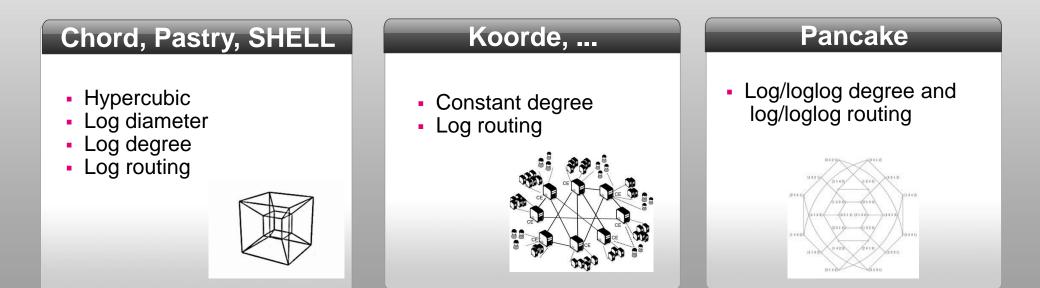
Locally Self-Adjusting Tree Networks

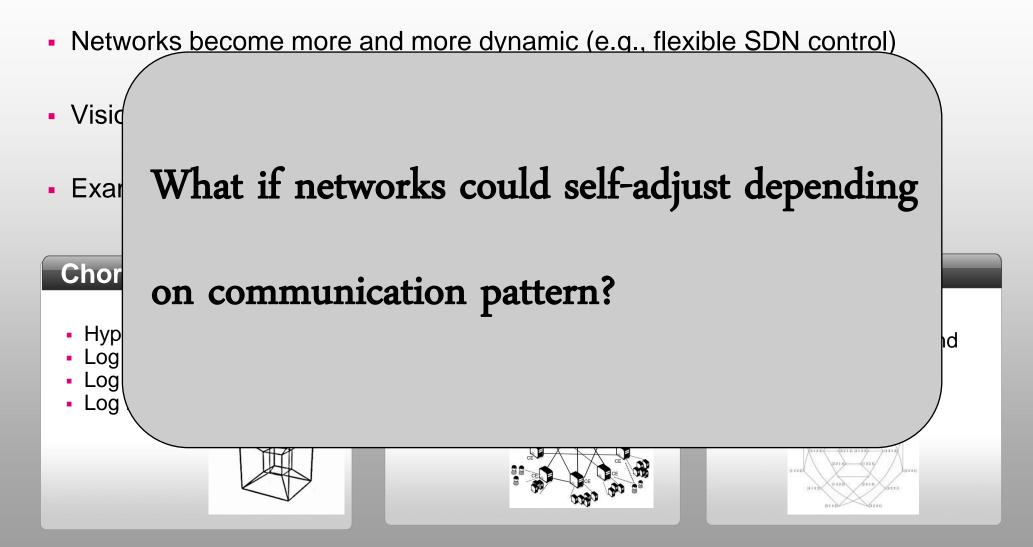
Chen Avin (BGU) Bernhard Häupler (MIT) Zvi Lotker (BGU) Christian Scheideler (U. Paderborn) **Stefan Schmid (T-Labs)**

From "Optimal" Networks to Self-Adjusting Networks

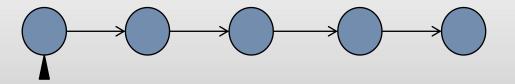
- Networks become more and more dynamic (e.g., flexible SDN control)
- Vision: go beyond classic "optimal" static networks
- Example (of this paper): Peer-to-peer

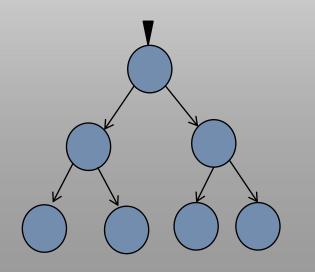


From "Optimal" Networks to Self-Adjusting Networks

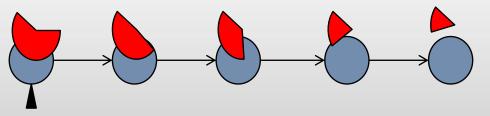


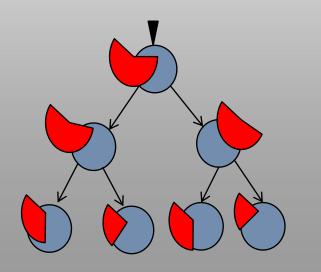
- Classic data structures: lists, trees
- Linked list: move frequently accessed elements to front!



