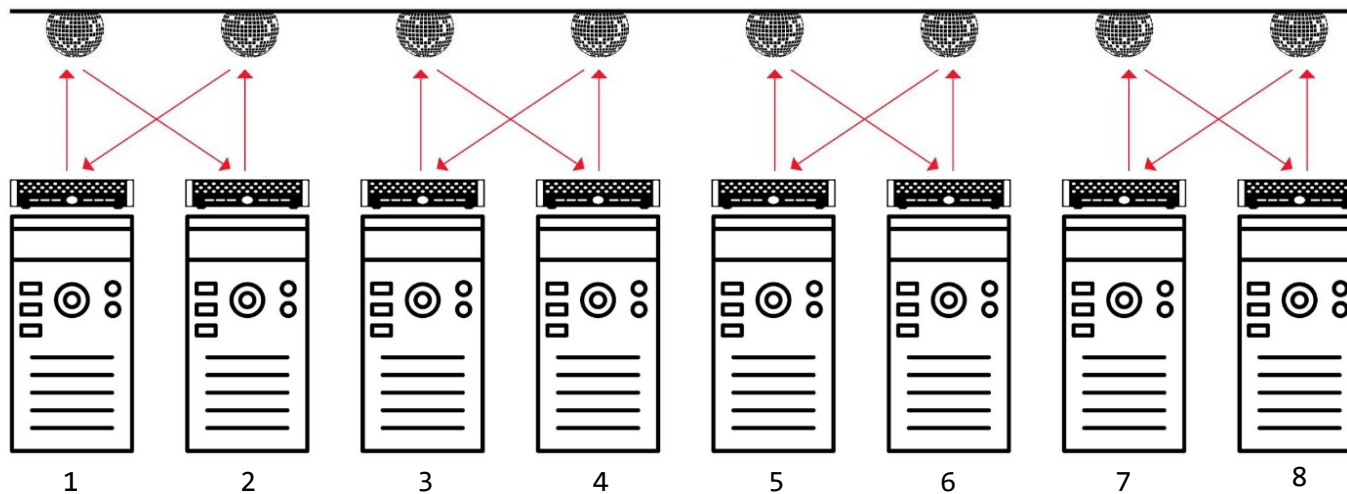
## Flexible and Demand-Aware Topologies



Self-Adjusting  
Networks

new  
demand:

	1	2	3	4	5	6	7	8
1								
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mirrors

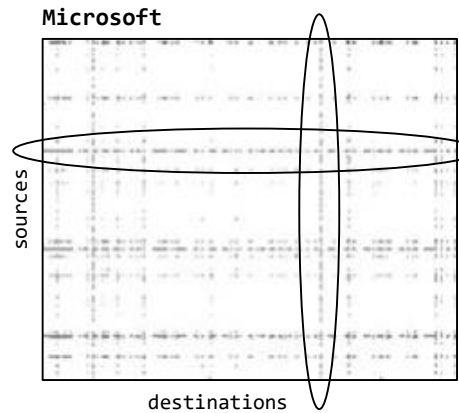
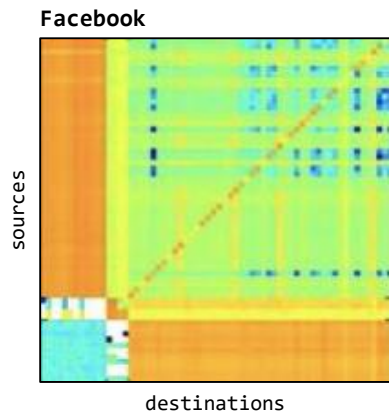
new flexible  
interconnect

# Our Motivation

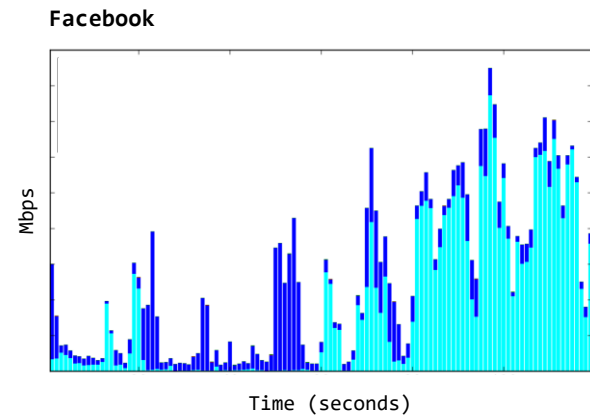
Much Structure in the Demand

Empirical studies:

traffic matrices **sparse** and **skewed**

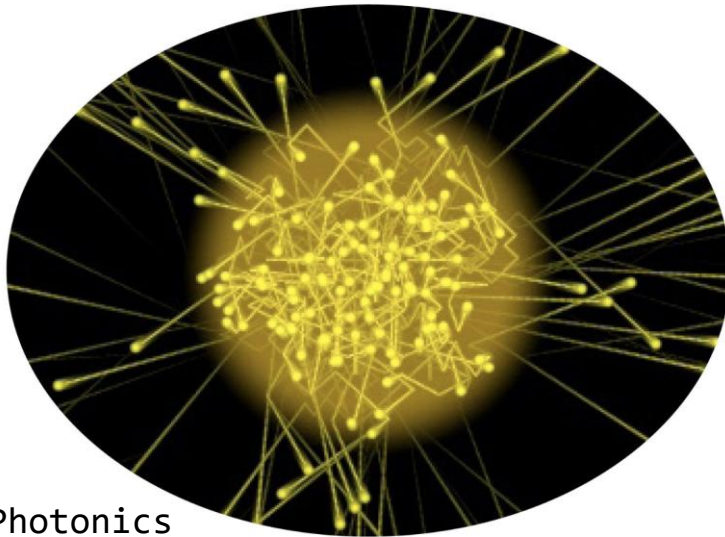


traffic **bursty** over time



My **hypothesis**: can be exploited.

# Sounds Crazy? Emerging Enabling Technology.



Photonics

H2020:

**“Photonics one of only five  
key enabling technologies  
for future prosperity.”**

US National Research Council:

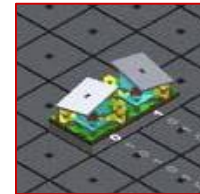
**“Photons are the new  
Electrons.”**

# Enabler

## Novel Reconfigurable Optical Switches

→ **Spectrum** of prototypes

- Different sizes, different reconfiguration times
- From our last year's ACM **SIGCOMM** workshop OptSys



Prototype 1



Prototype 2



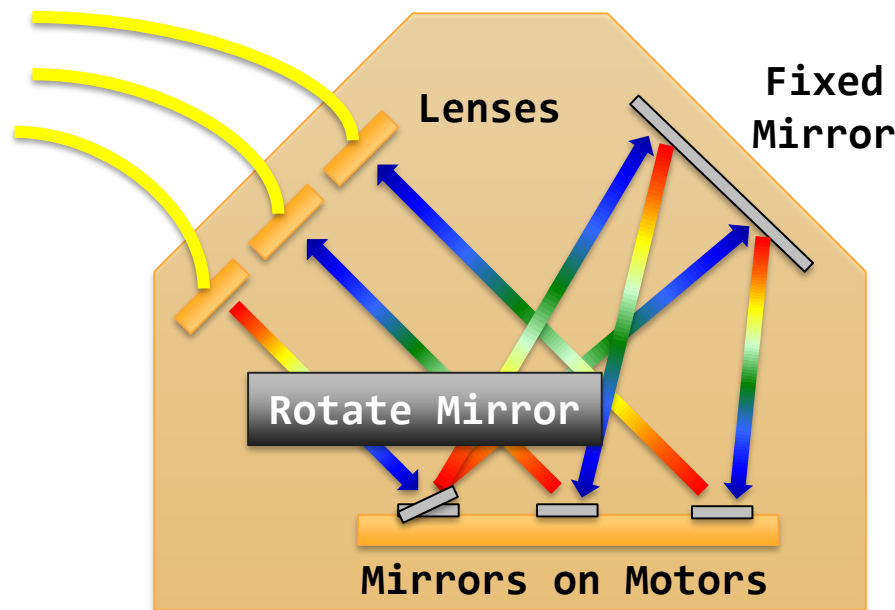
Prototype 3



# Example

## Optical Circuit Switch

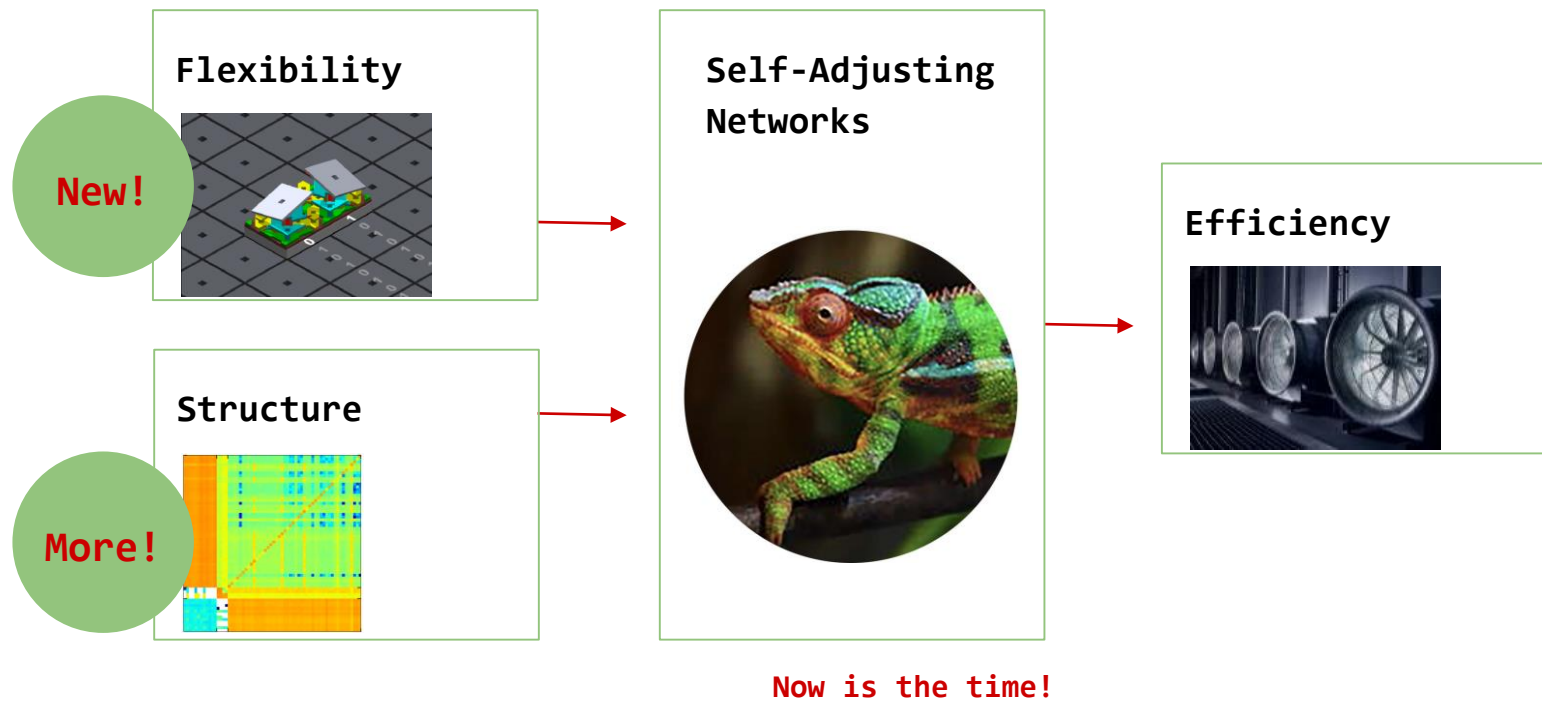
- Optical Circuit Switch rapid adaption of physical layer
  - Based on rotating mirrors



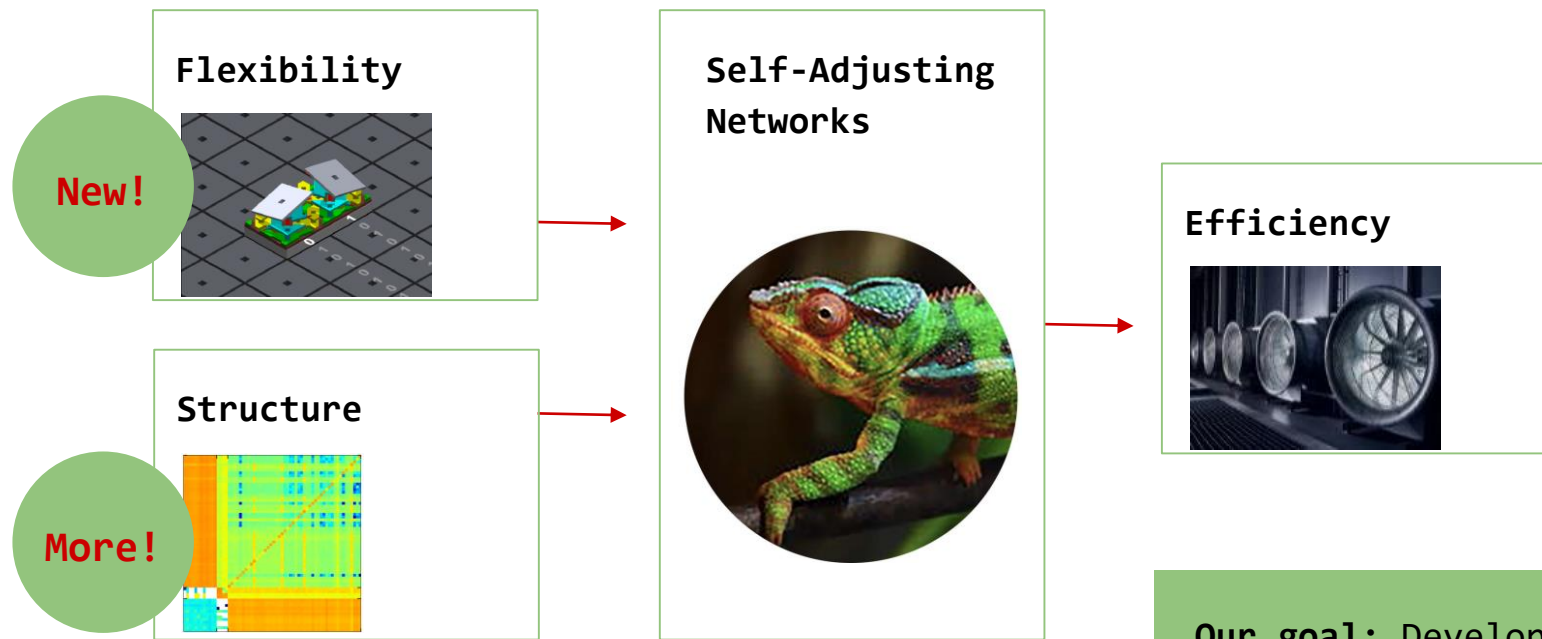
## Optical Circuit Switch

By Nathan Farrington, SIGCOMM 2010

# The Big Picture



# The Big Picture



Now is the time!

Our goal: Develop the theoretical **foundations** of demand-aware, self-adjusting networks.

# Unique Position

Demand-Aware, Self-Adjusting Systems

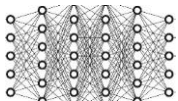
Everywhere, but mainly  
in software



Algorithmic trading



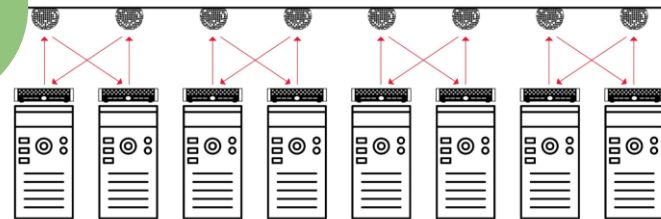
Recommender systems



Neural networks

VS

Our focus:  
in hardware



Question 1:

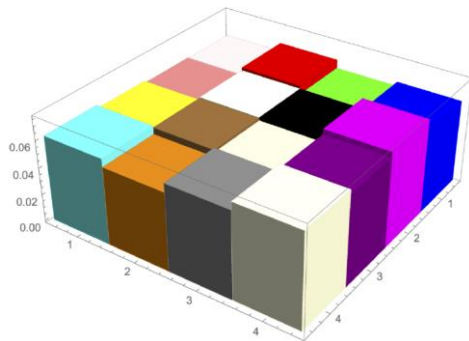
How to Quantify  
such “Structure”  
in the Demand?

# Intuition

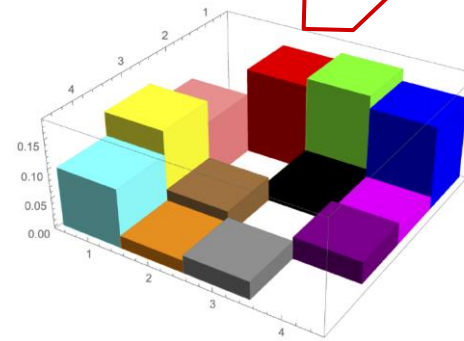
Which demand has more structure?

→ Traffic matrices of two different distributed ML applications

→ GPU-to-GPU



VS

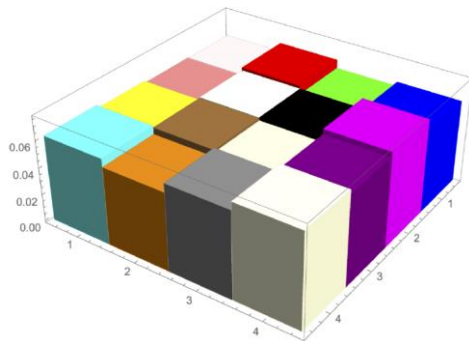


# Intuition

Which demand has more structure?

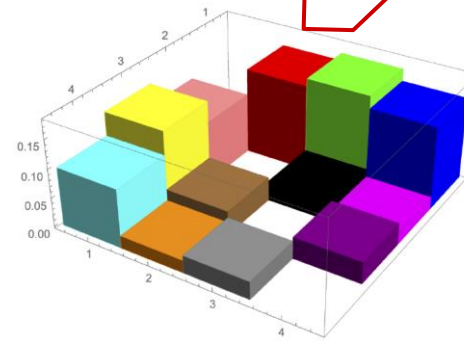
→ Traffic matrices of two different distributed ML applications

→ GPU-to-GPU



More uniform

VS



More structure

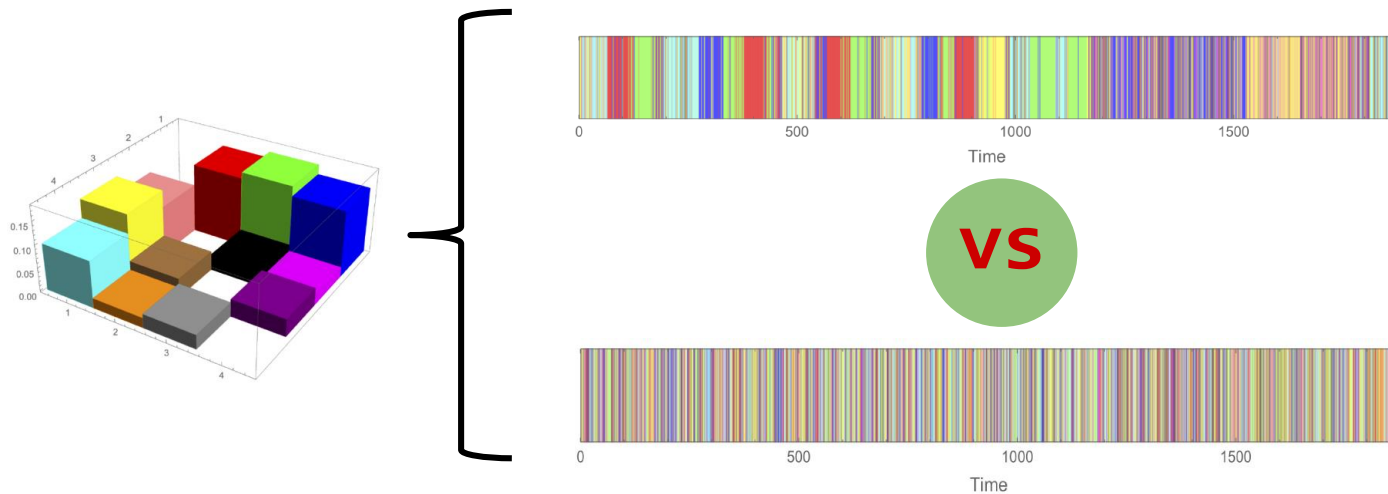
# Intuition

## Spatial vs temporal structure

→ Two different ways to generate same traffic matrix:

→ Same non-temporal structure

→ Which one has more structure?



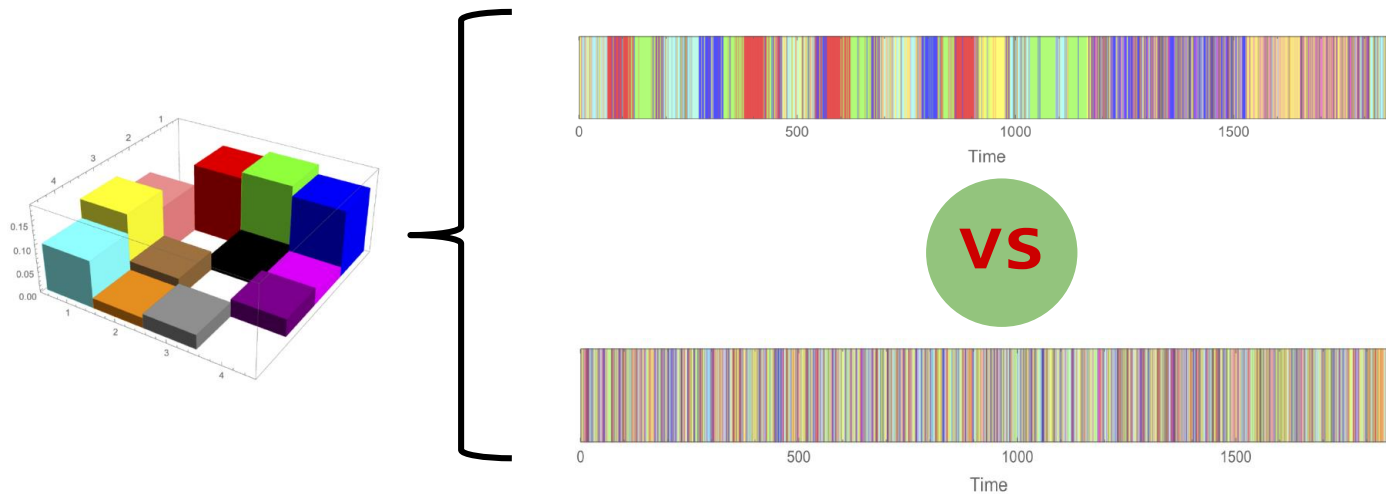


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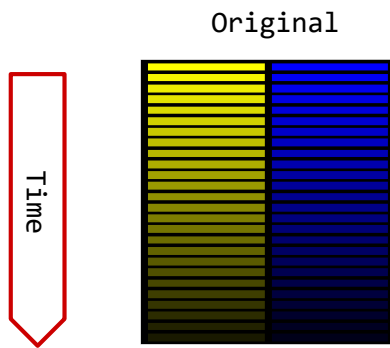


Systematically?