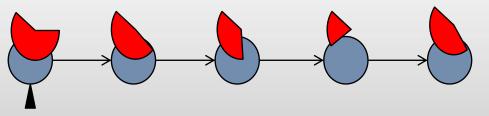


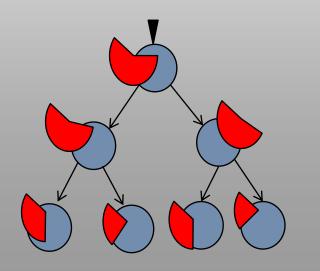
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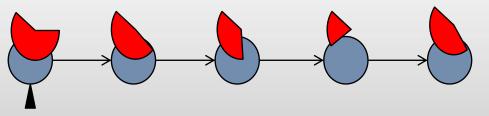


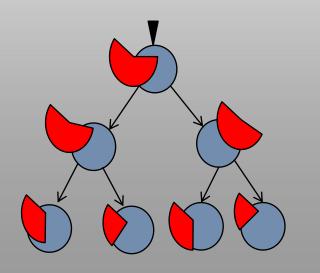
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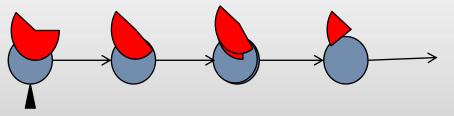


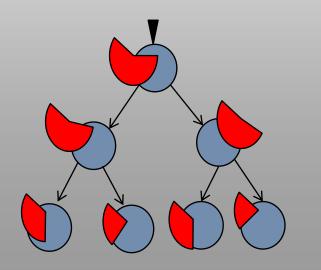
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- Classic data structures: lists, trees
- Linked list: move frequently accessed elements to front!



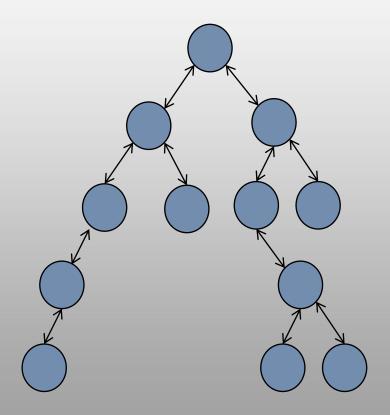


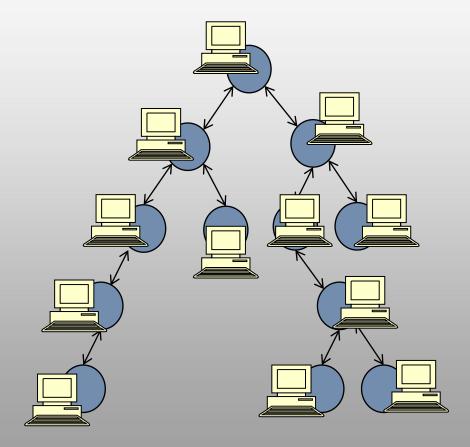
- Classic data structures: lists, trees •
- Linked list: move frequently accessed elements to front!

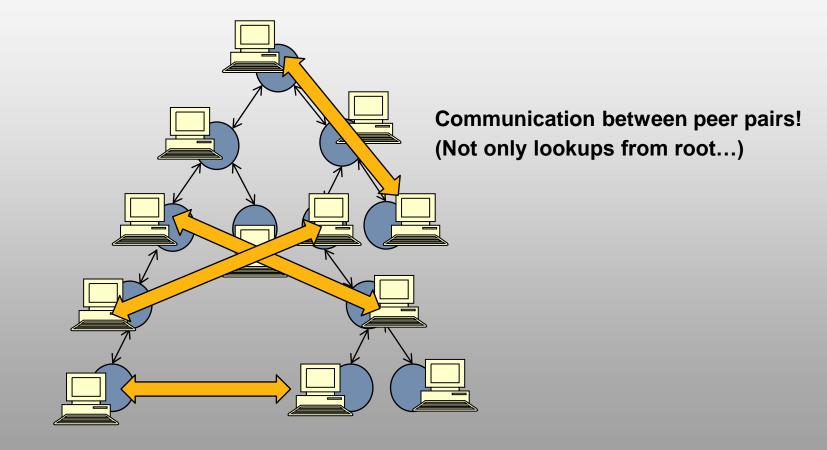
Trees: move frequently accessed elements

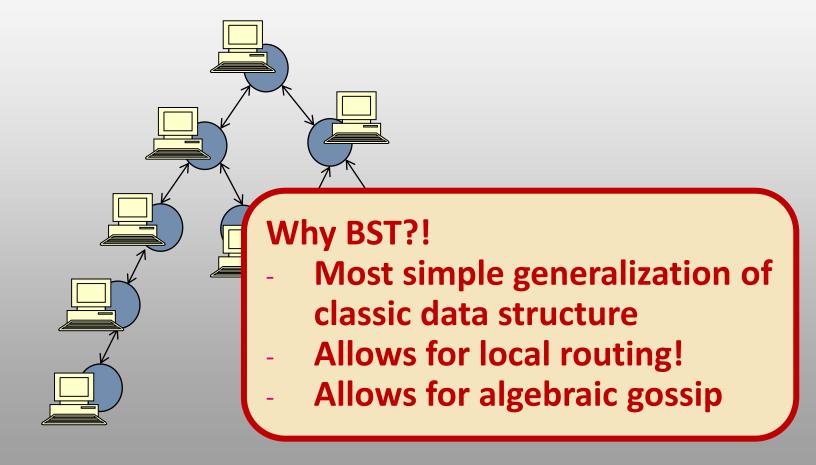


Stefan Schmid (T-Labs)









Model: Self-Adjusting SplayNets

Input:

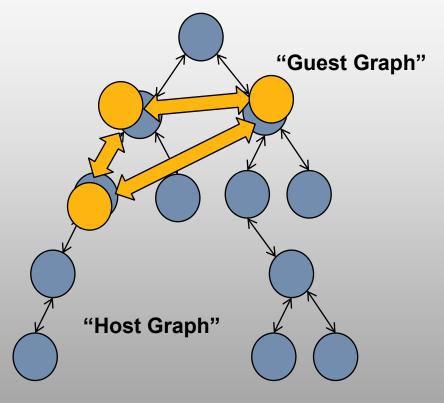
 communication pattern: (static or dynamic) graph

Output:

sequence of network adjustments

Cost metric:

- expected path length
- # (local) network updates



Our Contribution

SplayNets

- "Online algorithm" for self-adjusting distributed trees
- Optimal offline algorithm (polynomial time, for large class of graphs!)

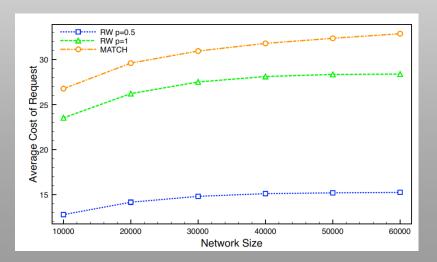
Locally Self-Adjusting Tree Networks

Chen Avin¹, Bernhard Haeupler², Zvi Lotker¹, Christian Scheideler³, Stefan Schmid⁴ ¹ Ben Gurion University, Israel; {avin,zvilo}@cse.bgu.ac.il ² Massachusetts Institute of Technology (MIT), USA; hauepler@mit.edu ³ University of Paderborn, Germany; scheideler@upd.de ⁴ TU Berlin & Telekom Innovation Laboratories, Germany; stefan@net.t-labs.tu-berlin.de

Abstract—This paper initiates the study of self-adjusting networks (or distributed data structures) whose topologies dynamically adapt to a communication pattern σ . We present a fully decentralized self-adjusting solution called SplayNet. A SplayNet is a distributed generalization of the classic splay tree concept. It ensures short paths (which can be found using local-greedy routing) between communication partners while minimizing topological rearrangements. We derive an upper bound for the amortized communication cost of a SplayNet based on empirical entropies of σ , and show that SplayNets have several interesting conversence properties. For instance. SplayNets features a

more frequently should become topologically closer to each other (i.e., the routing distance is reduced). This contrasts with most of today's structured peer-to-peer overlays whose topology is often optimized in terms of static global properties only, such as the node degree or the longest shortest routing path.