# Trace Complexity

Information-Theoretic Approach

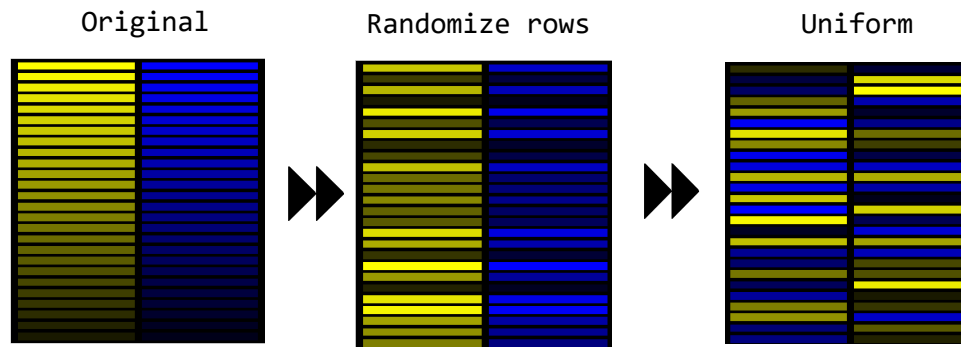
“Shuffle&Compress”



# Trace Complexity

Information-Theoretic Approach

“Shuffle&Compress”



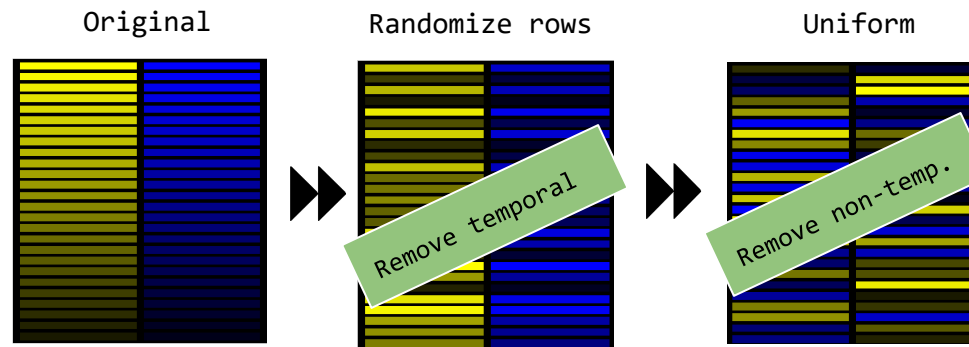
Increasing complexity (systematically randomized)

More structure (compresses better)

# Trace Complexity

Information-Theoretic Approach

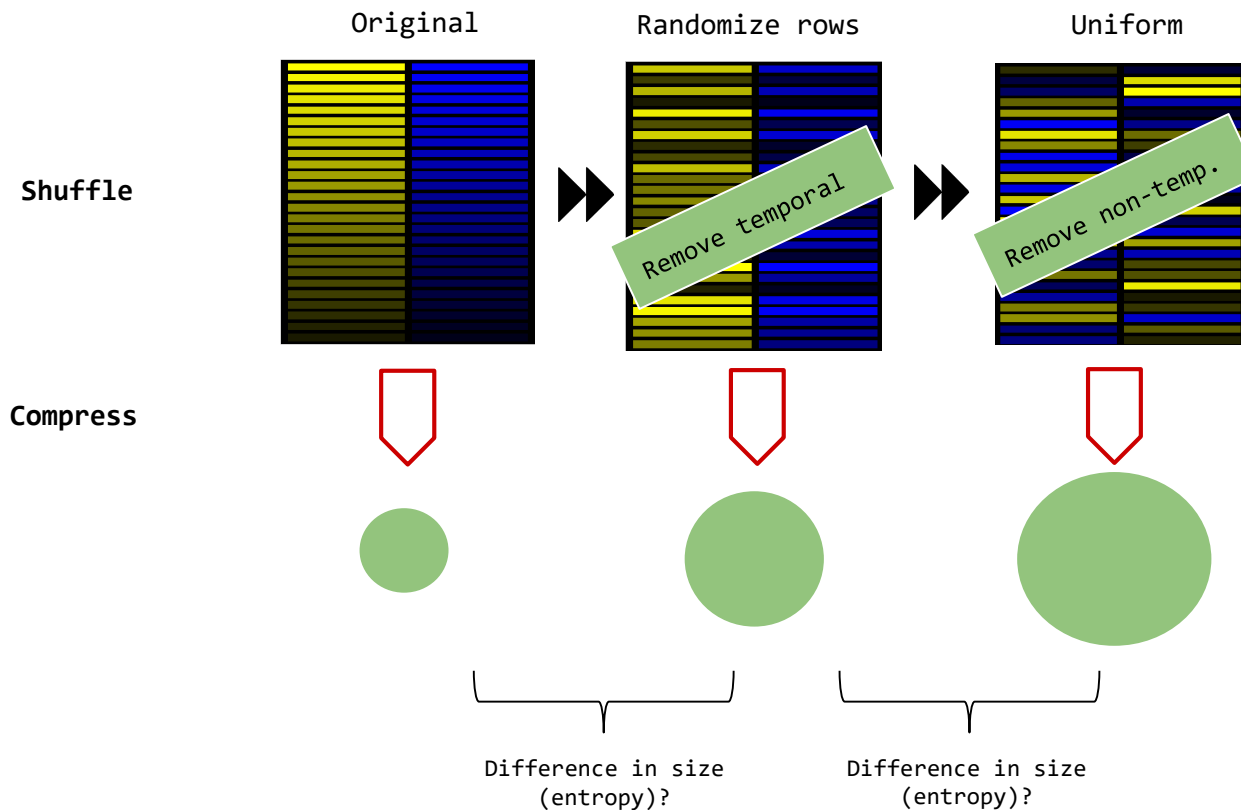
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# Trace Complexity

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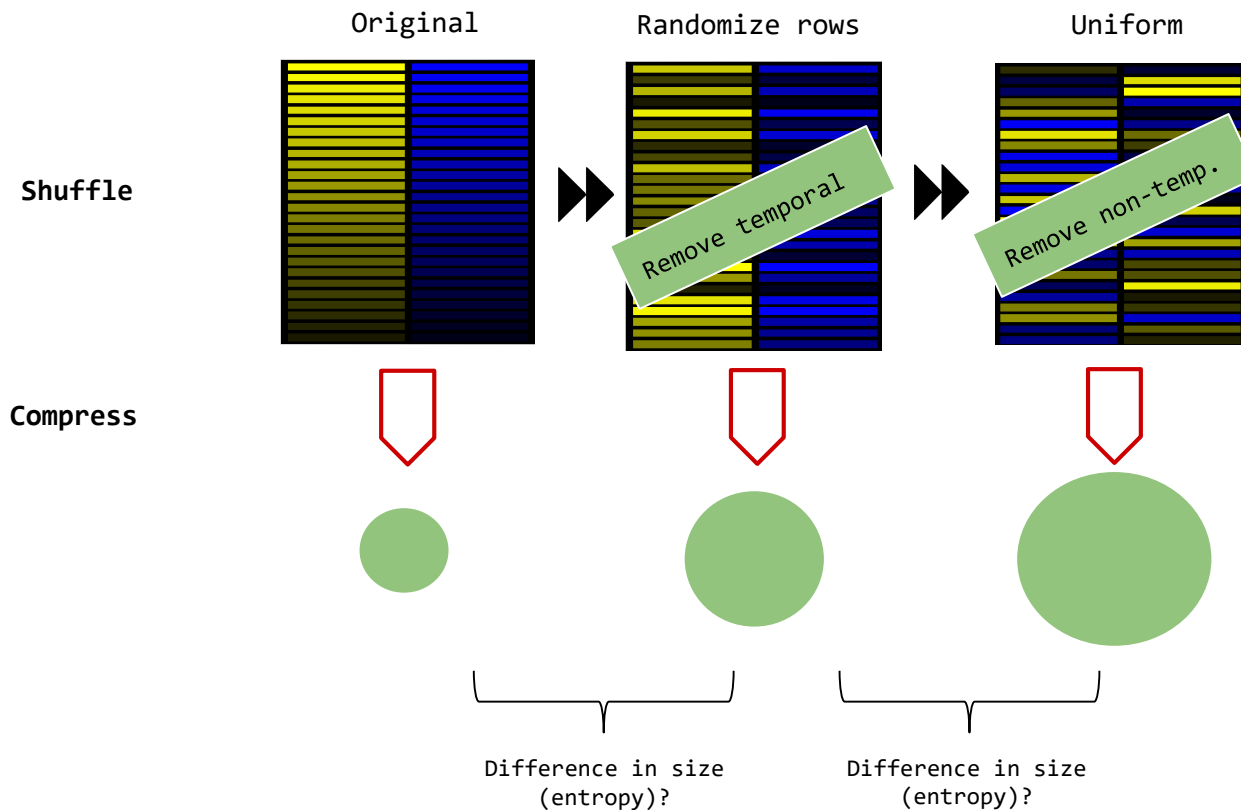
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# Trace Complexity

Information-Theoretic Approach

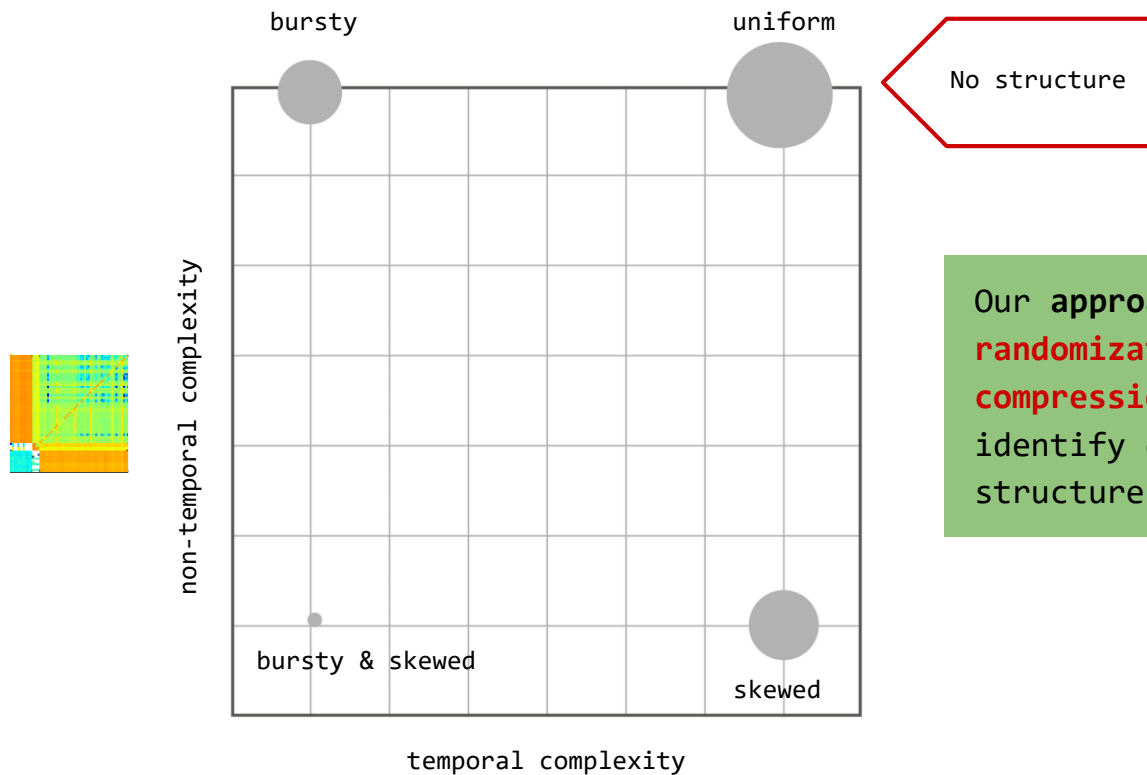
“Shuffle&Compress”



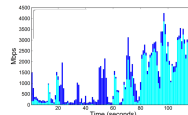
Can be used to define  
2-dimensional  
**complexity map!**

## Our Methodology

# Complexity Map

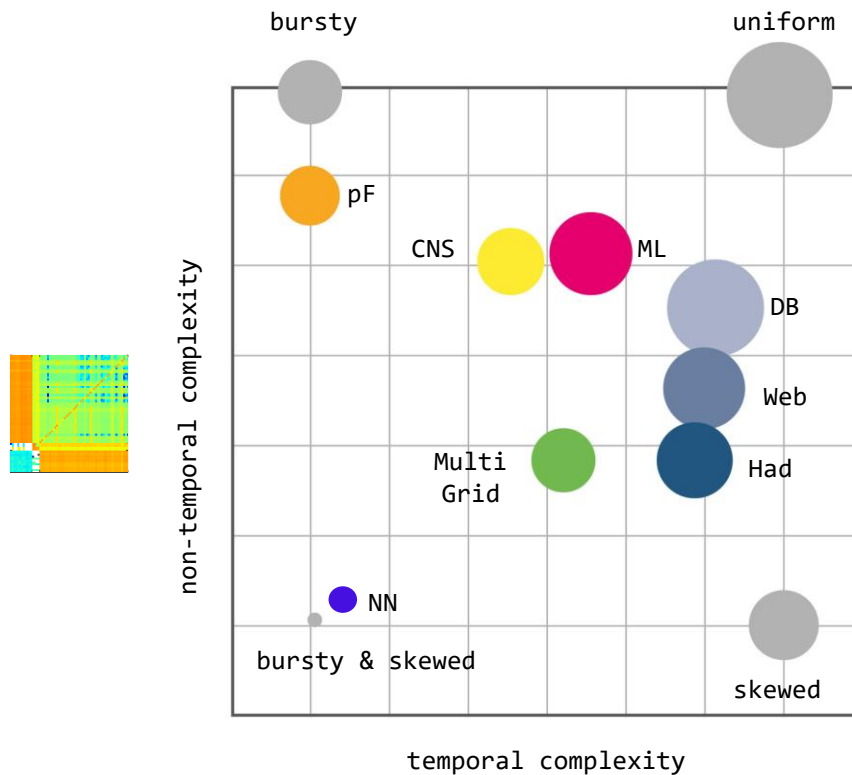


Our approach: iterative **randomization and compression** of trace to identify dimensions of structure.



## Our Methodology

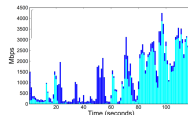
# Complexity Map



No structure

Our approach: iterative  
**randomization and  
compression** of trace to  
identify dimensions of  
structure.

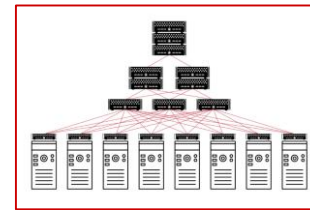
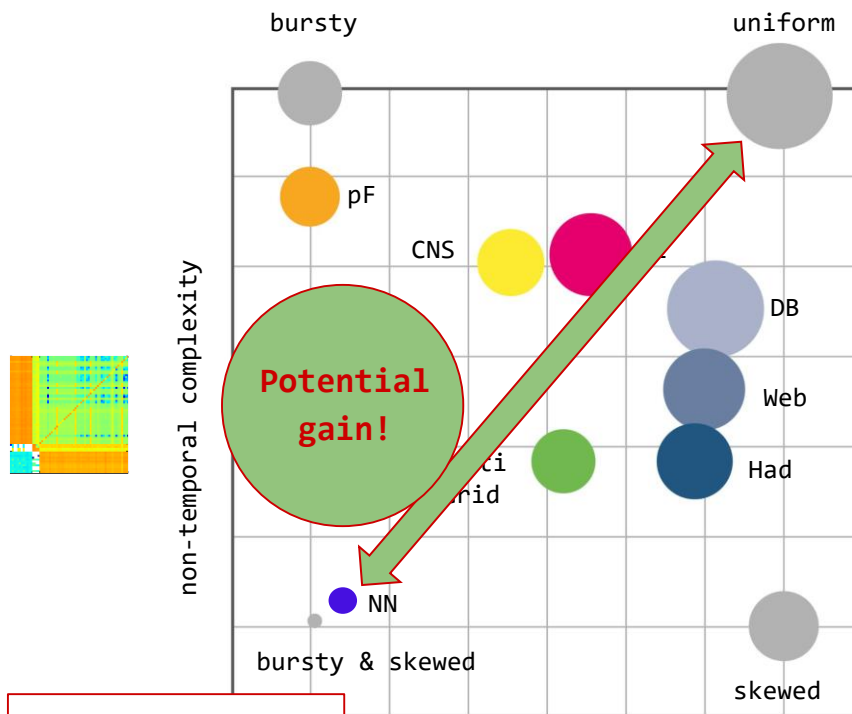
**Different  
structures!**





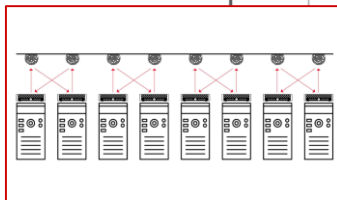
## Our Methodology

# Complexity Map

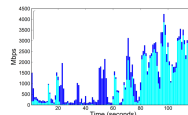


Our approach: iterative **randomization and compression** of trace to identify dimensions of structure.

**Different structures!**



temporal complexity



# ACM SIGMETRICS 2020

### On the Complexity of Traffic Traces and Implications

CHEN AVIN, School of Electrical and Computer Engineering, Ben Gurion University of the Negev, Israel

MANYA GHOBADI, Computer Science and Artificial Intelligence Laboratory, MIT, USA

CHEN GRINER, School of Electrical and Computer Engineering, Ben Gurion University of the Negev, Israel

STEFAN SCHMID, Faculty of Computer Science, University of Vienna, Austria

This paper presents a systematic approach to identify and quantify the types of structures featured by packet traces in communication networks. Our approach leverages an information-theoretic methodology, based on iterative randomization and compression of the packet trace, which allows us to systematically remove and measure dimensions of structure in the trace. In particular, we introduce the notion of *trace complexity* which approximates the entropy rate of a packet trace. Considering several real-world traces, we show that trace complexity can provide unique insights into the characteristics of various applications. Based on our approach, we also propose a traffic generator model able to produce a synthetic trace that matches the complexity levels of its corresponding real-world trace. Using a case study in the context of datacenters, we show that insights into the structure of packet traces can lead to improved demand-aware network designs: datacenter topologies that are optimized for specific traffic patterns.

CCS Concepts: • **Networks** → **Network performance evaluation**; **Network algorithms**; **Data center networks**; • **Mathematics of computing** → *Information theory*;

Additional Key Words and Phrases: trace complexity, self-adjusting networks, entropy rate, compress, complexity map, data centers

#### ACM Reference Format:

Chen Avin, Manya Ghobadi, Chen Griner, and Stefan Schmid. 2020. On the Complexity of Traffic Traces and Implications. *Proc. ACM Meas. Anal. Comput. Syst.* 4, 1, Article 20 (March 2020), 29 pages. <https://doi.org/10.1145/3379486>

#### 1 INTRODUCTION

Packet traces collected from networking applications, such as datacenter traffic, have been shown to feature much *structure*: datacenter traffic matrices are sparse and skewed [16, 39], exhibit

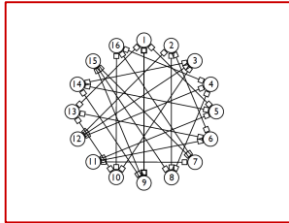
Question 2:

Given This Structure,  
What Can Be Achieved?  
Metrics and Algorithms?

A first insight: entropy of the demand.

# Models and Connection to Datastructures & Coding

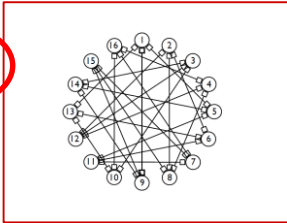
**Oblivious** networks  
(worst-case traffic)



More structure: **lower routing cost**

# Models and Connection to Datastructures & Coding

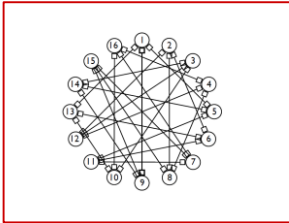
**Oblivious** networks  
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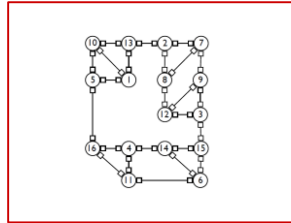
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# Models and Connection to Datastructures & Coding

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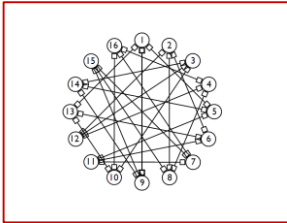
**Demand-aware** networks  
(spatial structure)



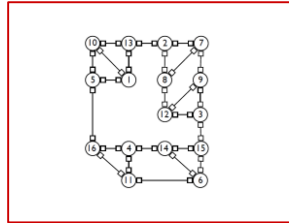
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# Models and Connection to Datastructures & Coding

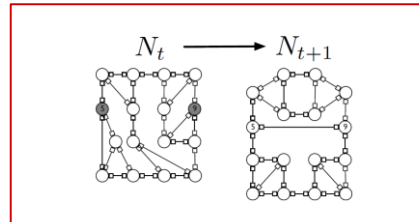
**Oblivious** networks  
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**Demand-aware** networks  
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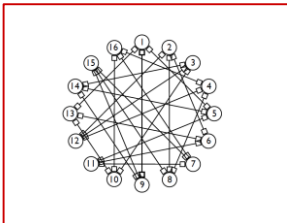
**Self-adjusting** networks  
(temporal structure)



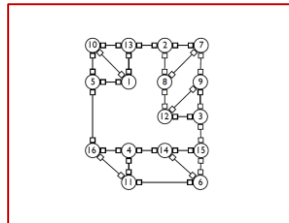
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# Models and Connection to Datastructures & Coding

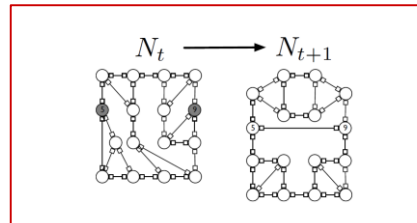
**Oblivious** networks  
(worst-case traffic)



**Demand-aware** networks  
(spatial structure)

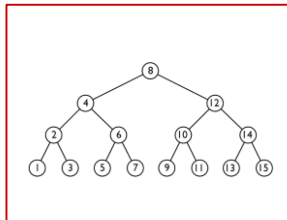


**Self-adjusting** networks  
(temporal structure)

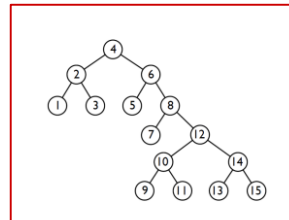


More structure: **lower routing cost**

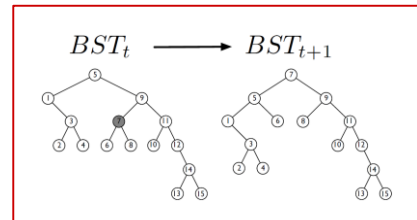
Traditional BST  
(Worst-case coding)



Demand-aware BST  
(Huffman coding)



Self-adjusting BST  
(Dynamic Huffman coding)

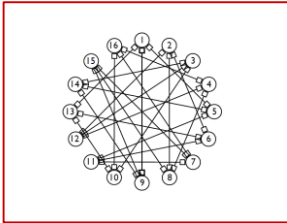


More structure: improved **access cost** / shorter **codes**

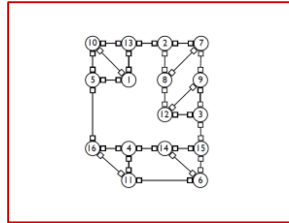


# Models and Connection to Datastructures & Coding

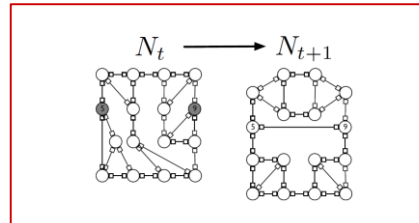
**Oblivious** networks  
(worst-case traffic)



**Demand-aware** networks  
(spatial structure)

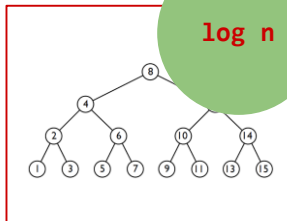


**Self-adjusting** networks  
(temporal structure)



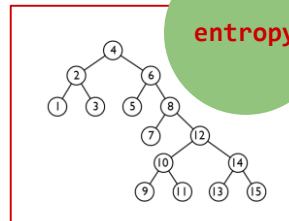
More structure: **lower routing cost**

Traditional BST  
(Worst-case)



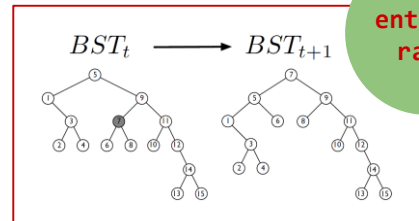
**log n**

Demand-aware BST  
(Huffman coding)



**entropy**

Self-adjusting BST  
(Dynamic Huffman coding)

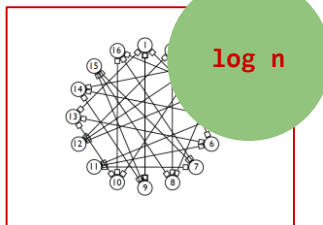


**entropy rate**

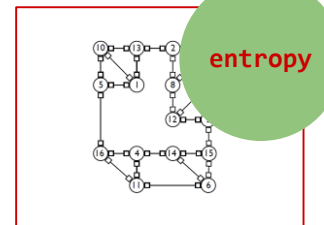
More structure: improved **access cost** / shorter **codes**

# Models and Connection to Datastructures & Coding

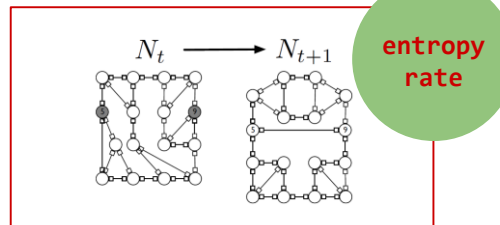
Traditional networks  
(worst-case traffic)



Demand-aware networks  
(spatial structure)



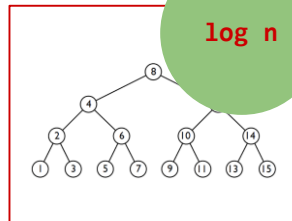
Self-adjusting networks  
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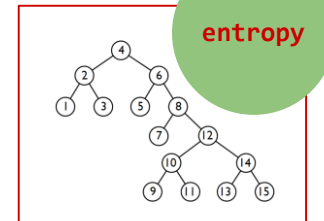
More than  
an analogy!

More structure  $\rightarrow$  lower routing cost

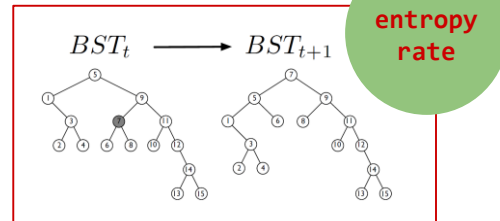
Traditional BST  
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Demand-aware BST  
(Huffman coding)



Self-adjusting BST  
(Dynamic Huffman coding)



More structure: improved access cost / shorter codes

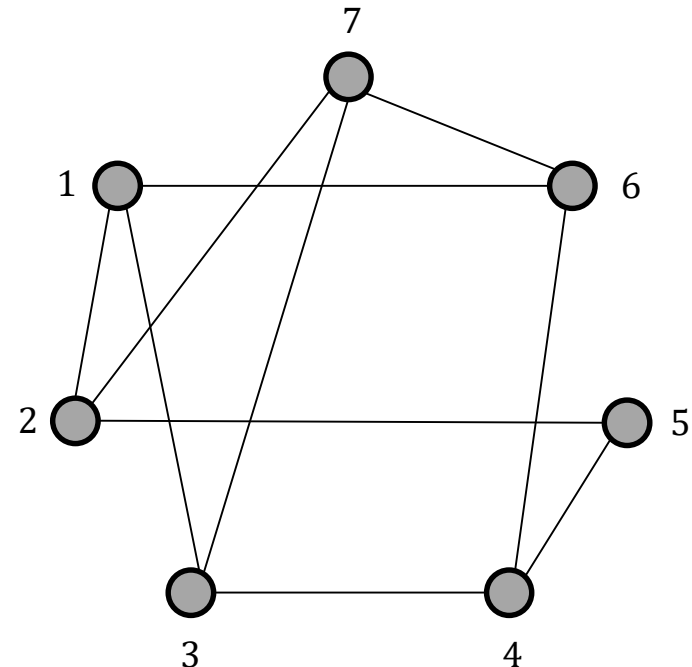
Generalize methodology:  
... and transfer  
entropy bounds and  
algorithms of data-  
structures to networks.

First result:  
Demand-aware networks  
of asymptotically  
optimal route lengths.

## Case Study “Route Lengths”

# Constant-Degree Demand-Aware Network

		Destinations						
		1	2	3	4	5	6	7
Sources	1	0	$\frac{2}{65}$	$\frac{1}{13}$	$\frac{1}{65}$	$\frac{1}{65}$	$\frac{2}{65}$	$\frac{3}{65}$
	2	$\frac{2}{65}$	0	$\frac{1}{65}$	0	0	0	$\frac{2}{65}$
	3	$\frac{1}{13}$	$\frac{1}{65}$	0	$\frac{2}{65}$	0	0	$\frac{1}{13}$
	4	$\frac{1}{65}$	0	$\frac{2}{65}$	0	$\frac{4}{65}$	0	0
	5	$\frac{1}{65}$	0	$\frac{3}{65}$	$\frac{4}{65}$	0	0	0
	6	$\frac{2}{65}$	0	0	0	0	0	$\frac{3}{65}$
	7	$\frac{3}{65}$	$\frac{2}{65}$	$\frac{1}{13}$	0	0	$\frac{3}{65}$	0



$$\text{ERL}(\mathcal{D}, N) = \sum_{(u,v) \in \mathcal{D}} p(u, v) \cdot d_N(u, v)$$

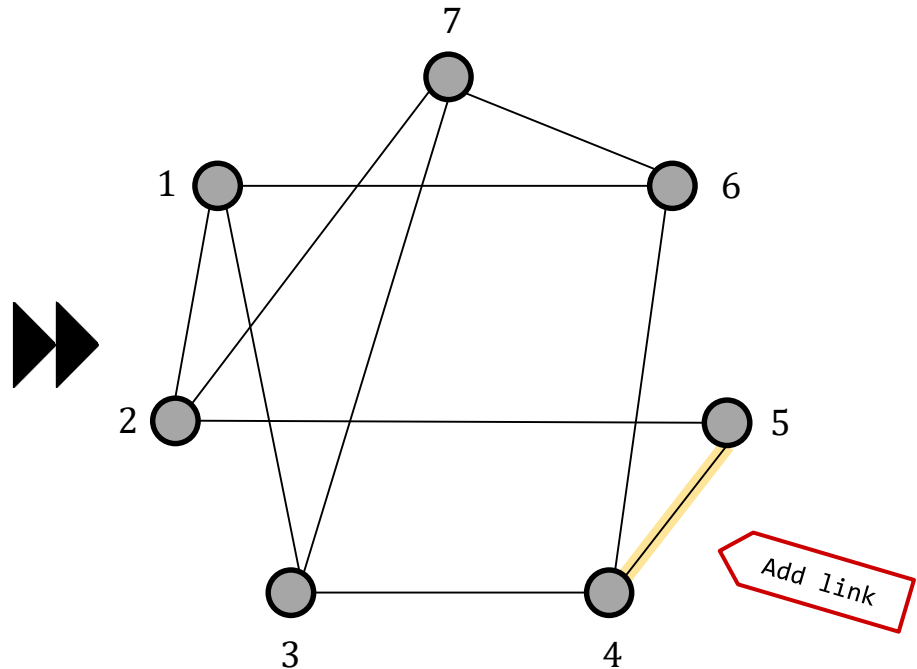
## Case Study “Route Lengths”

# Constant-Degree Demand-Aware Network

Sources

	Destinations						
	1	2	3	4	5	6	7
1	0	$\frac{2}{65}$	$\frac{1}{13}$	$\frac{1}{65}$	$\frac{1}{65}$	$\frac{2}{65}$	$\frac{3}{65}$
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6	$\frac{2}{65}$	0		0	0	0	$\frac{3}{65}$
7	$\frac{3}{65}$		$\frac{1}{13}$	0	0	$\frac{3}{65}$	0

Much from 4 to 5



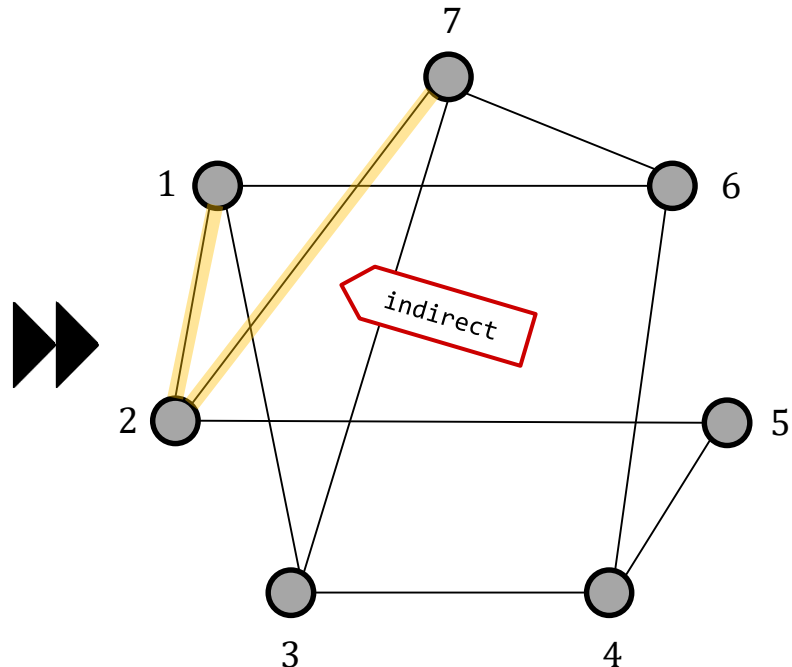
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## Case Study “Route Lengths”

# Constant-Degree Demand-Aware Network

Communicated with many

		Destinations						
		1	2	3	4	5	6	7
Sources	1	0	$\frac{2}{65}$	$\frac{1}{13}$	$\frac{1}{65}$	$\frac{1}{65}$	$\frac{2}{65}$	$\frac{3}{65}$
	2	$\frac{2}{65}$	0	$\frac{1}{65}$	0	0	0	$\frac{2}{65}$
	3	$\frac{1}{13}$	$\frac{1}{65}$	0	$\frac{2}{65}$	0	0	$\frac{1}{13}$
	4	$\frac{1}{65}$	0	$\frac{2}{65}$	0	$\frac{4}{65}$	0	0
	5	$\frac{1}{65}$	0	$\frac{3}{65}$	$\frac{4}{65}$	0	0	0
	6	$\frac{2}{65}$	0	0	0	0	0	$\frac{3}{65}$
	7	$\frac{3}{65}$	$\frac{2}{65}$	$\frac{1}{13}$	0	0	$\frac{3}{65}$	0



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## Case Study “Route Lengths”

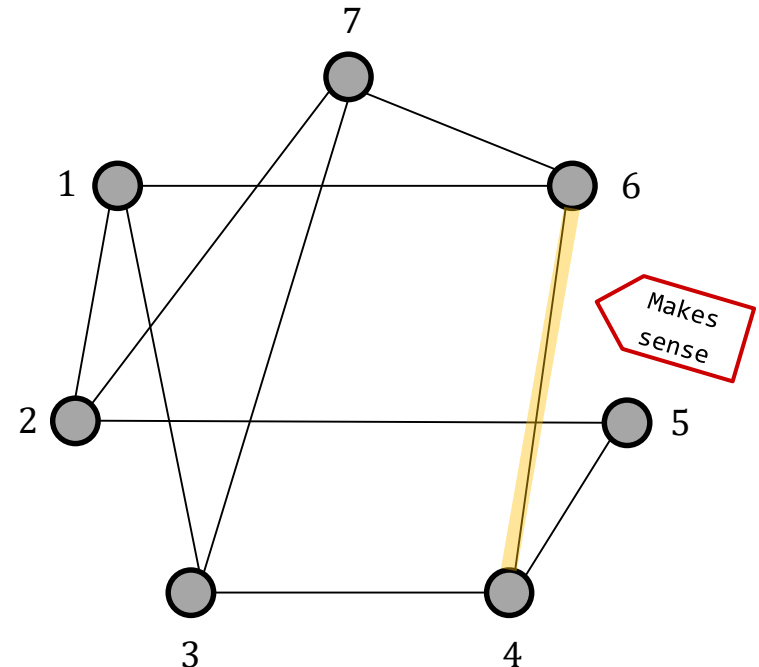
# Constant-Degree Demand-Aware Network

Destinations

	1	2	3	4	5	6	7
1	0	$\frac{2}{65}$	$\frac{1}{13}$	$\frac{1}{65}$	$\frac{1}{65}$	$\frac{2}{65}$	$\frac{3}{65}$
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6	$\frac{2}{65}$	0	0	0	0	0	$\frac{3}{65}$
7	$\frac{3}{65}$	$\frac{2}{65}$	$\frac{1}{13}$	0	0	$\frac{3}{65}$	0

Sources

Don't  
communicate



Makes  
sense

$$\text{ERL}(\mathcal{D}, N) = \sum_{(u,v) \in \mathcal{D}} p(u, v) \cdot d_N(u, v)$$

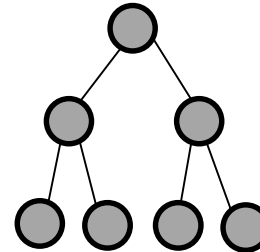
# Examples

→ DAN for  $\Delta=3$

→ E.g., complete **binary**

✓ **tree** would be **log n**

→ Can we do better?



→ DAN for  $\Delta=2$

→ Set of **lines** and **cycles**



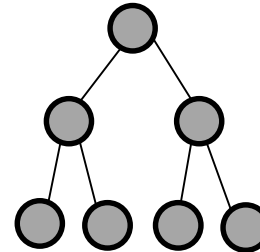
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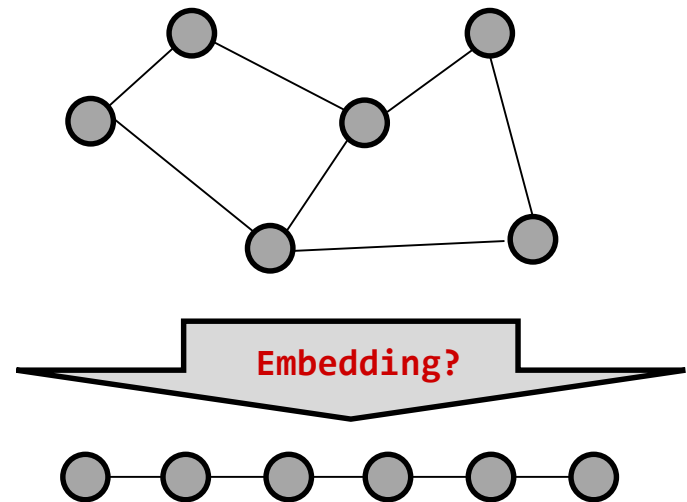
**How  
hard?**



Related Problem

# Virtual Network Embedding Problem (VNEP)

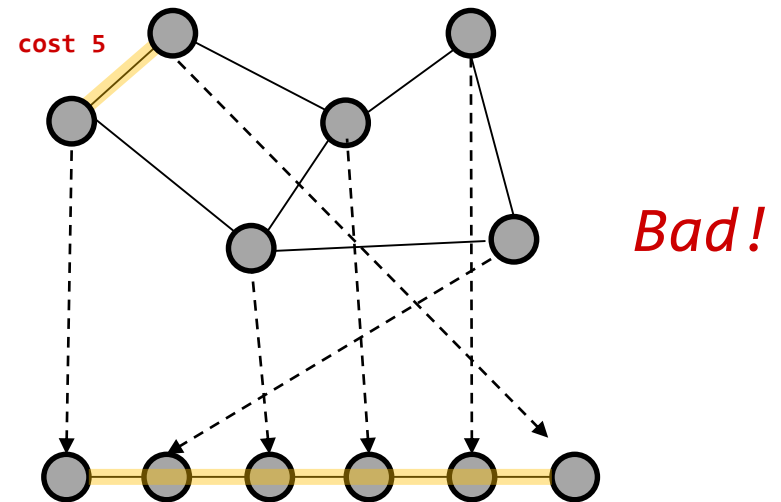
Example  $\Delta=2$ : A Minimum Linear  
Arrangement (MLA) Problem  
→ Minimizes sum of virtual  
edges



Related Problem

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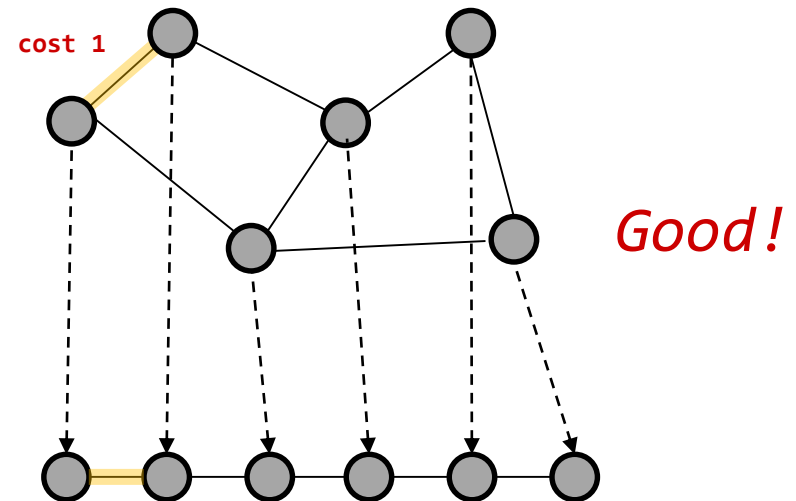
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Related Problem

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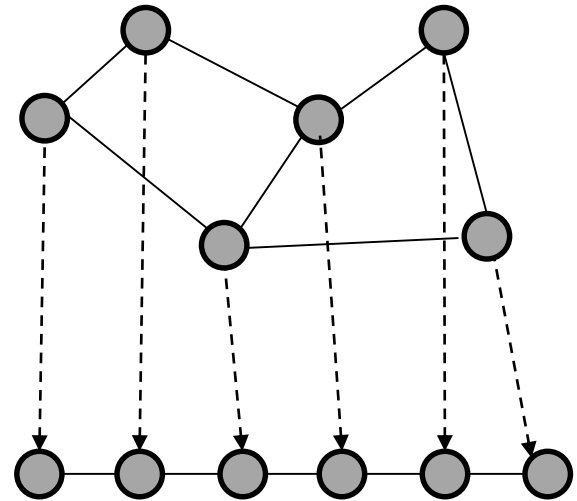


Related Problem

# Virtual Network Embedding Problem (VNEP)

Example  $\Delta=2$ : A Minimum Linear  
Arrangement (**MLA**) Problem  
→ Minimizes sum of virtual  
edges

MLA is **NP-hard**  
→ ... and so is our problem!



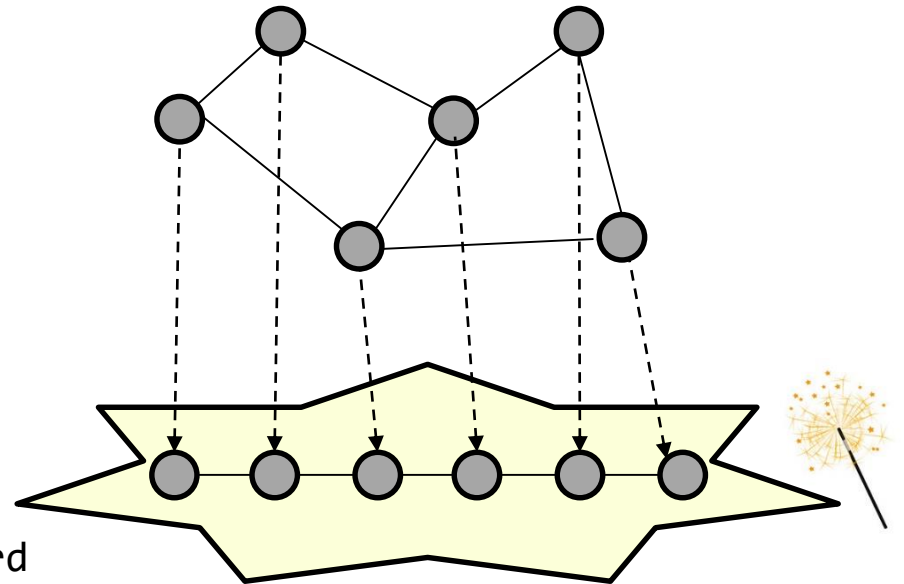
Related Problem

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Example  $\Delta=2$ : A Minimum Linear  
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But what about  $\Delta > 2$ ?  
→ Embedding problem still hard  
→ But we have a new **degree of  
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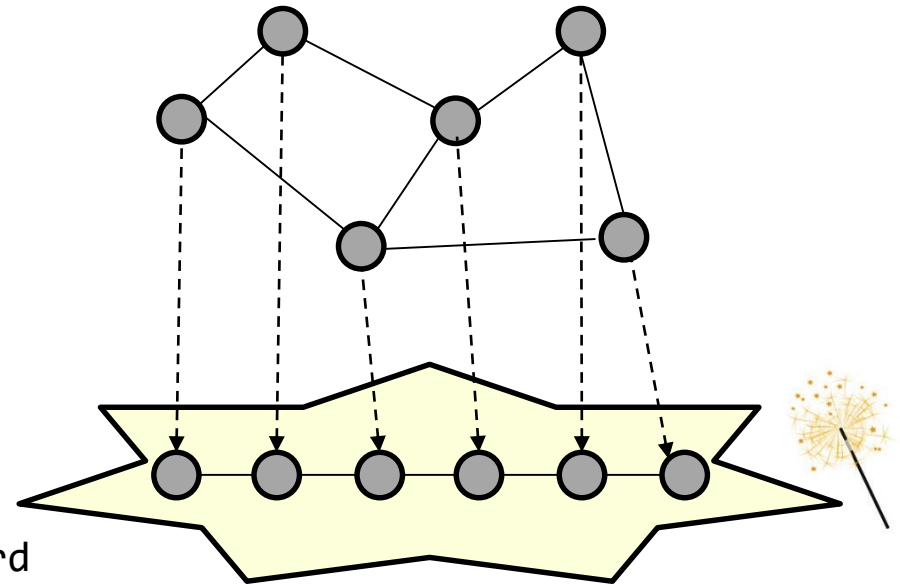
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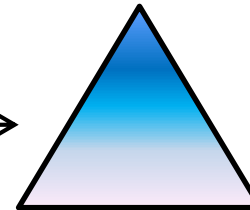
But what about  $\Delta > 2$ ?  
→ Embedding problem still hard  
→ But we have a new **degree of  
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Simplifies problem?!

# Algorithm: Idea

		Destinations						
		1	2	3	4	5	6	7
Sources	1	0	$\frac{2}{65}$	$\frac{1}{13}$	$\frac{1}{65}$	$\frac{1}{65}$	$\frac{2}{65}$	$\frac{3}{65}$
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	7	$\frac{3}{65}$	$\frac{2}{65}$	$\frac{1}{13}$	0	0	$\frac{3}{65}$	0



Huffman tree:  
“ego-tree”

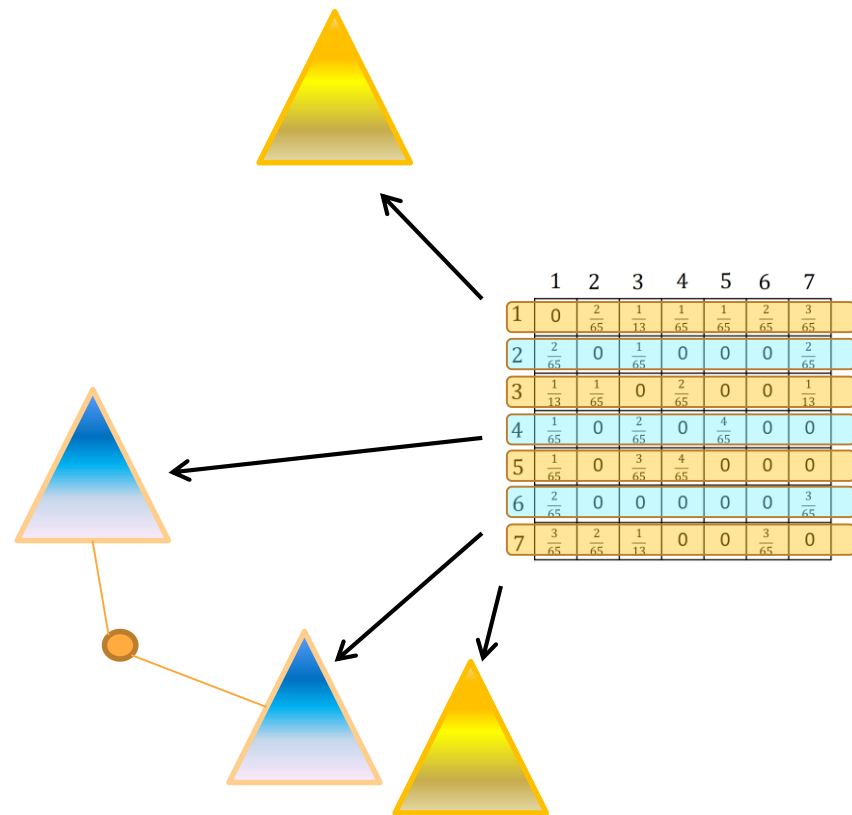
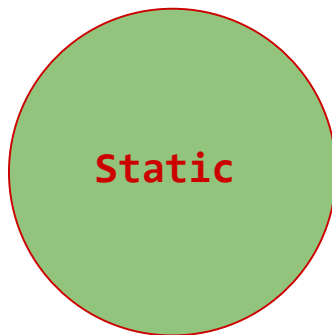
# Entropy Upper Bound

→ Idea for algorithm:

- union of trees
- reduce degree
- but keep distances

→ Ok for sparse demands

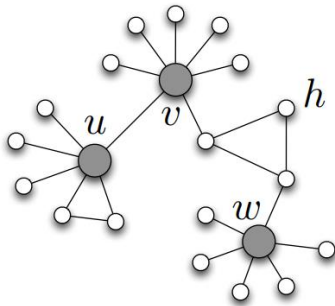
- not everyone gets tree
- helper nodes



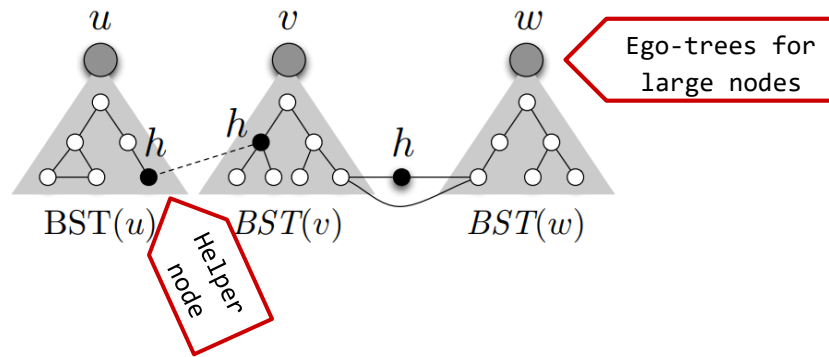


# Intuition of Algorithm

Demand graph:



Demand-aware network:



## Further Reading

# TON 2016, DISC 2017, CCR 2019, INFOCOM 2019

### Demand-Aware Network Designs of Bounded Degree\*

Chen Avin<sup>1</sup>, Kaushik Mondal<sup>1</sup>, and Stefan Schmid<sup>2</sup>

<sup>1</sup> Communication Systems Engineering Department  
Ben Gurion University of the Negev, Israel  
avin@cse.bgu.ac.il, mondal@post.bgu.ac.il

<sup>2</sup> Department of Computer Science  
Aalborg University, Denmark  
schmiste@cs.aau.dk

#### Abstract

Traditionally, networks such as datacenter interconnects are designed to optimize worst-case performance under *arbitrary* traffic patterns. Such network designs can however be far from optimal when considering the *actual* workloads and traffic patterns which they serve. This insight led to the development of demand-aware datacenter interconnects which can be reconfigured depending on the workload.