This paper focuses on a most fundamental network, a distributed binary search tree (BST) network. Such networks are a natural first extension of classic data structures. Moreover, they facilitate simple and local



Performance evaluation:

- General bounds on amortized costs
- Lower bounds (empirical entropy)
- Analysis of convergence times for important static comm. patterns
- Optimality of online algorithm for special patterns (e.g., matchings)
- Simulation study (Facebook data)

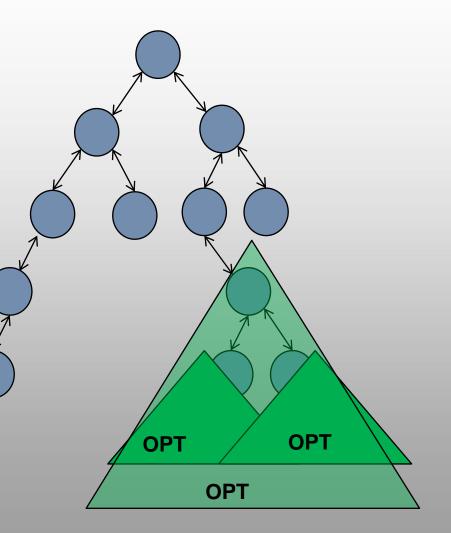
The Optimal Offline Solution

Dynamic program

- Binary search: decouple left from right!
- Polynomial time (unlike MLA!)
- So: solved M"BST"A

See also:

 Related problem of phylogenetic trees

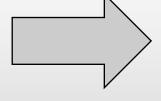


The Online SplayNets Algorithm

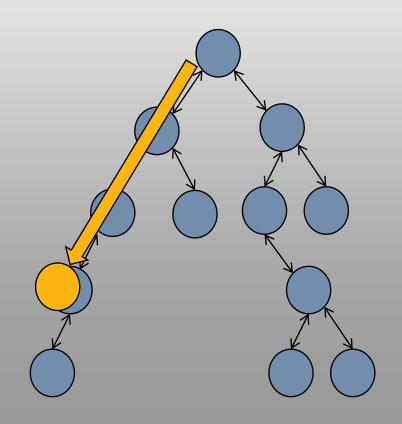
From Splay tree to SplayNet:

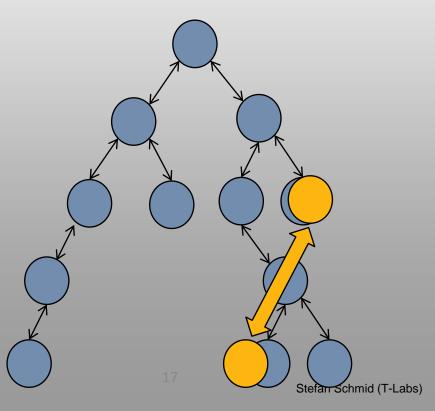
Algorithm 1 Splay Tree Algorithm ST 1: (* upon lookup (u) *)

2: splay u to root of T

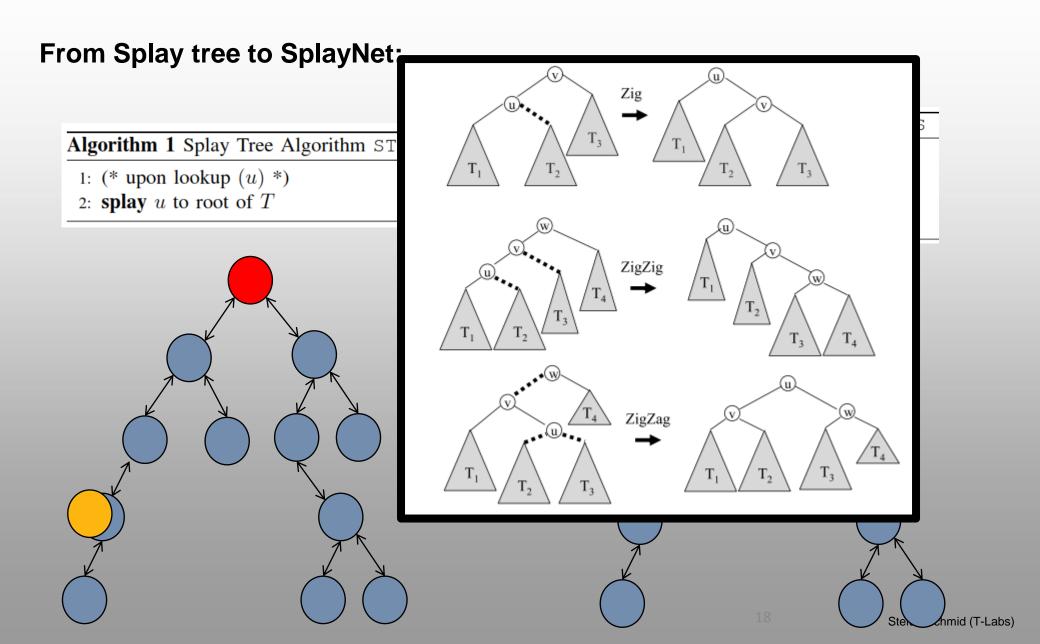


Algorithm 2 Double Splay Algorithm DS1: (* upon request (u, v) in T *)2: $w := \alpha_T(u, v)$ 3: T' := splay u to root of T(w)4: splay v to the child of T'(u)