Motivated by these trends, this paper initiates the algorithmic study of demand-aware networks (DANs), and in particular the design of bounded degree networks. The inputs to the network

### Toward Demand-Aware Networking: A Theory for Self-Adjusting Networks

Chen Avin  
Ben Gurion University, Israel  
avin@cse.bgu.ac.il

Stefan Schmid  
University of Vienna, Austria  
stefan\_schmid@univie.ac.at

This article is an editorial note submitted to CCR. It has NOT been peer reviewed.  
The authors take full responsibility for this article's technical content. Comments can be posted through CCR Online.

#### ABSTRACT

The physical topology is emerging as the next frontier in an ongoing effort to render communication networks more flexible. While first empirical results indicate that these flexibilities can be exploited to reconfigure and optimize the network toward the workload it serves and, e.g., providing the same bandwidth at lower infrastructure cost, only little is known today about the fundamental algorithmic problems underlying the design of reconfigurable networks. This paper initiates the study of the theory of demand-aware, self-adjusting networks. Our main position is that self-adjusting networks should be seen through the lens of self-adjusting data-



Figure 1: Taxonomy of topology optimization

design of efficient datacenter networks has received much attention over the last years. The topologies underlying mod-

## SplayNet: Towards Locally Self-Adjusting Networks

Stefan Schmid\*, Chen Avin\*, Christian Scheideler, Michael Borokhovich, Bernhard Haeupler, Zvi Lotker

**Abstract**—This paper initiates the study of locally self-adjusting networks: networks whose topology adapts dynamically and in a decentralized manner, to the communication pattern  $\sigma$ . Our vision can be seen as a distributed generalization of the self-adjusting datastructures introduced by Sleator and Tarjan [22]: In contrast to their splay trees which dynamically optimize the lookup costs from a *single node* (namely the tree root), we seek to minimize the routing cost between arbitrary *communication pairs* in the network.

As a first step, we study distributed binary search trees (BSTs), which are attractive for their support of greedy routing. We introduce a simple model which captures the fundamental tradeoff between the benefits and costs of self-adjusting networks. We present the *SplayNet* algorithm and formally analyze its performance, and prove its optimality in specific case studies. We also introduce lower bound techniques based on interval cuts and

toward static metrics, such as the diameter or the length of the longest route: the self-adjusting paradigm has not spilled over to distributed networks yet.

We, in this paper, initiate the study of a distributed generalization of self-optimizing datastructures. This is a non-trivial generalization of the classic splay tree concept: While in classic BSTs, a *lookup request* always originates from the same node, the tree root, distributed datastructures and networks such as skip graphs [2], [13] have to support *routing requests* between arbitrary pairs (or *peers*) of communicating nodes; in other words, both the source as well as the destination of the requests become variable. Figure 1 illustrates the difference between classic and distributed binary search trees.

In this paper, we ask: Can we gain similar benefits from self-

## Demand-Aware Network Design with Minimal Congestion and Route Lengths

Chen Avin  
Communication Systems Engineering Dept.  
Ben Gurion University of the Negev, Israel

Kaushik Mondal  
Communication Systems Engineering Dept.  
Ben Gurion University of the Negev, Israel

Stefan Schmid  
Faculty of Computer Science  
University of Vienna, Austria

**Abstract**—Emerging communication technologies allow to reconfigure the physical network topology at runtime, enabling *demand-aware networks (DANs)*: networks whose topology is optimized toward the workload they serve. However, today, only little is known about the fundamental algorithmic problems underlying the design of such demand-aware networks. This paper presents the first bounded-degree, demand-aware network, *d-DAN*, which minimizes both congestion and route lengths. The designed network is provably (asymptotically) optimal in each dimension individually: we show that there do not exist any bounded-degree networks providing shorter routes (independently of the load), nor do there exist networks providing lower loads (independently of the route lengths). The main building block of the designed *d-DAN* networks are *ego-trees*: communication sources arrange their communication partners in an optimal tree, individually. While the union of these ego-trees forms the basic structure of *d-DANs*, further techniques are presented to ensure bounded degrees (for scalability).

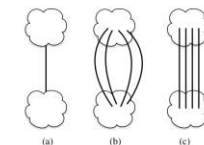


Fig. 1. Challenge of designing demand-aware networks: (a) Optimizing for route lengths only may result in bottlenecks and high loads. (b) Optimizing for congestion only, by distributing load across multiple paths, can result in long routes. (c) Ideally, we aim to design networks that minimize both congestion and route lengths, using a small number of links (constant degree).

#### 1. INTRODUCTION

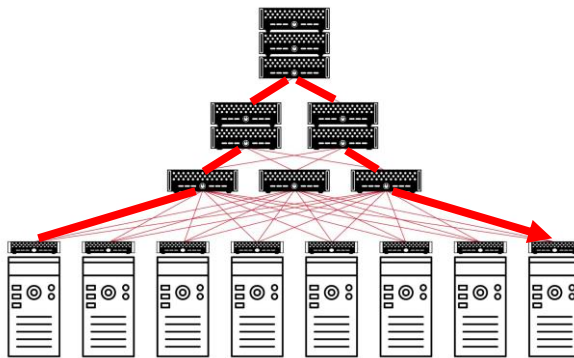
##### A. Motivation

Data center networks have become a critical infrastructure of our digital society. With the trend toward more data-intensive applications, data center network traffic is growing quickly [7], [13]. As much of this traffic is *internal* to the data center (e.g.,

However, only little is known today about the *algorithmic* challenge of designing demand-aware networks which provide low congestion *and* short routes (in the number of hops), for

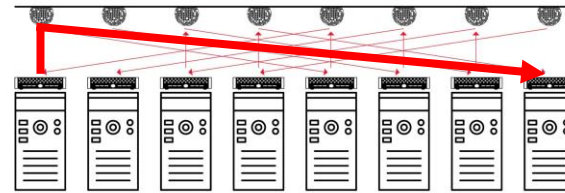
# It is more complicated..

- Self-adjusting networks may be really useful to serve large flows (**elephant flows**): avoiding multi-hop routing



6 hops

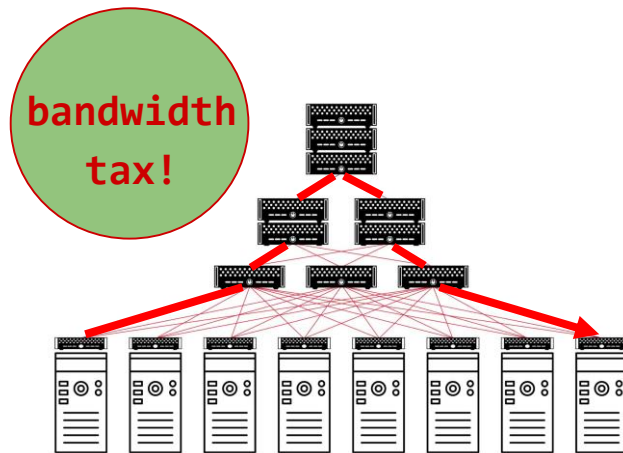
VS



1 hop

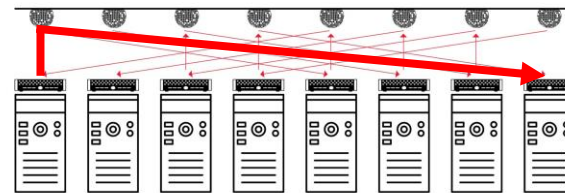
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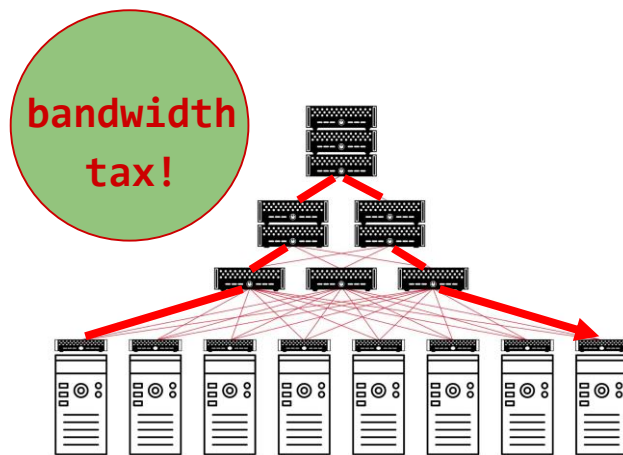
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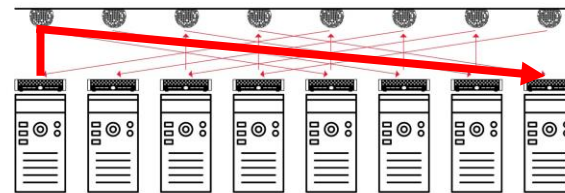
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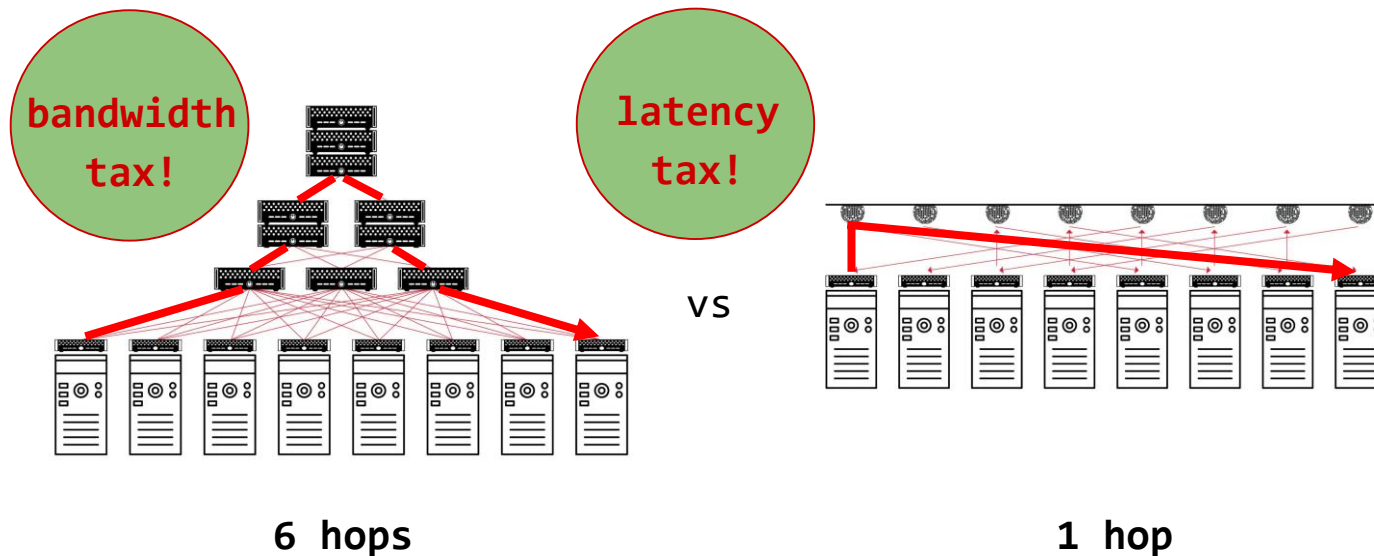


1 hop

- However, requires optimization and adaption, which **takes time**

# It is more complicated..

- Self-adjusting networks may be really useful to serve large flows (**elephant flows**): avoiding multi-hop routing



- However, requires optimization and adaption, which **takes time**

Indeed, it is more complicated than that...

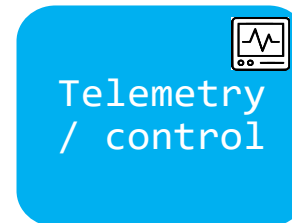
# Challenge: Traffic Diversity

## Diverse patterns:

- Shuffling/Hadoop:  
**all-to-all**
- All-reduce/ML: **ring** or **tree** traffic patterns
  - **Elephant** flows
- Query traffic: skewed
  - **Mice** flows
- Control traffic: does not evolve  
but has non-temporal structure

## Diverse requirements:

- ML is **bandwidth** hungry,  
small flows are **latency**-sensitive



# Opportunity: Tech Diversity

Diverse topology components:

→ demand-oblivious and  
demand-aware

Demand-  
oblivious



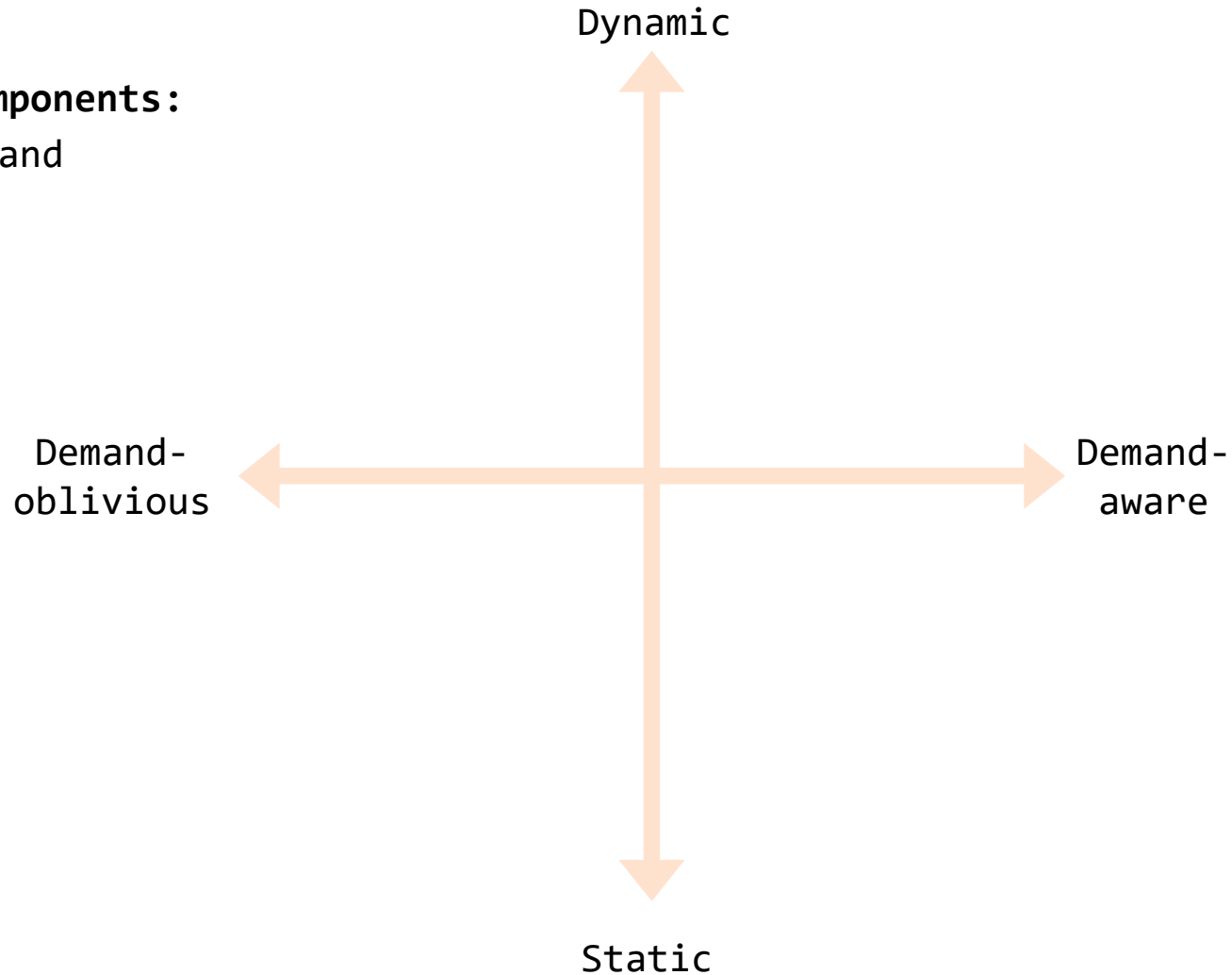
Demand-  
aware



# Opportunity: Tech Diversity

Diverse topology components:

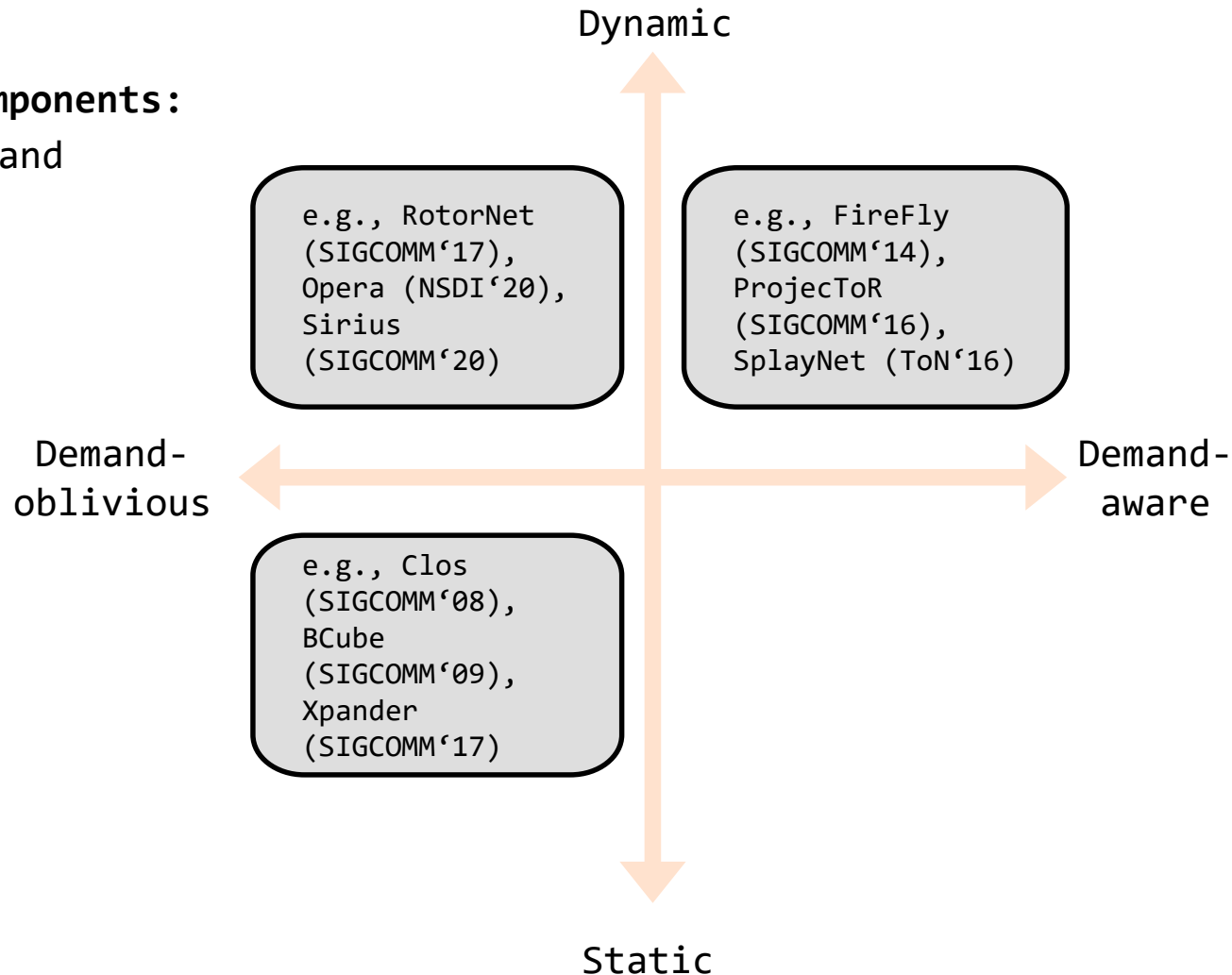
- demand-**oblivious** and demand-**aware**
- static vs dynamic



# Opportunity: Tech Diversity

Diverse topology components:

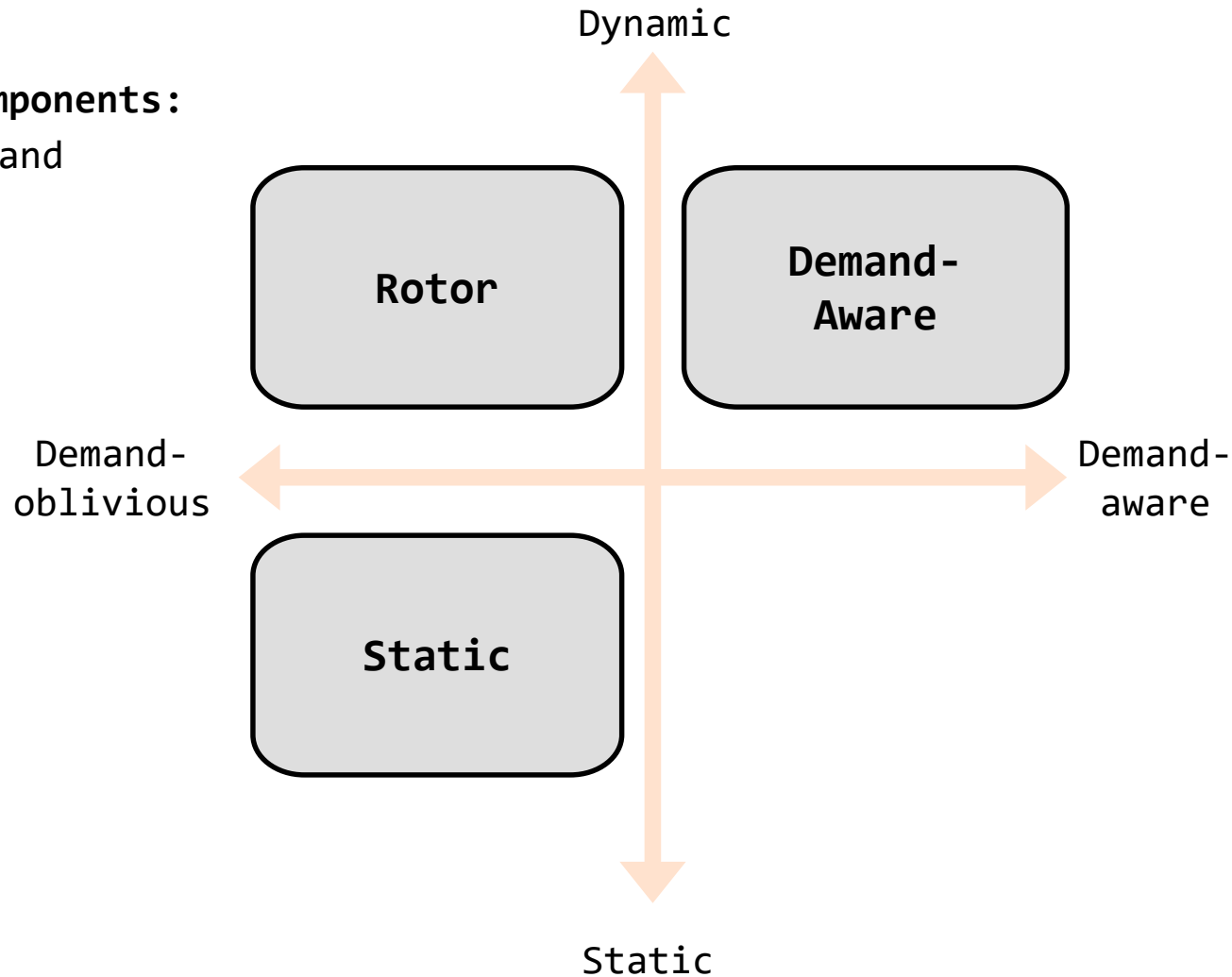
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# Opportunity: Tech Diversity

Diverse topology components:

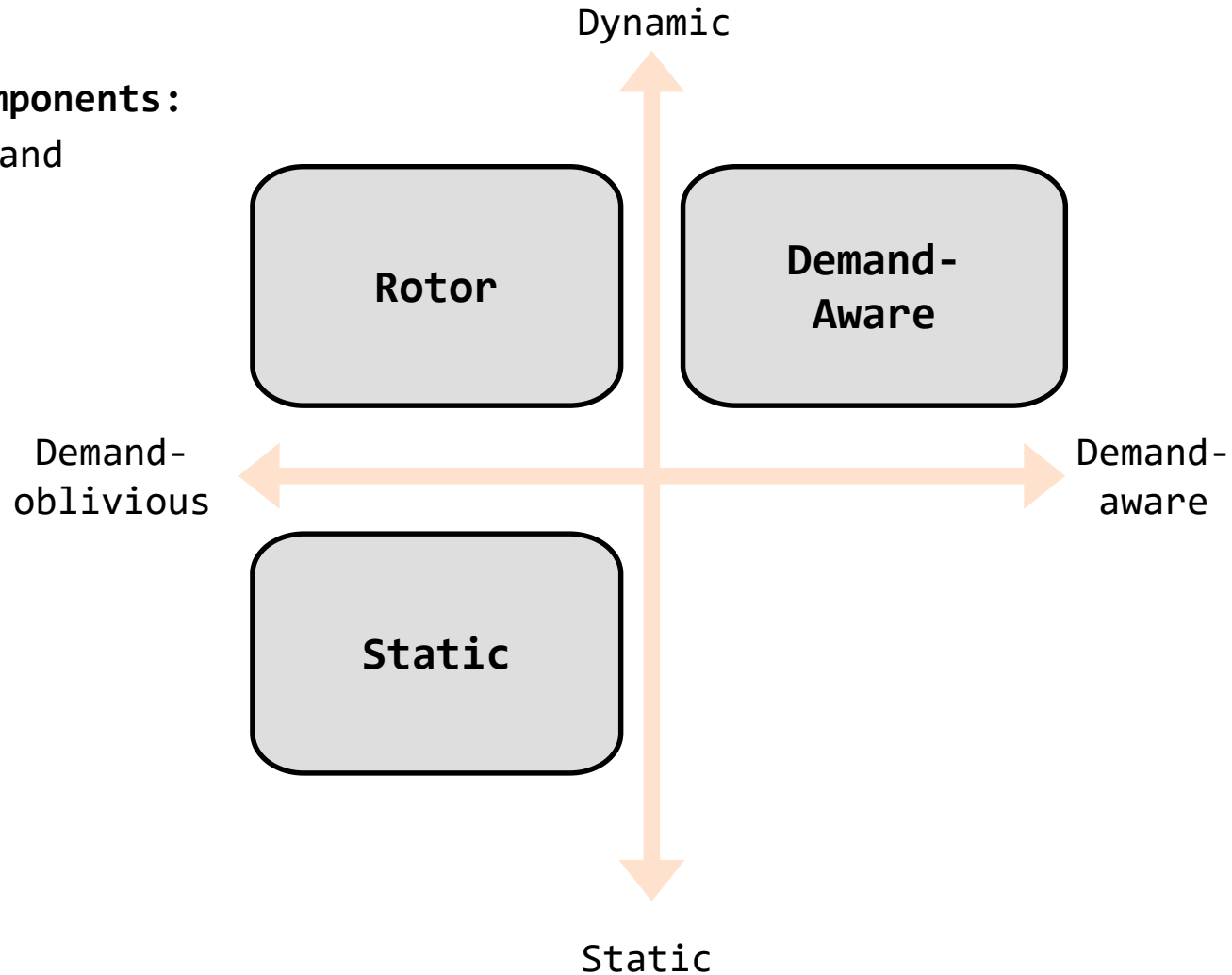
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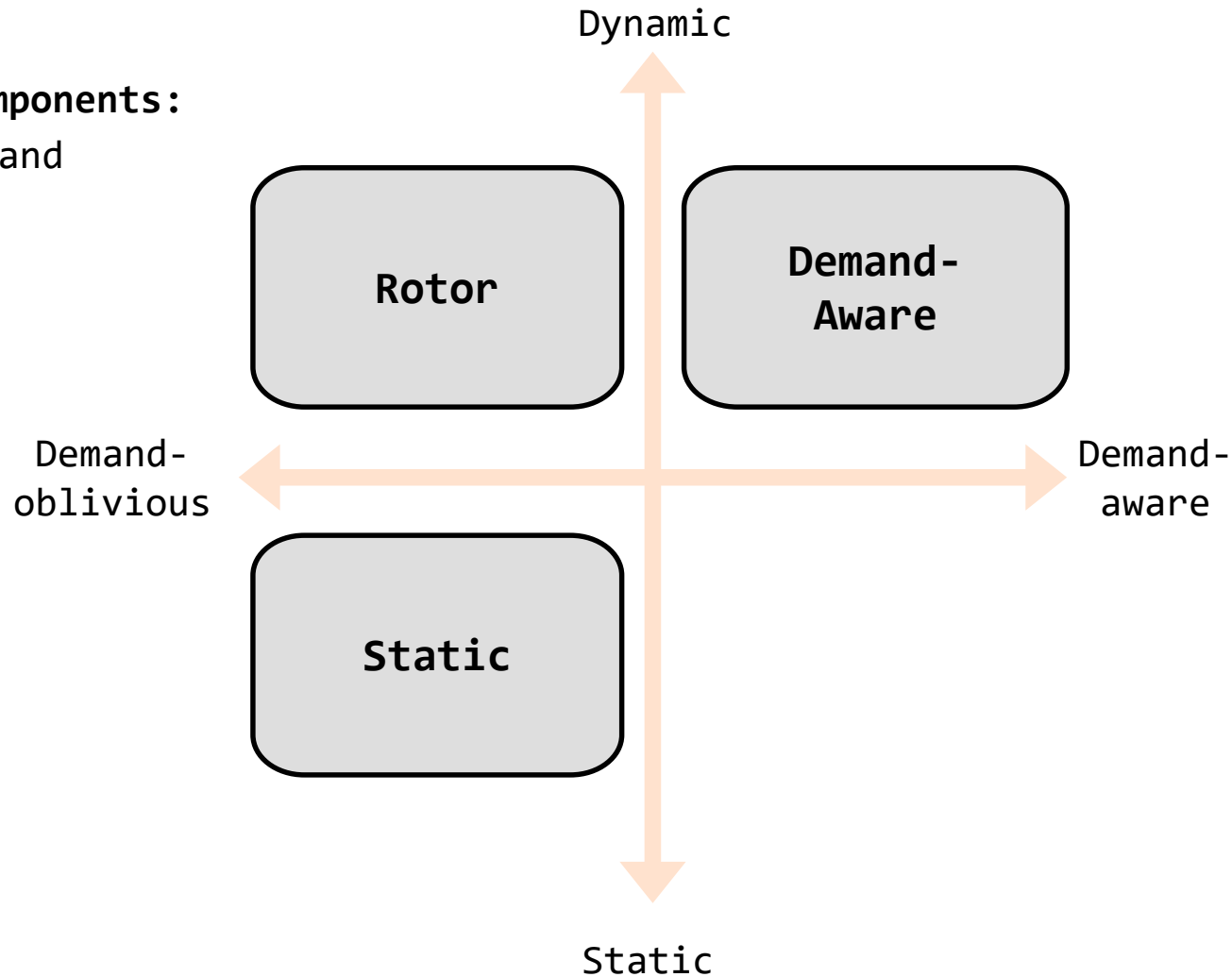


Which approach  
is best?

# Opportunity: Tech Diversity

Diverse topology components:

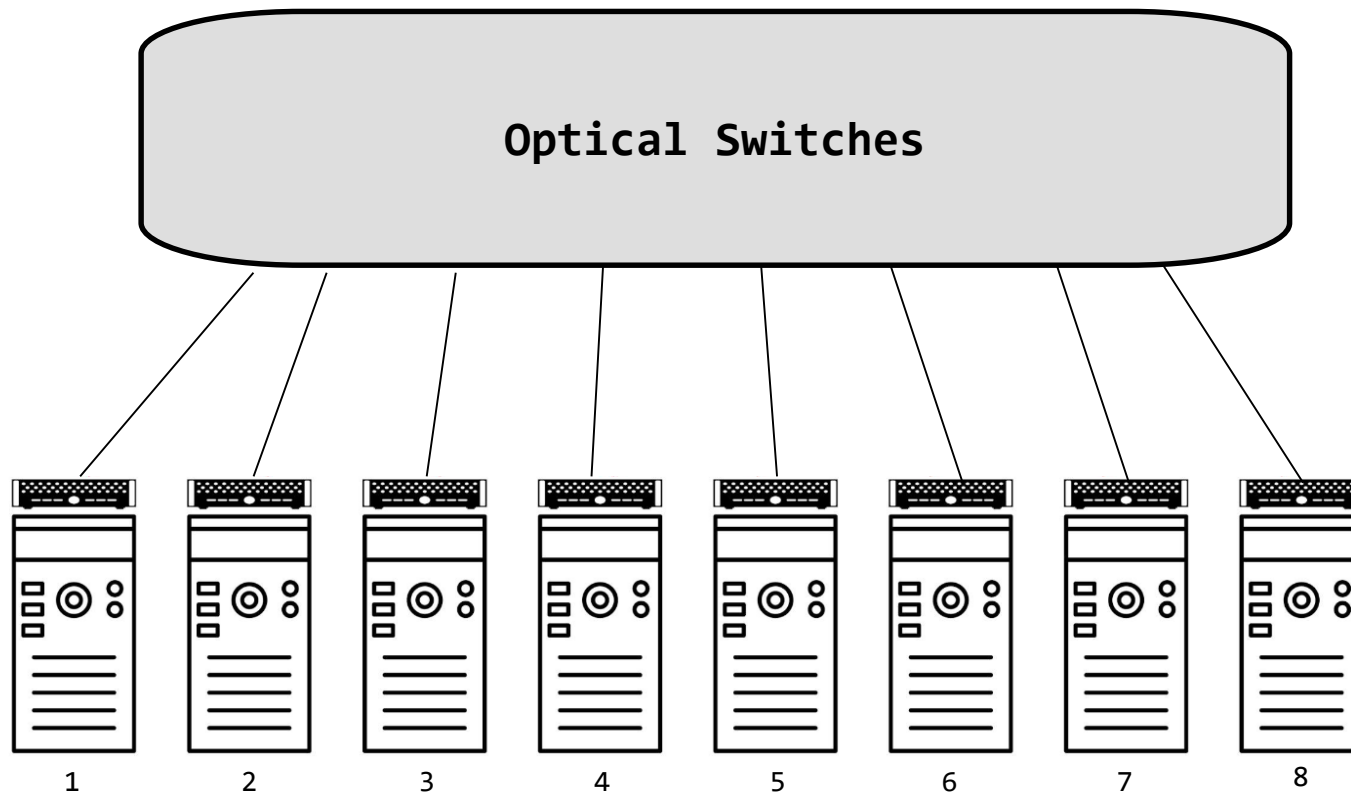
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- static vs dynamic



Which approach  
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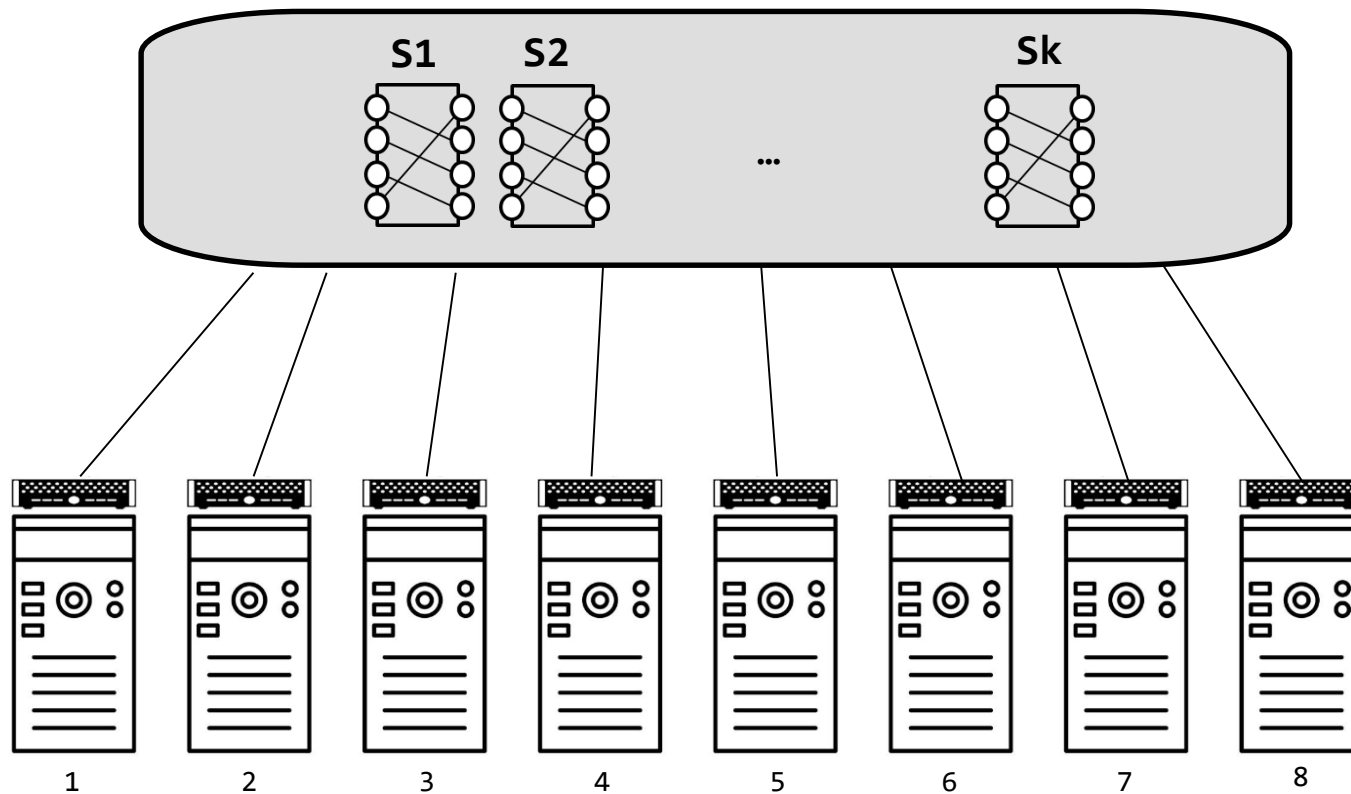
As always in CS:  
It depends...

# Rack Interconnect



Typical rack internconnect: **ToR-Matching-ToR (TMT)** model

# Rack Interconnect

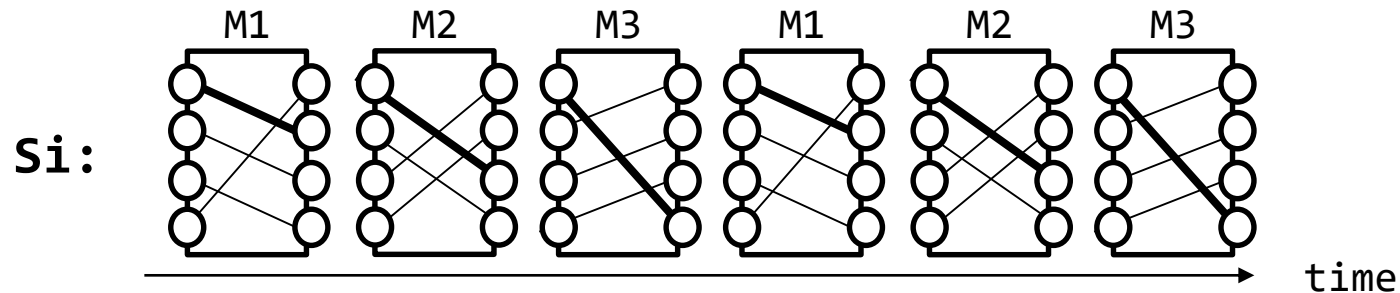


Typical rack interconnect: **ToR-Matching-ToR (TMT)** model

# Details: Switch Types

Periodic Switch (aka Rotor Switch)

Rotor switch: **periodic** matchings (demand-oblivious)

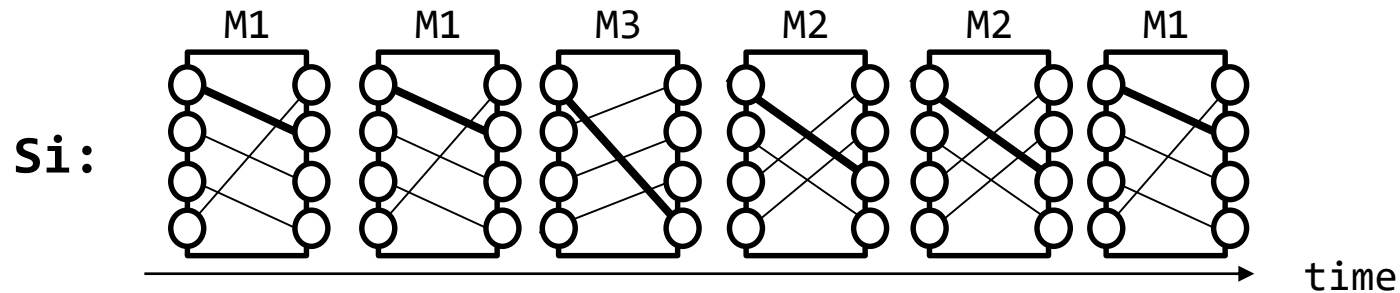




# Details: Switch Types

## Demand-Aware Switch

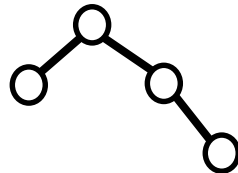
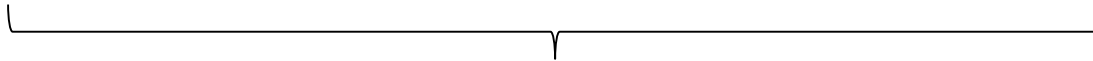
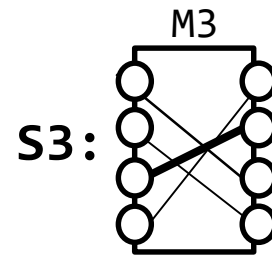
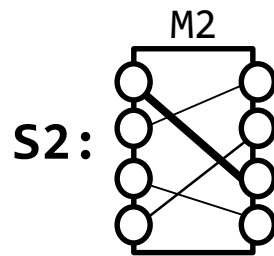
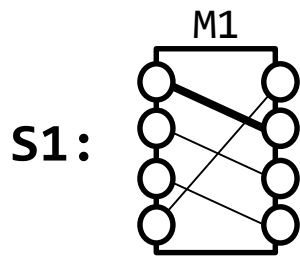
Demand-aware switch: **optimized** matchings



# Details: Switch Types

## Static Switch

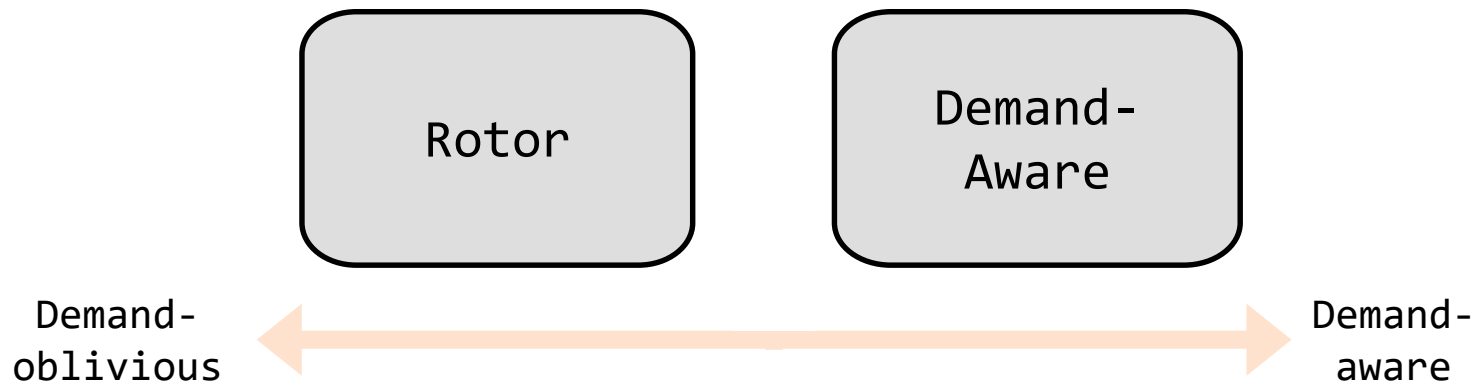
Static switches: **combine** for optimized static topology



e.g, tree, expander

# Design Tradeoffs (1)

The “Awareness-Dimension”



**Good for all-to-all traffic!**

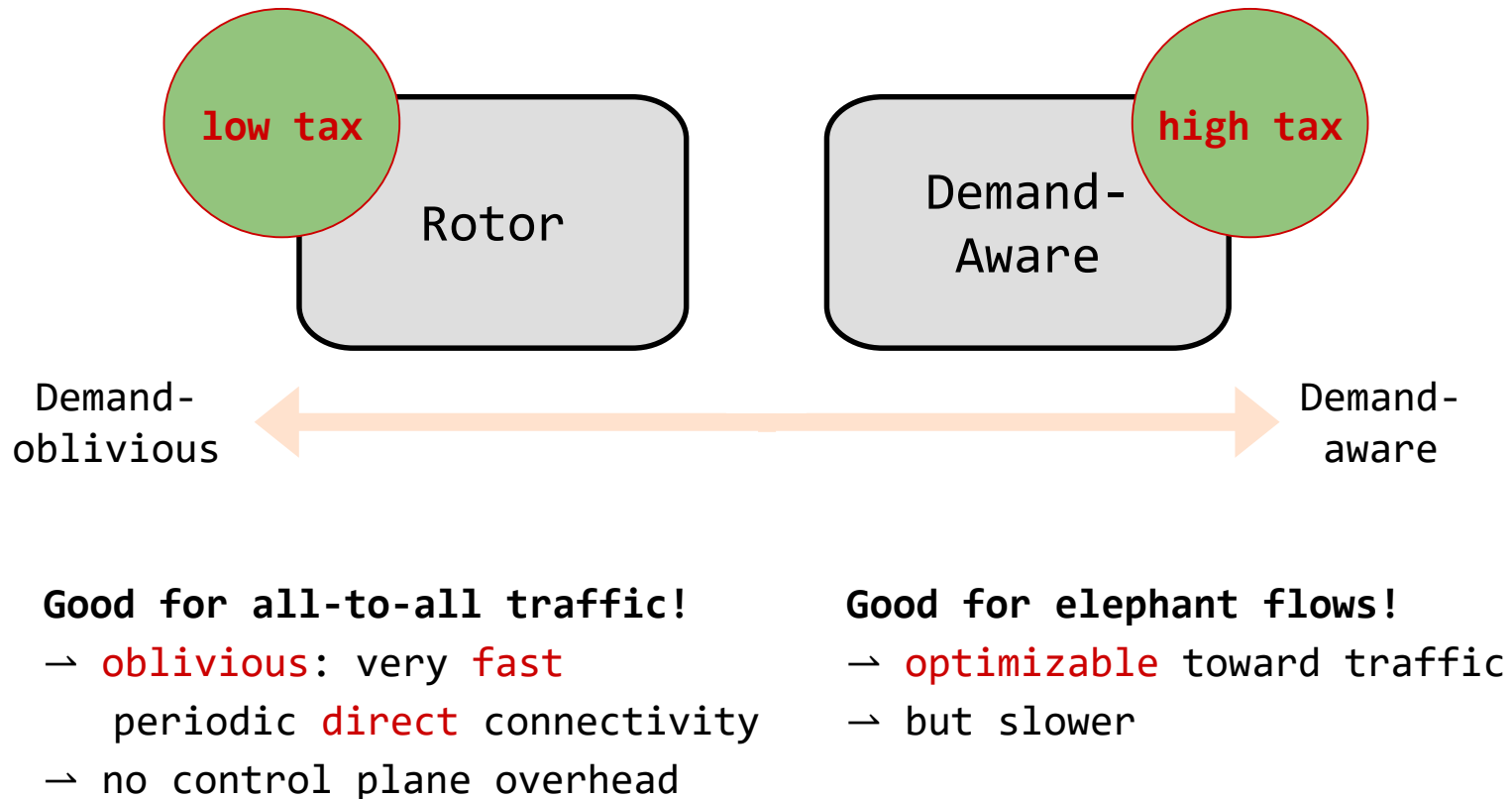
- **oblivious**: very **fast**  
periodic **direct** connectivity
- no control plane overhead

**Good for elephant flows!**

- **optimizable** toward traffic
- but slower

# Design Tradeoffs (1)

The “Awareness-Dimension”



**Compared to static networks: latency tax!**

# Design Tradeoffs (2)

## The “Flexibility-Dimension”

**Good for high throughput!**

- direct connectivity saves bandwidth along links

**Good for low latency!**

- no need to wait for reconfigurable links
- **compared to dynamic:**  
**bandwidth tax (multi-hop)**

Dynamic

**Rotor /  
Demand-  
Aware**

**Clos**

Static

# Design Tradeoffs (2)

## The “Flexibility-Dimension”

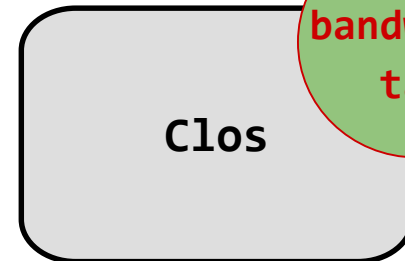
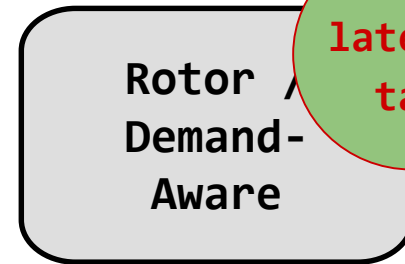
Good for high throughput!