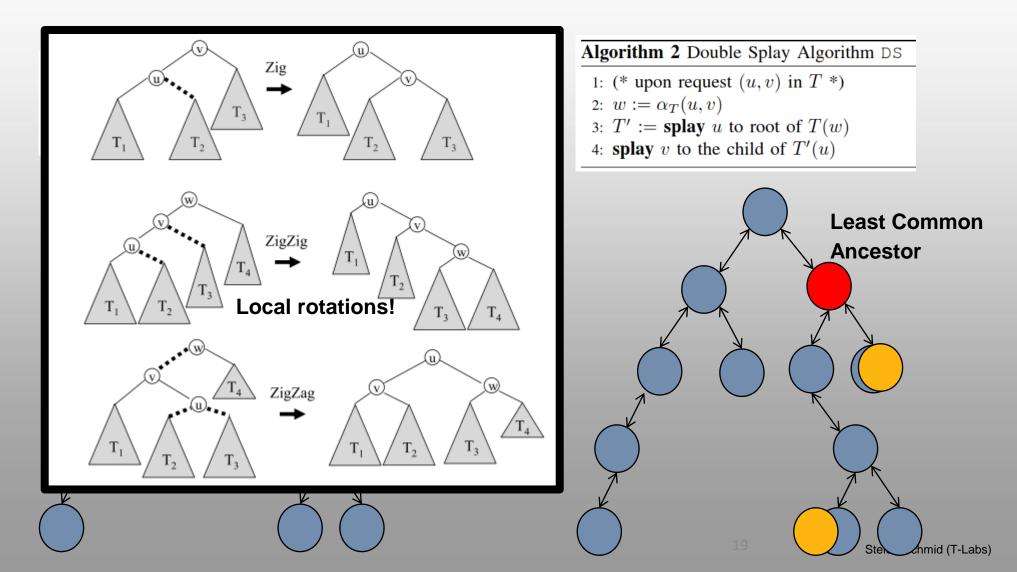


The Online SplayNets Algorithm



The Online SplayNets Algorithm

From Splay tree to SplayNet:



Analysis: Basic Lower and Upper Bounds

Upper Bound

A-Cost < H(X) + H(Y)

where H(X) and H(Y) are empirical entropies of sources resp. destinations

Adaption of Tarjan&Sleator

Lower Bound

A-Cost > H(X|Y) + H(Y|X)

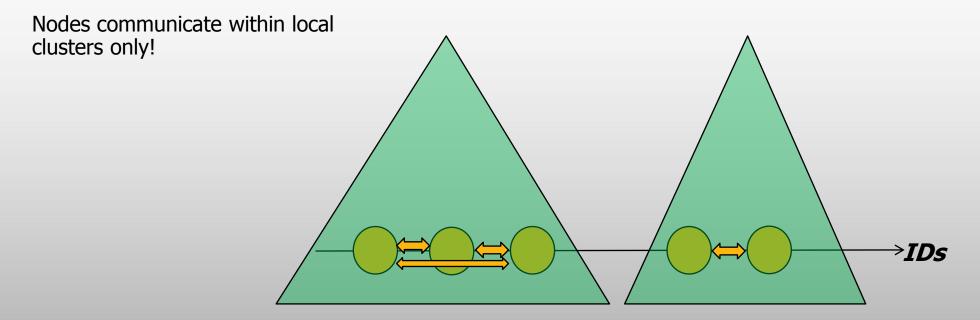
where H(|) are conditional entropies.

Assuming that each node is the root for "its tree"

Therefore, our algorithm is optimal, e.g., if communication pattern describes a product distribution!

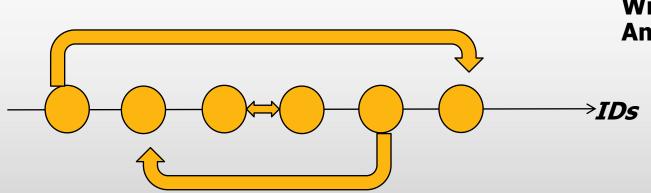
Properties: Convergence

Cluster scenario:



Over time, nodes will form clusters in BST! No paths "outside".