- direct connectivity saves bandwidth along links

Good for low latency!

- no need to wait for reconfigurable links
- **compared to dynamic:**  
**bandwidth tax (multi-hop)**

Dynamic



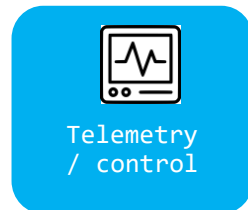
Static

# First Observations

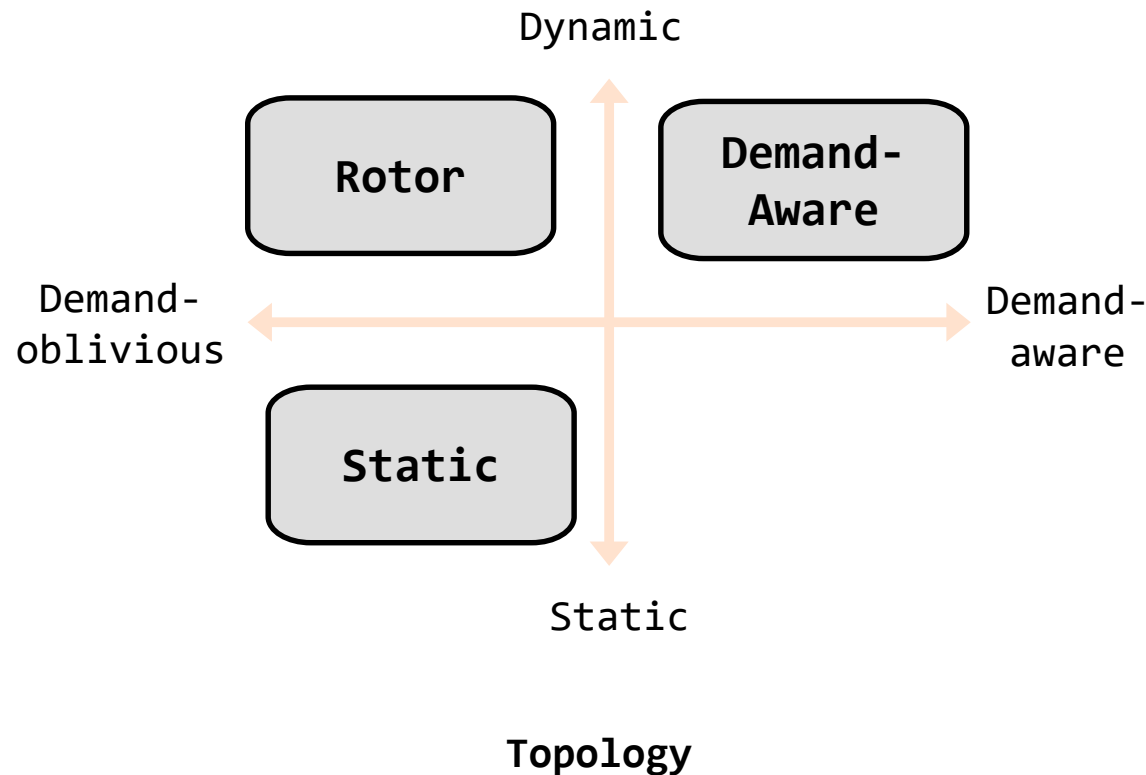
- **Observation 1:** Different topologies provide different tradeoffs.
- **Observation 2:** Different traffic requires different topology types.
- **Observation 3:** A **mismatch of demand** and topology can increase **flow completion times**.

# Examples:

## Match or Mismatch?



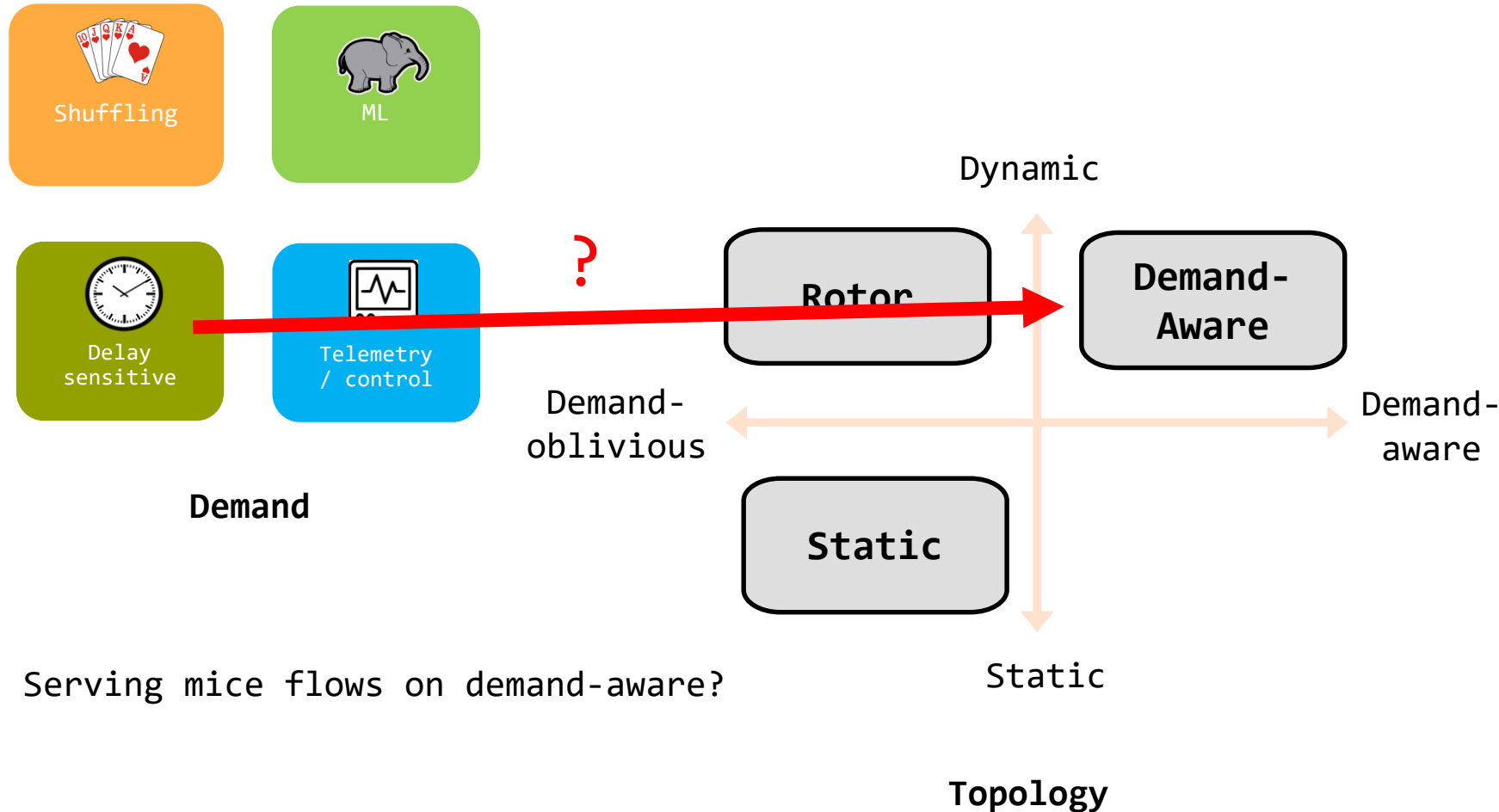
Demand





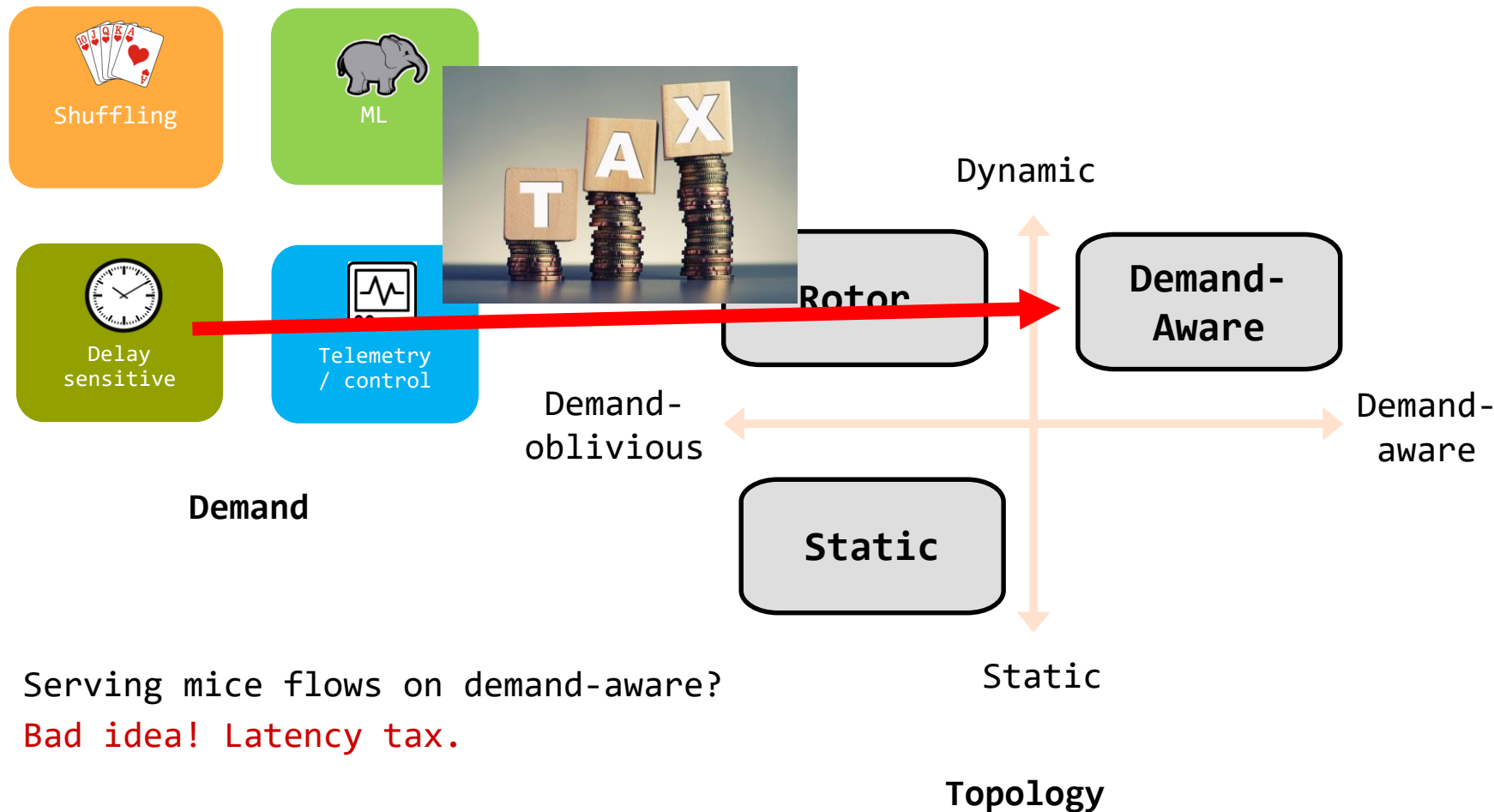
# Examples:

## Match or Mismatch?



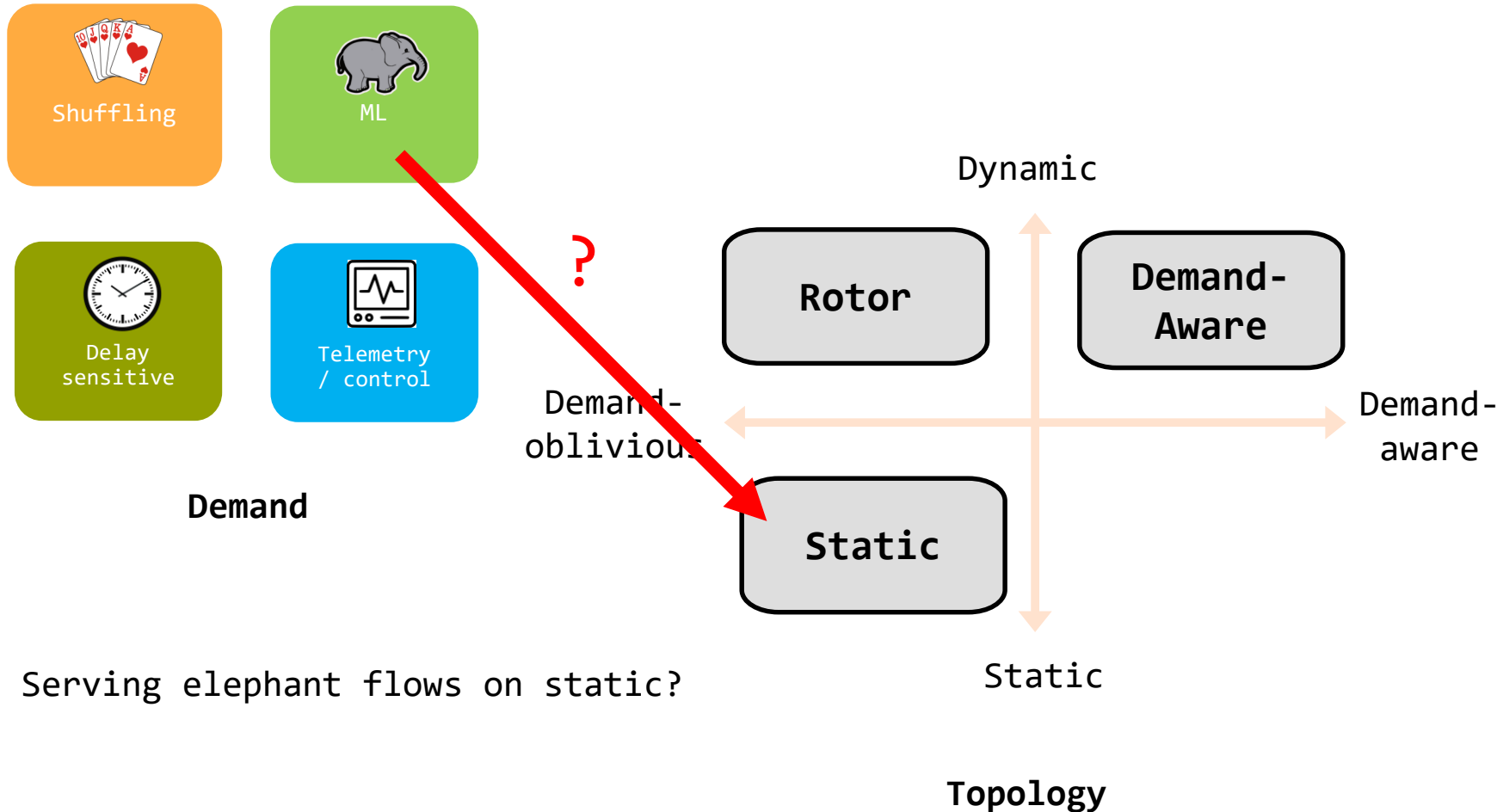
# Examples:

## Match or Mismatch?



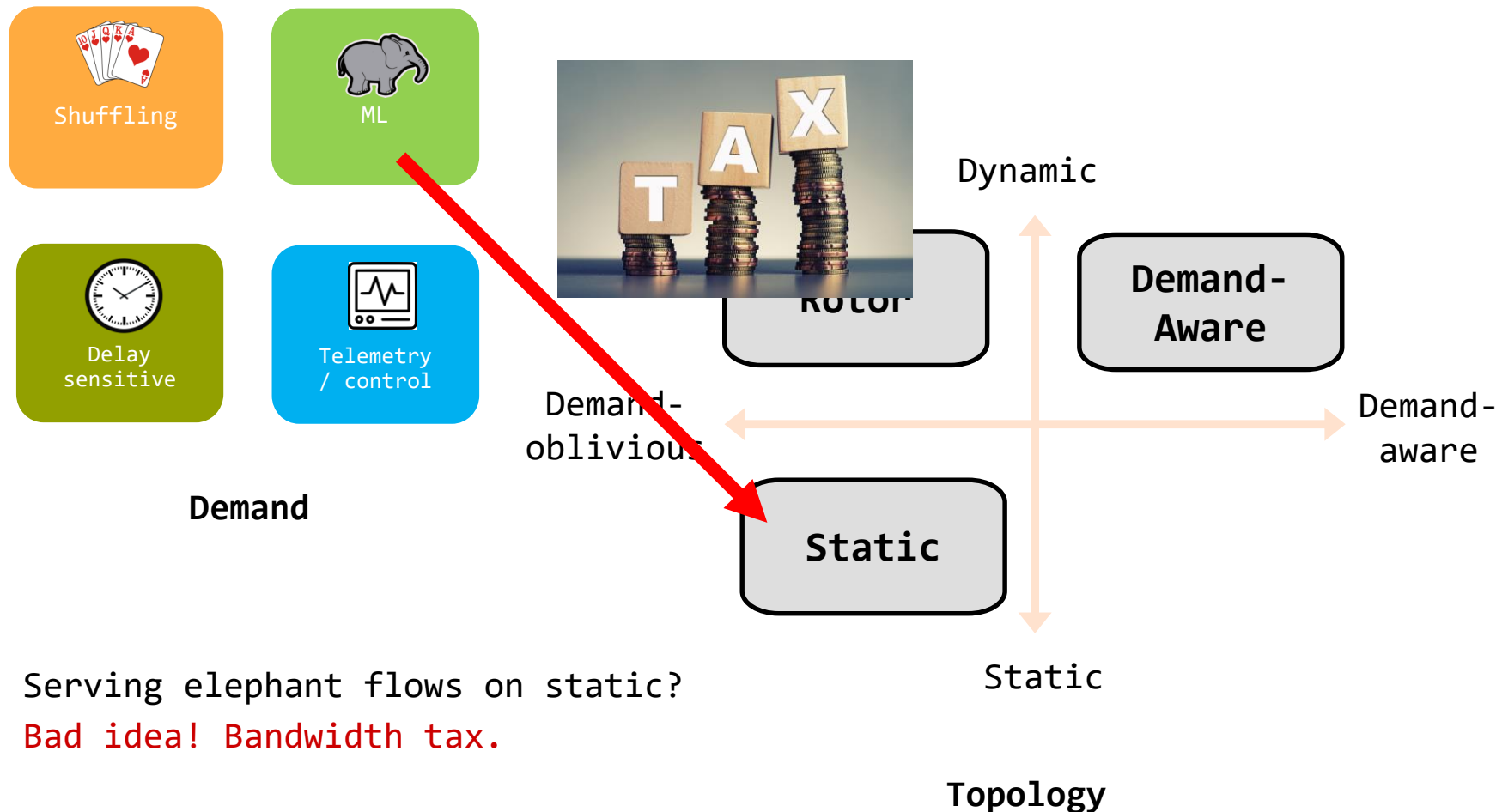
# Examples:

## Match or Mismatch?



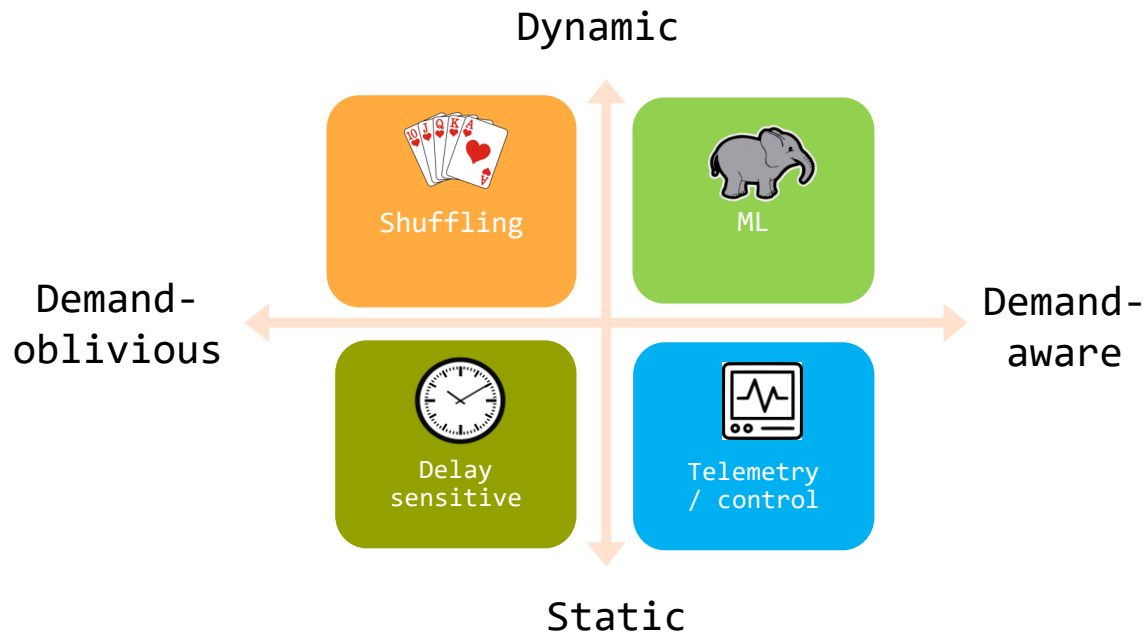
# Examples:

## Match or Mismatch?



# Cerberus:

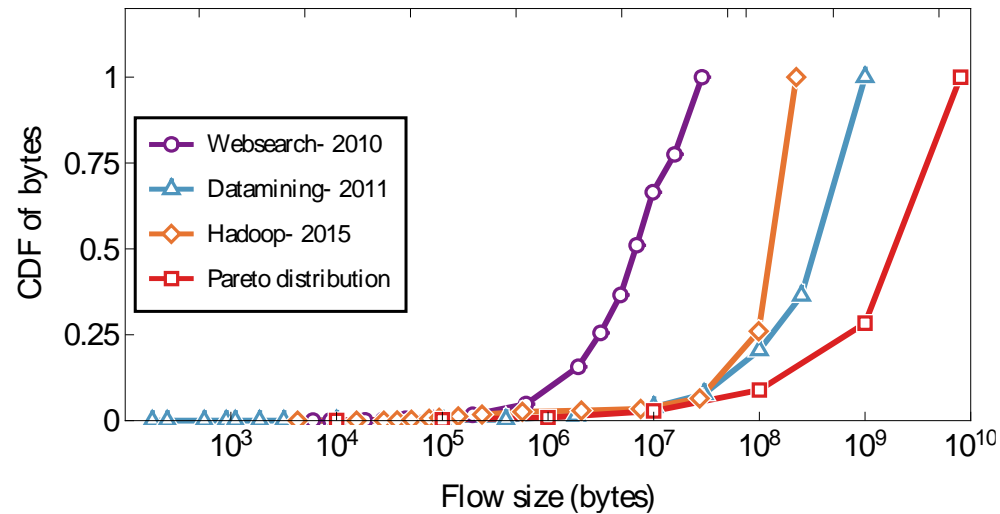
*It's a  Match!*



Our system Cerberus\* serves traffic on the “best topology”!

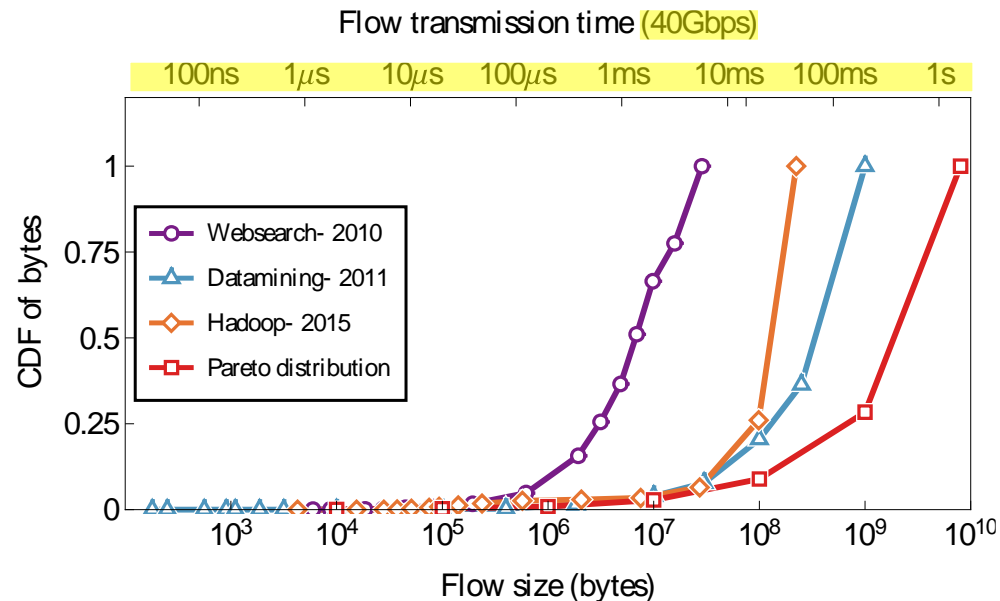
\* Griner et al., ACM SIGMETRICS 2022

# Flow Size Matters



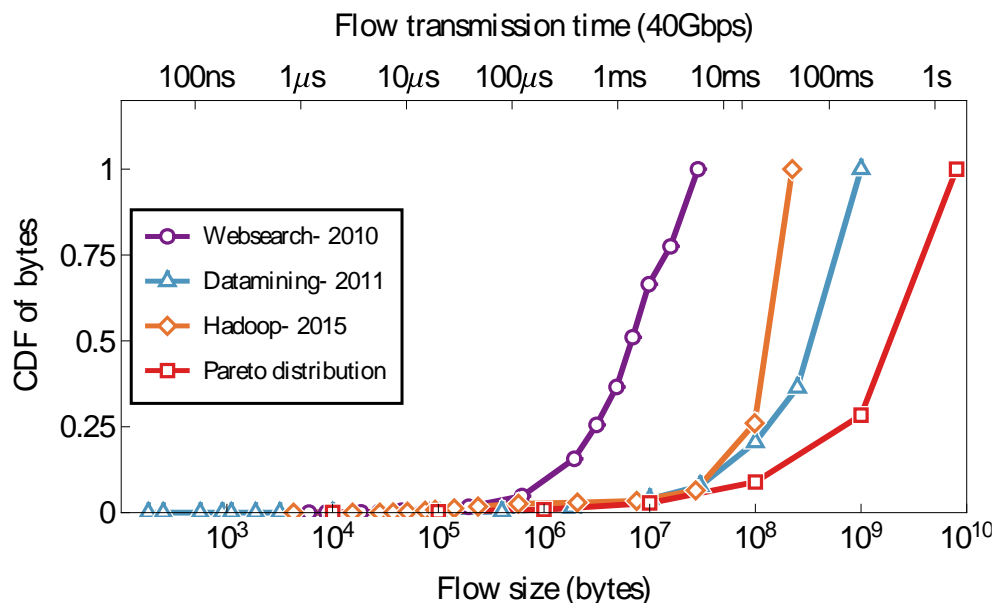
→ **Observation 1:** Different apps have different flow size distributions.

# Flow Size Matters



- **Observation 1:** Different apps have different flow size distributions.
- **Observation 2:** The transmission time of a flow depends on its size.

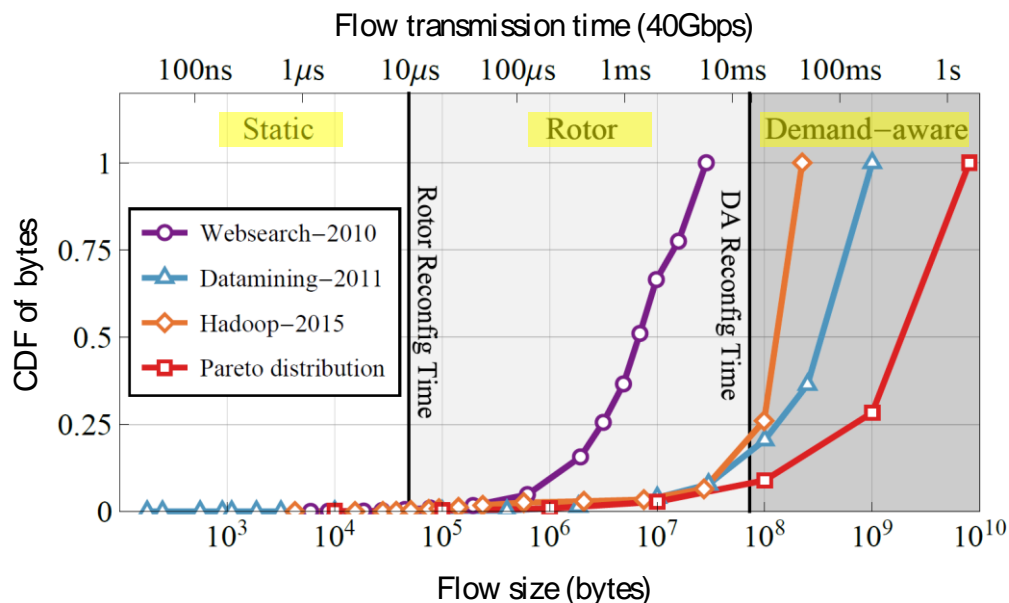
# Flow Size Matters



- **Observation 1:** Different apps have different flow size distributions.
- **Observation 2:** The transmission time of a flow depends on its size.
- **Observation 3:** For small flows, flow completion time suffers if network needs to be reconfigured first.
- **Observation 4:** For large flows, reconfiguration time may amortize.



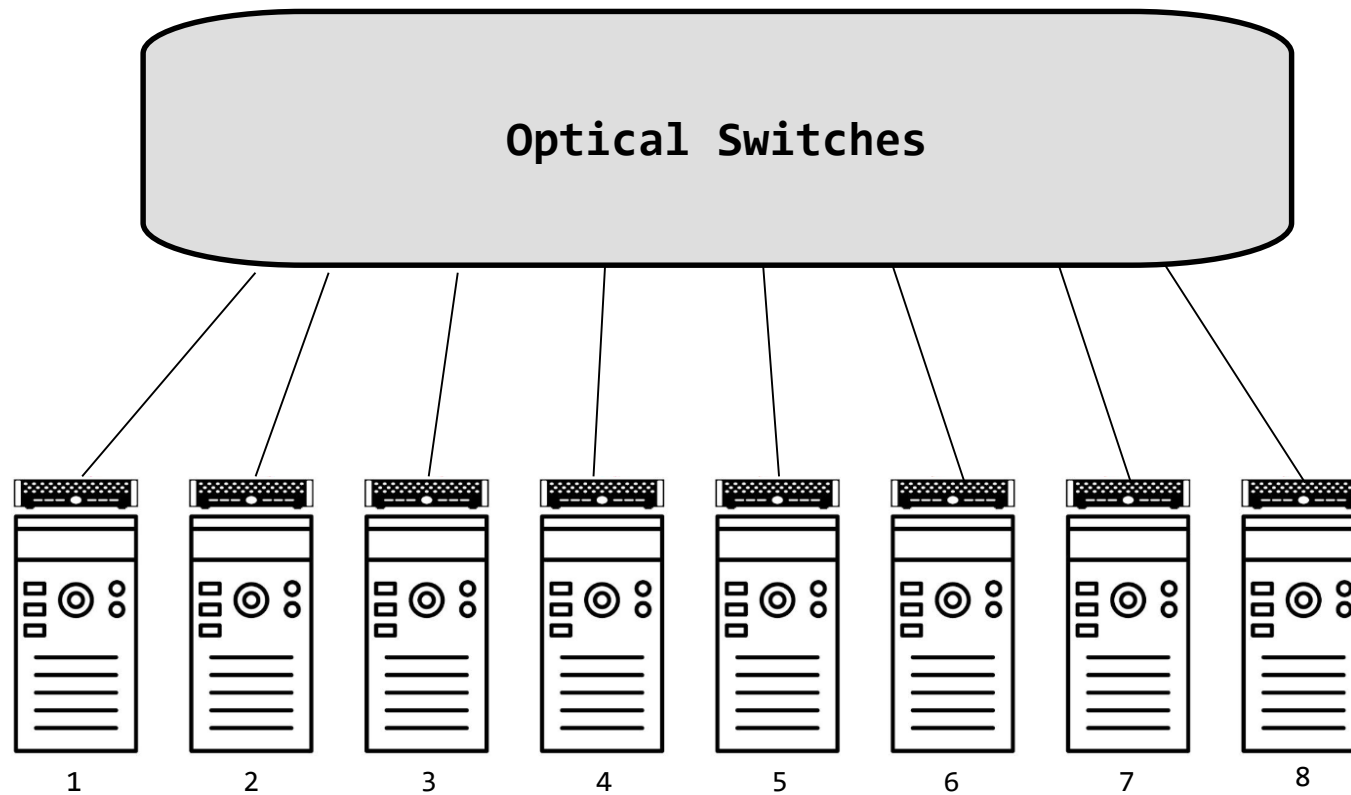
# Flow Size Matters



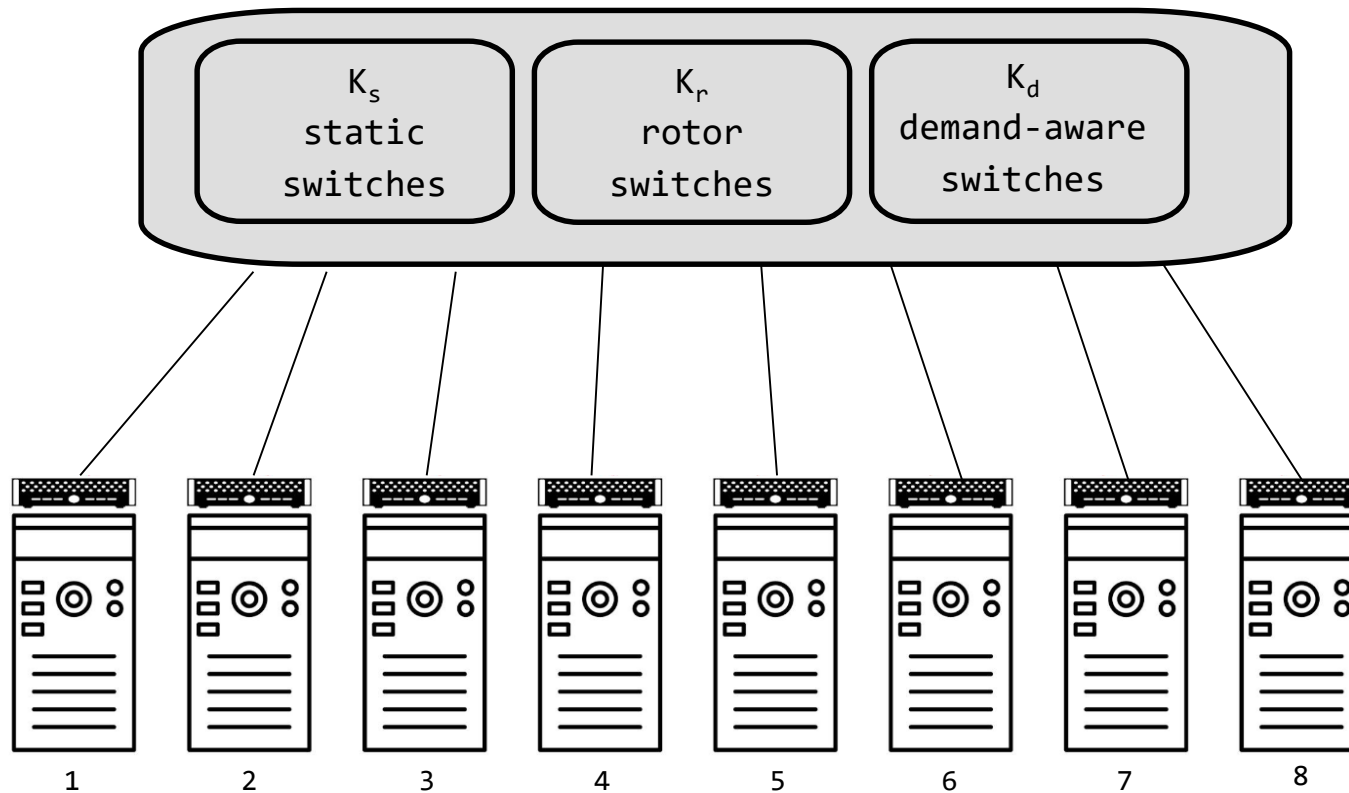
*It's a Match!*

- **Observation 1:** Different apps have different flow size distributions.
- **Observation 2:** The transmission time of a flow depends on its size.
- **Observation 3:** For small flows, flow completion time suffers if network needs to be reconfigured first.
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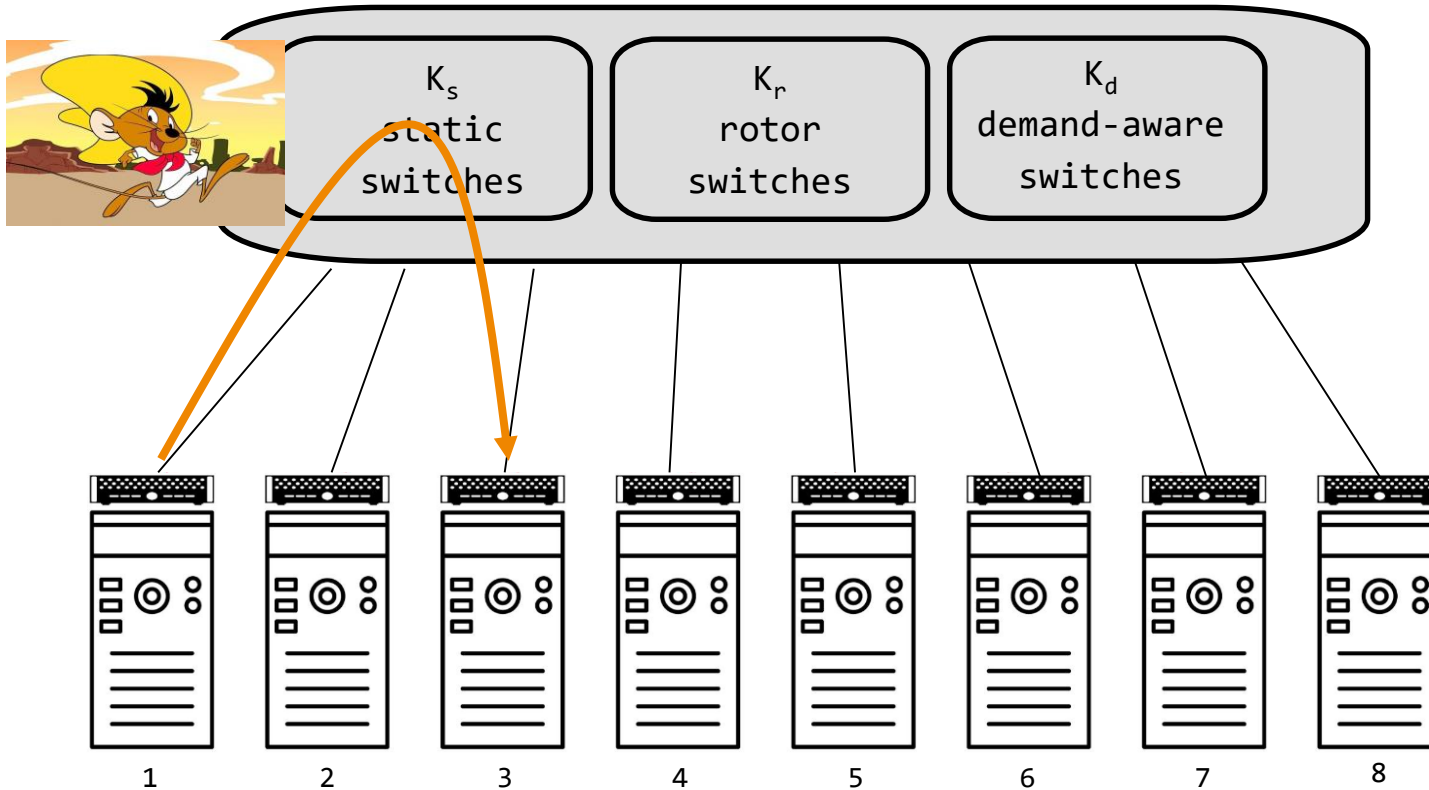
# Cerberus



# Cerberus

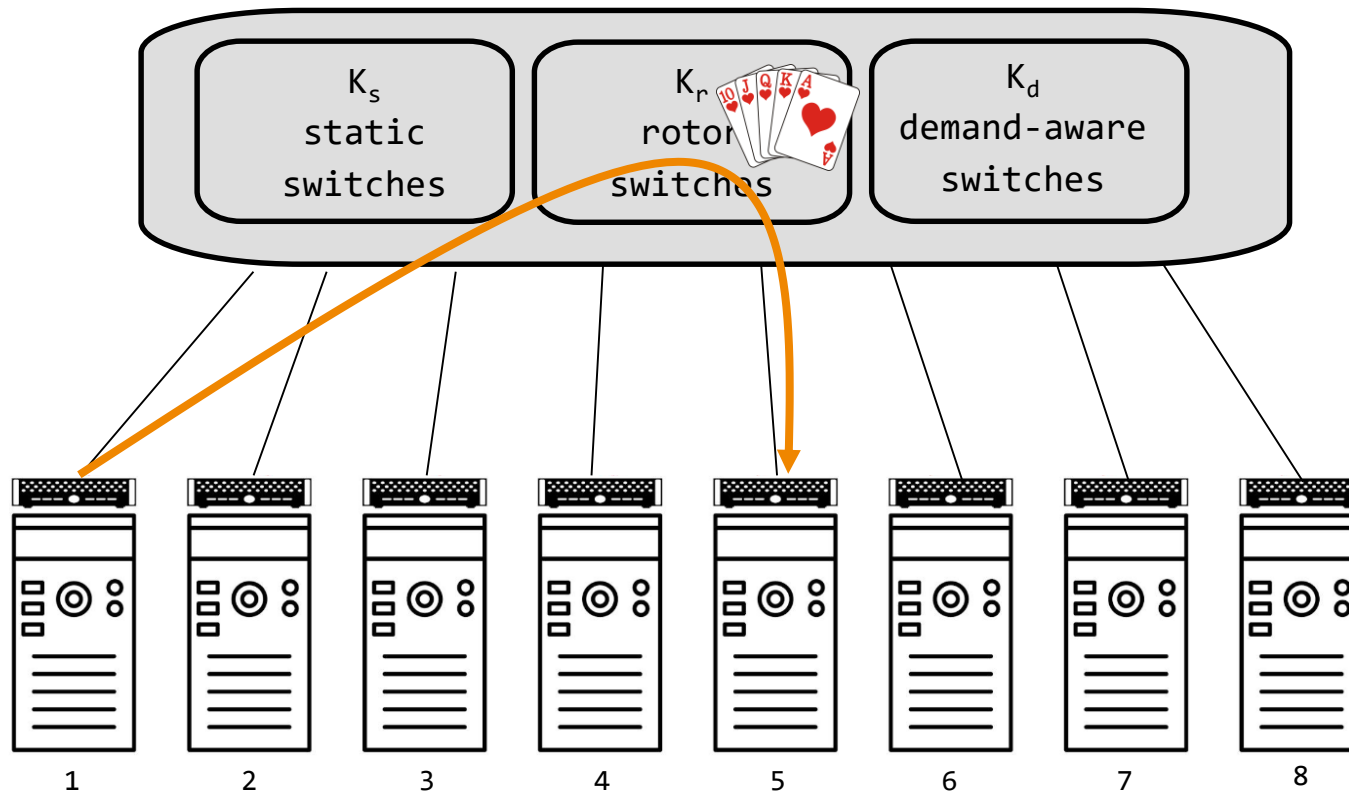


# Cerberus



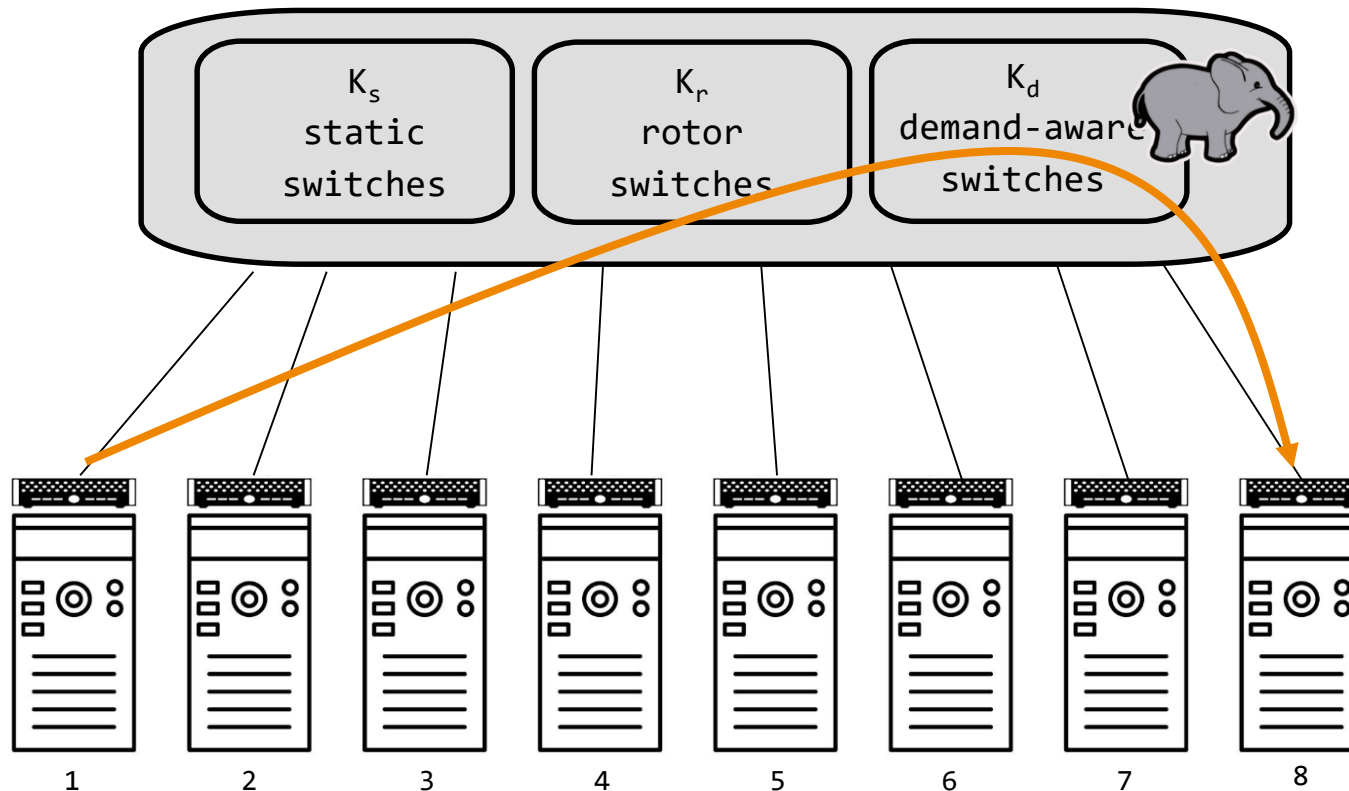
Scheduling: **Small flows** go via static switches...

# Cerberus



Scheduling: ... medium flows via rotor switches...