Properties: Optimal Solutions

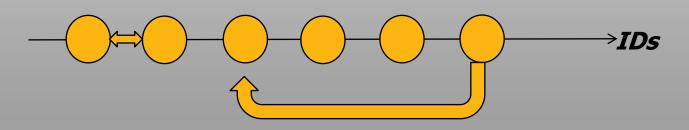


Will converge to optimum: Amortized costs 1.

Non-crossing matching (= "no polygamy") scenario:

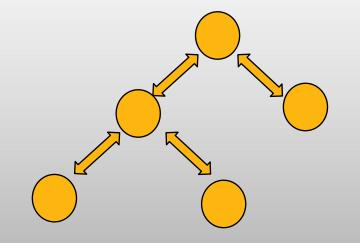
Laminated scenario:

Will converge to optimum: Amortized costs 1.

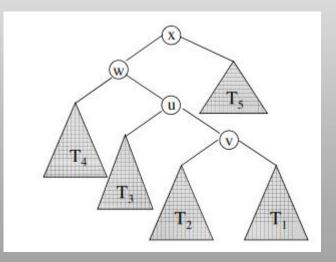


Properties: Optimal Solutions

Multicast scenario (BST): Example

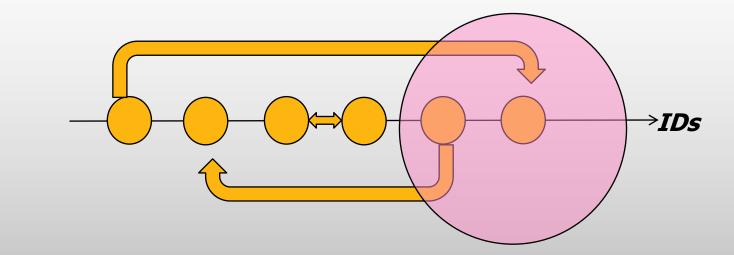


Invariant over "stable" subtrees (from right):

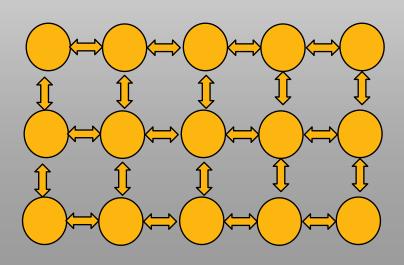


Improved Lower Bounds (and More Optimality)

Via interval cuts or conductance entropy:

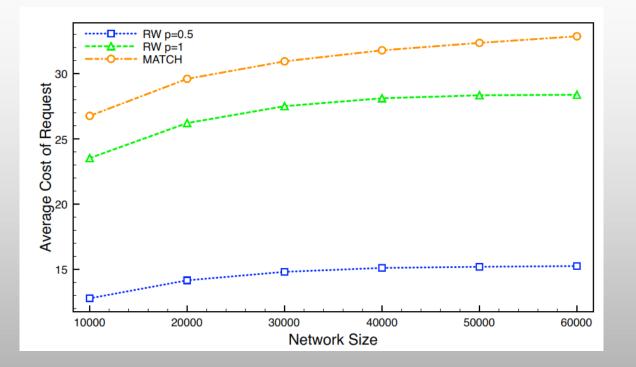


Grid:



Cut of interval: entropy yields amortized costs!

Simulation Results

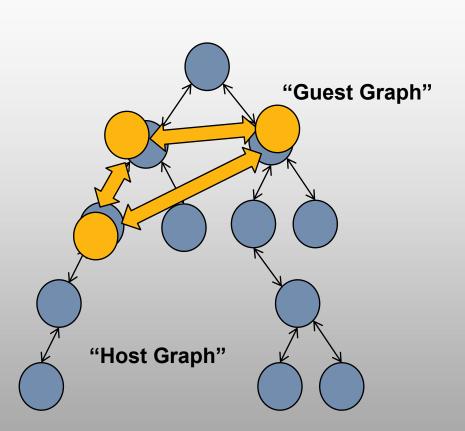


- Facebook component with 63k nodes and 800k edges
- SplayNet exploit random walk locality, to less extent also matching

Conclusion

- Vision: self-adjusting networks
- Interesting generalization of Splay trees
- SplayNets
 - Formal analysis reveals nice properties
 - Amortized costs good: but tight?
 - Competitive ratio remains open
- Future work? Yes ☺

Thank you! Questions?



Algorithm 2 Double Splay Algorithm DS

- 1: (* upon request (u, v) in T *)
- 2: $w := \alpha_T(u, v)$
- 3: T' := splay u to root of T(w)
- 4: splay v to the child of T'(u)