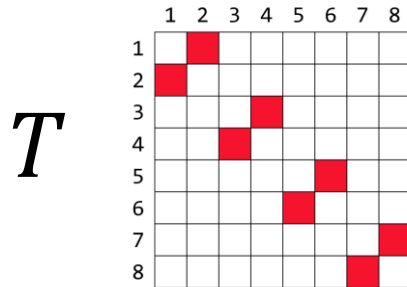
# Cerberus



**Scheduling:** ... and **large flows** via demand-aware switches  
(if one available, otherwise via rotor).

# Throughput Analysis

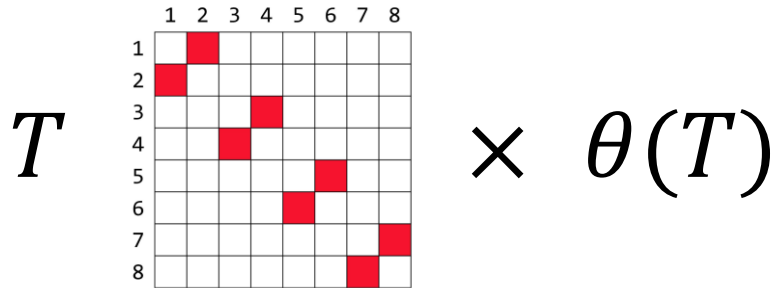
Demand Matrix



**Metric:** throughput  
of a demand matrix...

# Throughput Analysis

Demand Matrix



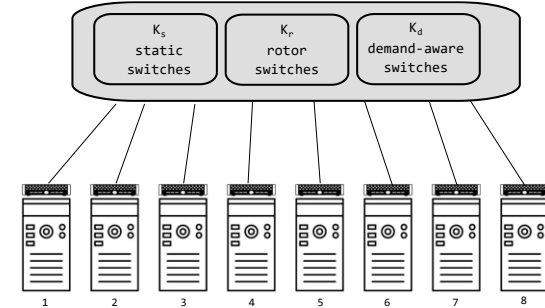
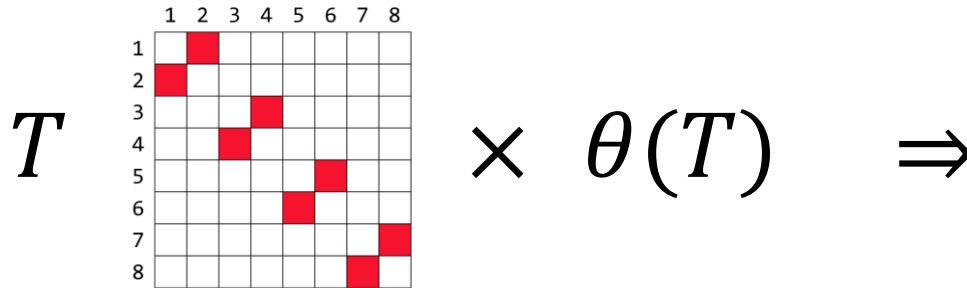
**Metric:** throughput  
of a demand matrix...

... is the maximal scale  
down **factor** by which  
traffic is **feasible**.



# Throughput Analysis

Demand Matrix



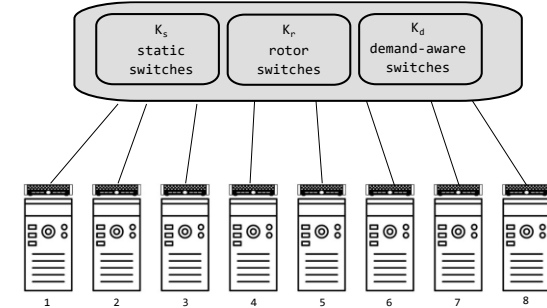
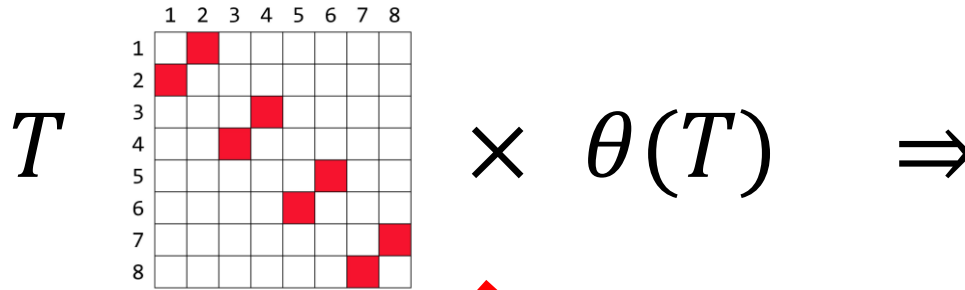
**Metric:** throughput  
of a demand matrix...

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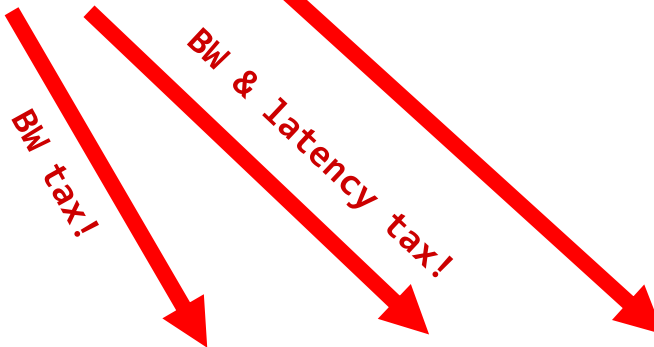
Throughput of network  $\theta^*$ :  
**worst case**  $T$

# Throughput Analysis

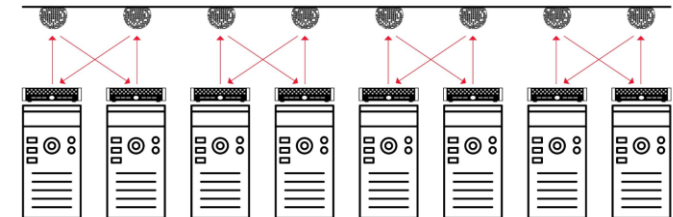
Demand Matrix



**Worst** demand matrix for static and rotor: **permutation**. Best case for demand-aware!

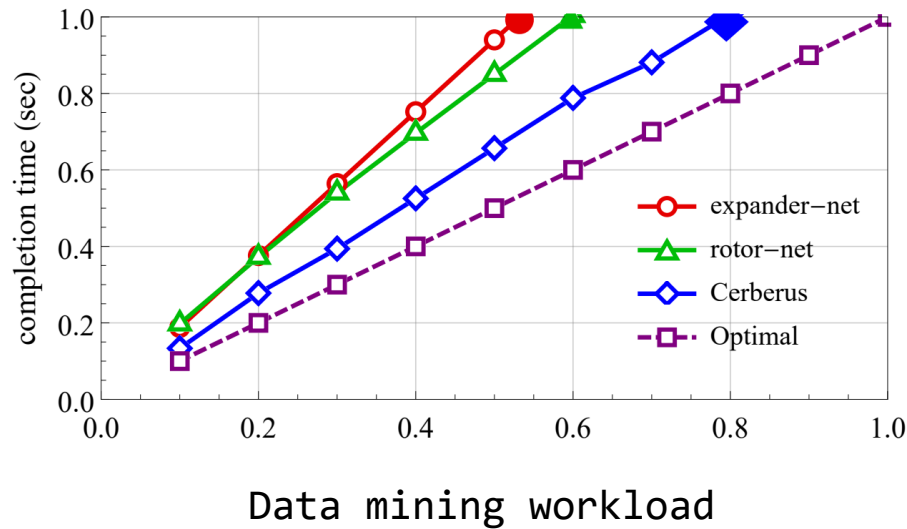


	<i>expander-net</i>	<i>rotor-net</i>	CERBERUS
BW-Tax	✓	✓	✗
LT-Tax	✗	✓	✓
$\theta(T)$	Thm 2	Thm 3	Thm 5
$\theta^*$	0.53	0.45	Open
Datamining	0.53	0.6	0.8 (+33%)
Permutation	0.53	0.45	$\approx 1$ (+88%)
Case Study	0.53	0.66	0.9 (+36%)



# Completion Time

→ Demand completion time: How long does it take to serve a demand matrix?



→ Also useful in analysis: throughput can be computed more easily via demand completion time.

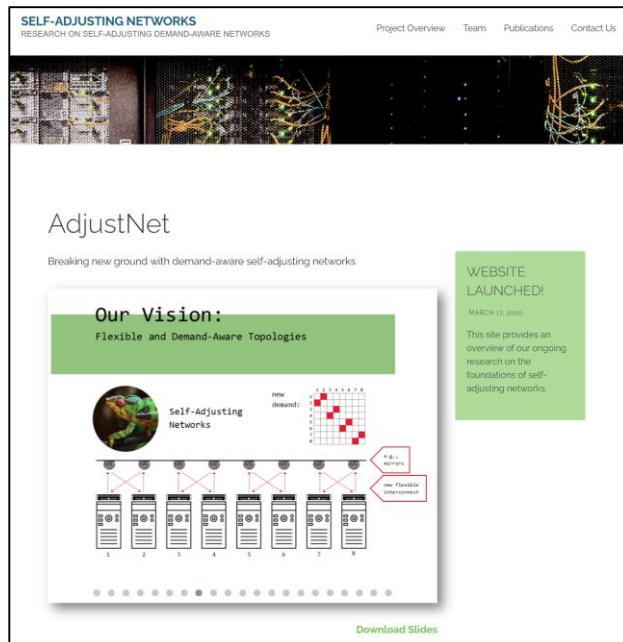
# Conclusion

- Diverse traffic requires diverse technologies
- Cerberus aims to assign traffic to its best topology
  - Depending on flow size
- Many challenges
  - Impact on routing and congestion control
  - Sensitivity analysis
  - Prototyping

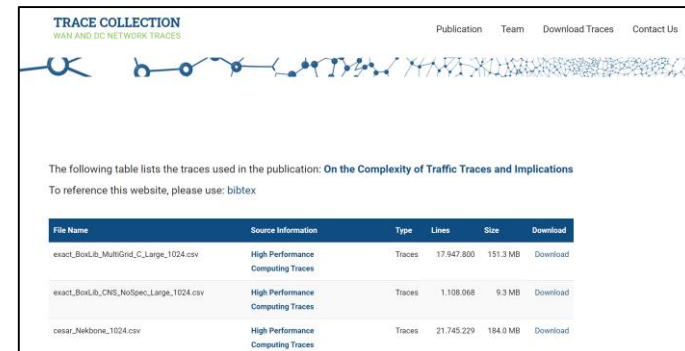


Thank you!

# Websites



<http://self-adjusting.net/>  
Project website



<https://trace-collection.net/>  
Trace collection website

# Further Reading

## Static DAN

### Demand-Aware Network Designs of Bounded Degree

Chen Avin<sup>1</sup> Kaushik Mondal<sup>2</sup> Stefan Schmid<sup>2</sup>

**Abstract** Traditionally, networks such as datacenter interconnects are designed to optimize worst-case performance under *arbitrary* traffic patterns. Such network designs can however be far from optimal when considering the *actual* workloads and traffic patterns which they serve. This insight led to the development of demand-aware datacenter interconnects which can be reconfigured depending on the workload.

#### 1 Introduction

The problem studied in this paper is motivated by the advent of more flexible datacenter interconnects, such as Project Tor [29, 31]. These interconnects aim to overcome a fundamental drawback of traditional datacenter network designs: the fact that network designers must decide in *advance* on how much capacity to provision between electrical packet switches, e.g., between Top-of-Rack (ToR) switches in datacenters. This leads to an undesirable tradeoff [42]: either capacity is over-provisioned and therefore the interconnect expensive (e.g., a fat-tree provides full-bisection bandwidth), or one may risk congestion, resulting in a poor cloud application performance. Accordingly, systems such as Project Tor provide a reconfigurable interconnect, allowing to establish links flexibly and in a *demand-aware* manner. For example, direct links or at least short communication paths can be established between frequently communicating ToR switches. Such links can be implemented using a bounded number of lasers, mirrors,

## Robust DAN

### rDAN: Toward Robust Demand-Aware Network Designs

Chen Avin<sup>1</sup> Alexandr Hercules<sup>1</sup> Andreas Loukas<sup>2</sup> Stefan Schmid<sup>3</sup>  
<sup>1</sup> Ben-Gurion University, IL. <sup>2</sup> EPFL, CH. <sup>3</sup> University of Vienna, AT & TU Berlin, DE

#### Abstract

We currently witness the emergence of interesting new network topologies optimized towards the traffic matrices they serve, such as demand-aware datacenter interconnects (e.g., Project Tor) and demand-aware peer-to-peer overlay networks (e.g., SplayNets). This paper introduces a formal framework and approach to reason about and design robust demand-aware networks (*DAN*). In particular, we establish a connection between the communication frequency of two nodes and the path length between them in the network, and show that this relationship depends on the *entropy* of the communication matrix. Our main contribution is a novel robust, yet sparse, family of networks, short *rDANs*, which guarantee an expected path length that is proportional to the entropy of the communication patterns.

## Overview: Models

### Toward Demand-Aware Networking: A Theory for Self-Adjusting Networks

Chen Avin<sup>1</sup>  
Ben Gurion University, Israel  
avin@cse.bgu.ac.il

Stefan Schmid<sup>2</sup>  
University of Vienna, Austria  
stefan\_schmid@univie.ac.at

This article is an editorial note submitted to CCR. It has NOT been peer reviewed.  
The authors take full responsibility for this article's technical content. Comments can be posted through CCR Online.

#### ABSTRACT

The physical topology is emerging as the next frontier in an ongoing effort to render communication networks more flexible. While first empirical results indicate that these flexibility can be exploited to reconfigure and optimize the network toward the workload it serves and, e.g., providing the same bandwidth at lower infrastructure cost, only little is known today about the fundamental algorithmic problems underlying the design of reconfigurable networks. This paper initiates the study of the theory of demand-aware, self-adjusting networks. Our main position is that self-adjusting networks should be seen through the lens of self-adjusting datastructures. Accordingly, we present a taxonomy classifying the different algorithmic models of demand-oblivious, fixed demand-aware, and reconfigurable demand-aware networks, introduce a formal model, and identify objectives and evaluation metrics. We also demonstrate, by examples, the inherent



Figure 1: Taxonomy of topology optimization

design of efficient datacenter networks has received much attention over the last years. The topologies underlying modern datacenter networks range from trees [7, 8] over hypercubes [9, 10] to expander networks [11] and provide high connectivity at low cost [1].

Until now, these networks also have in common that their topology is *fixed* and *oblivious* to the actual demand (i.e.,

## Dynamic DAN

### SplayNet: Towards Locally Self-Adjusting Networks

Stefan Schmid\*, Chen Avin\*, Christian Scheidegger, Michael Borokhovich, Bernhard Haeupler, Zvi Lotker

**Abstract**—This paper initiates the study of locally self-adjusting networks: networks whose topology adapts dynamically and in a decentralized manner, to the communication pattern  $\sigma$ . Our vision can be seen as a distributed generalization of the self-adjusting datastructures introduced by Sleator and Tarjan [22]: In contrast to their splay trees which dynamically optimize the lookup costs from a *single node* (namely the tree root), we seek to minimize the routing cost between *arbitrary communication pairs* in the network. As a first step, we study distributed binary search trees (BSTs), which are attractive for their support of greedy routing. We introduce a simple model which captures the fundamental tradeoff between the benefits and costs of self-adjusting networks. We present the *SplayNet* algorithm and formally analyze its performance, and prove its optimality in specific case studies. We also introduce lower bound techniques based on interval cuts and edge expansion, to study the limitations of any demand-optimized network. Finally, we extend our study to multi-tree networks, and highlight an intriguing difference between classic and distributed splay trees.

#### 1. INTRODUCTION

In the 1980s, Sleator and Tarjan [22] proposed an appealing new paradigm to design efficient Binary Search Tree (BST) datastructures: rather than optimizing traditional metrics such

toward static metrics, such as the diameter or the length of the longest route: the self-adjusting paradigm has not spilled over to distributed networks yet.

We, in this paper, initiate the study of a distributed generalization of self-optimizing datastructures. This is a non-trivial generalization of the classic splay tree concept: While in classic BSTs, a *lookup request* always originates from the same node, the tree root, distributed datastructures and networks such as skip graphs [2], [13] have to support *routing requests* between arbitrary pairs (or *peers*) of communicating nodes; in other words, both the source as well as the destination of the requests become variable. Figure 1 illustrates the difference between classic and distributed binary search trees.

In this paper, we ask: Can we reap similar benefits from self-adjusting *entire networks*, by adaptively reducing the distance between frequently communicating nodes?

As a first step, we explore fully decentralized and self-adjusting Binary Search Tree networks: in these networks, nodes are arranged in a binary tree which respects node identifiers. A BST topology is attractive as it supports greedy routing: a node can decide locally to which port to forward a request given its destination address.

## Static Optimality

### ReNets: Toward Statically Optimal Self-Adjusting Networks

Chen Avin<sup>1</sup> Stefan Schmid<sup>2</sup>  
<sup>1</sup> Ben Gurion University, Israel <sup>2</sup> University of Vienna, Austria

#### Abstract

This paper studies the design of *self-adjusting* networks whose topology dynamically adapts to the workload, in an *online* and *demand-aware* manner. This problem is motivated by emerging optical technologies which allow to reconfigure the datacenter topology at runtime. Our main contribution is *ReNet*, a self-adjusting network which maintains a balance between the benefits and costs of reconfigurations. In particular, we show that *ReNets* are *statically optimal* for arbitrary sparse communication demands, i.e., perform at least as good as any fixed demand-aware network designed with a perfect knowledge of the future demand. Furthermore, *ReNets* provide *compact* and *local* routing, by leveraging ideas from self-adjusting datastructures.

#### 1 Introduction

Modern datacenter networks rely on efficient network topologies (based on fat-trees [1], hypercubes [2, 3], or expander [4] graphs) to provide a high connectivity at low cost [5]. These datacenter networks have in common that their topology is *fixed* and *oblivious* to the actual demand (i.e., workload or communication pattern) they currently serve. Rather, they are designed for all-to-all communication patterns, by ensuring properties such as full bisection bandwidth or  $O(\log n)$  route lengths between *any* node pair in a constant-degree  $n$ -node network. However, demand-oblivious networks can be inefficient for more *specific* demand patterns, as they usually arise in *workloads*. *ReNets* address this issue and aim to provide a *statically optimal* solution.

## Concurrent DANs

### CBNet: Minimizing Adjustments in Concurrent Demand-Aware Tree Networks

Osário Augusto de Oliveira Souza<sup>1</sup> Olga Goussevskaia<sup>2</sup> Stefan Schmid<sup>2</sup>  
<sup>1</sup> Universidade Federal de Minas Gerais, Brazil <sup>2</sup> University of Vienna, Austria

**Abstract**—This paper studies the design of demand-aware network topologies: networks that dynamically adapt themselves toward the demand they currently serve, in an *online* manner. While demand-aware networks may be significantly more efficient than demand-oblivious networks, frequent adjustments are still costly. Furthermore, a centralized controller of such networks may become a bottleneck.

CBNet is based on concepts from self-adjusting data structures, and in particular, CBTrees [12]. CBNet gradually adapts the network topology toward the communication pattern in an *online* manner, i.e., without previous knowledge of the demand distribution. At the same time, *bidirectional semi-splaying* and *counters* are used to maintain state, minimize reconfiguration

# Selected References

## **On the Complexity of Traffic Traces and Implications**

Chen Avin, Manya Ghobadi, Chen Griner, and Stefan Schmid.  
ACM SIGMETRICS, Boston, Massachusetts, USA, June 2020.

## **Survey of Reconfigurable Data Center Networks: Enablers, Algorithms, Complexity**

Klaus-Tycho Foerster and Stefan Schmid.  
*SIGACT News*, June 2019.

## **Toward Demand-Aware Networking: A Theory for Self-Adjusting Networks (Editorial)**

Chen Avin and Stefan Schmid.  
ACM SIGCOMM Computer Communication Review (CCR), October 2018.

## **Dynamically Optimal Self-Adjusting Single-Source Tree Networks**

Chen Avin, Kaushik Mondal, and Stefan Schmid.  
14th Latin American Theoretical Informatics Symposium (LATIN), University of Sao Paulo, Sao Paulo, Brazil, May 2020.

## **Demand-Aware Network Design with Minimal Congestion and Route Lengths**

Chen Avin, Kaushik Mondal, and Stefan Schmid.  
38th IEEE Conference on Computer Communications (INFOCOM), Paris, France, April 2019.

## **Distributed Self-Adjusting Tree Networks**

Bruna Peres, Otavio Augusto de Oliveira Souza, Olga Goussevskaia, Chen Avin, and Stefan Schmid.  
38th IEEE Conference on Computer Communications (INFOCOM), Paris, France, April 2019.

## **Efficient Non-Segregated Routing for Reconfigurable Demand-Aware Networks**

Thomas Fenz, Klaus-Tycho Foerster, Stefan Schmid, and Anaïs Villedieu.  
*IFIP Networking*, Warsaw, Poland, May 2019.

## **DaRTree: Deadline-Aware Multicast Transfers in Reconfigurable Wide-Area Networks**

Long Luo, Klaus-Tycho Foerster, Stefan Schmid, and Hongfang Yu.  
IEEE/ACM International Symposium on Quality of Service (IWQoS), Phoenix, Arizona, USA, June 2019.

## **Demand-Aware Network Designs of Bounded Degree**

Chen Avin, Kaushik Mondal, and Stefan Schmid.  
31st International Symposium on Distributed Computing (DISC), Vienna, Austria, October 2017.

## **SplayNet: Towards Locally Self-Adjusting Networks**

Stefan Schmid, Chen Avin, Christian Scheideler, Michael Borokhovich, Bernhard Haeupler, and Zvi Lotker.  
IEEE/ACM Transactions on Networking (TON), Volume 24, Issue 3, 2016. Early version: IEEE IPDPS 2013.

## **Characterizing the Algorithmic Complexity of Reconfigurable Data Center Architectures**

Klaus-Tycho Foerster, Monia Ghobadi, and Stefan Schmid.  
ACM/IEEE Symposium on Architectures for Networking and Communications Systems (ANCS), Ithaca, New York, USA, July 2018.

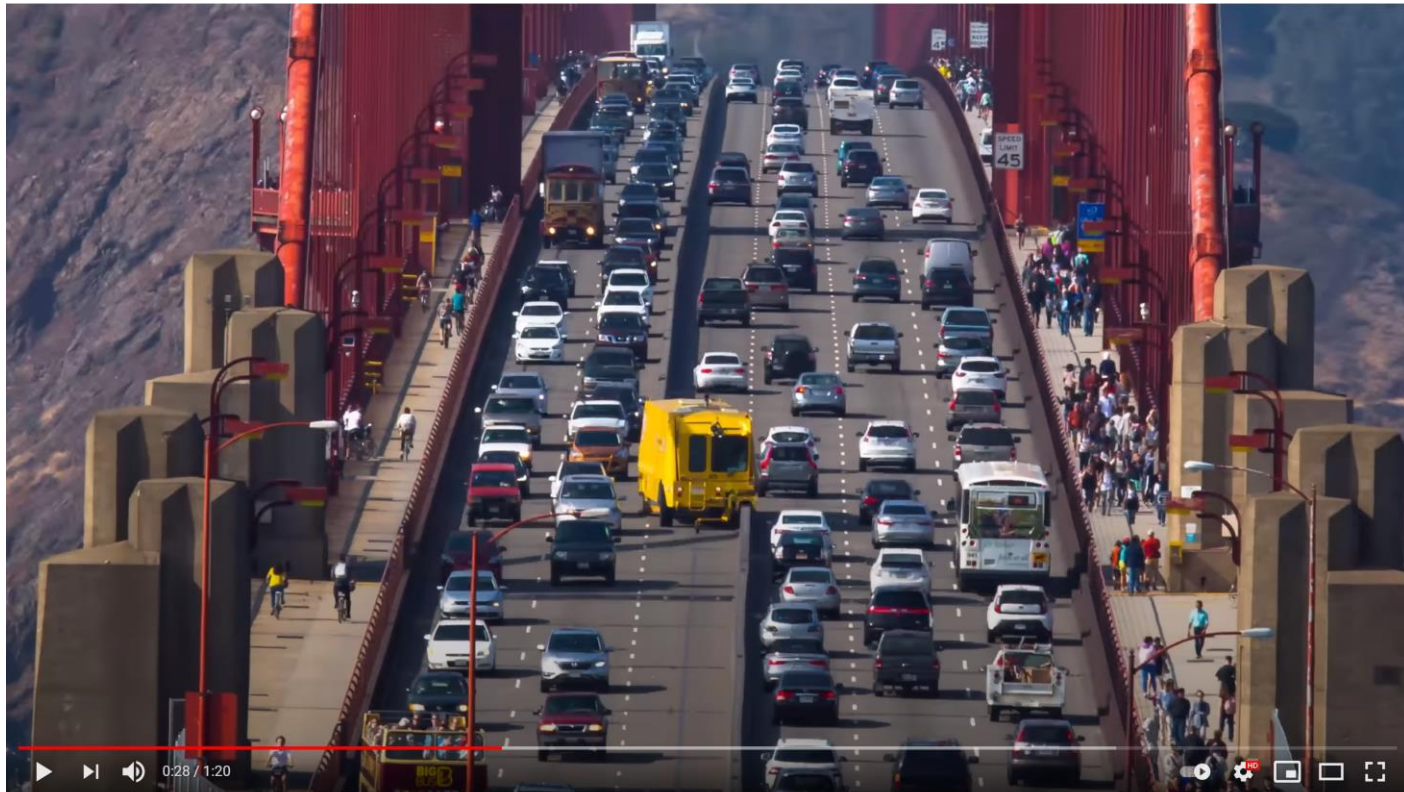
# Bonus Material



Hogwarts Stair



# Bonus Material



Golden Gate Zipper

# Bonus Material

07 May 2021 | 16:55 GMT

## Reconfigurable Optical Networks Will Move Supercomputer Data 100X Faster

Newly designed HPC network cards and software that  
reshapes topologies on-the-fly will be key to success

By Michelle Hampson



Photo illustration: Shutterstock

In HPC