

# Request Complexity of VNet Topology Extraction: Dictionary-Based Attacks

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# Introduction

- Cloud infrastructure = **secret**
  - Strategic reasons
  - Security reasons: bottlenecks,...
- Cloud providers now rent *virtual networks*
- Cloud provider answers customer requests:
  - **Yes** or **No**



*Cloud providers*

Do these answers leak information about the topology ?

Cloud Infrastructure  $H$  = static symmetric graph

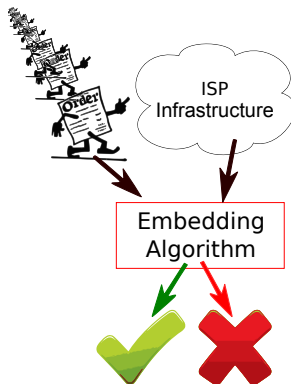
## Our questions

- Can we infer ISP infrastructure  $H$  using only ISP answers?
- How many requests do we need?

## A request:

- A graph  $G$  to realise
- Along with capacity requirements  $\in [0, 1]$

In the following: only **unit capacities**



# Our model

Cloud Infrastructure  $H$  = static symmetric graph

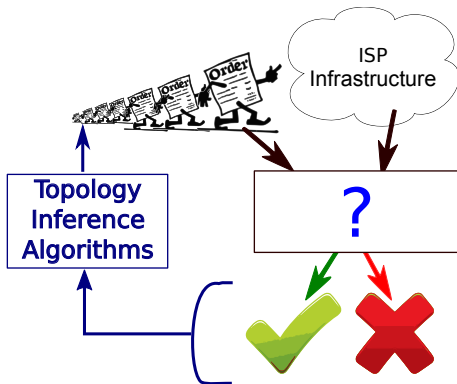
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# Embedding properties

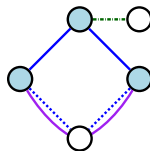
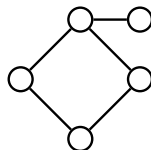
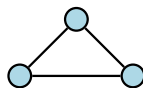
$G \mapsto^? H$ : **Yes** if:

- Every node in  $G$  is mapped to exactly one node in  $H$
- Every edge in  $G$  is mapped to exactly one *path* in  $H$

*path* in  $H \Rightarrow$

- each node on the path is a *relay* node
- relaying costs  $\epsilon$  for each node on the path

Request      Substrate



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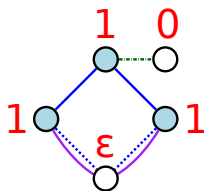
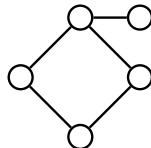
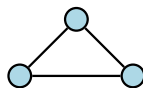
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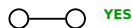
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If we know  $H$  is a tree

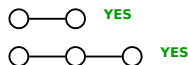


Principle: **grow** a topology in  $H$ :

$G_1, \dots, G_k$  s.t.  $\forall i < j, G_i \subset G_j$

- ① find a diameter
- ② mark extremities explored.
- ③ for each unexplored vertex
  - ① append longest chains
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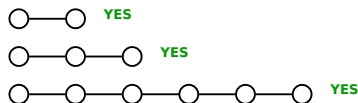
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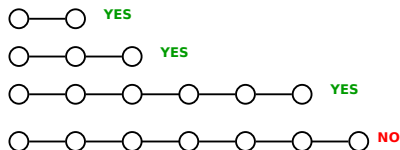
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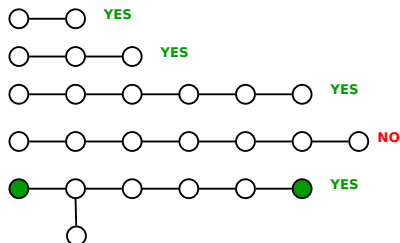


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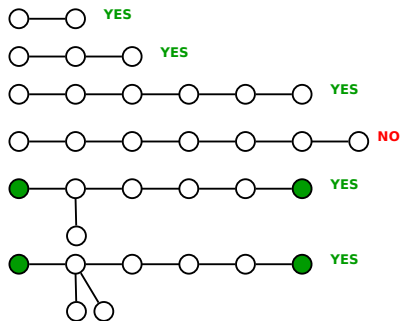
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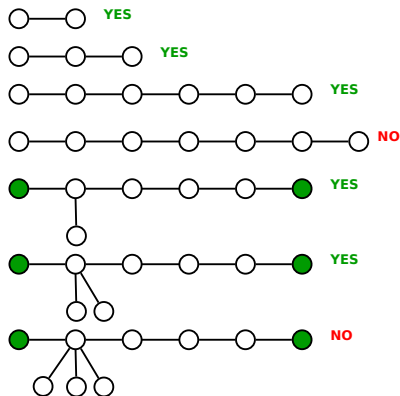
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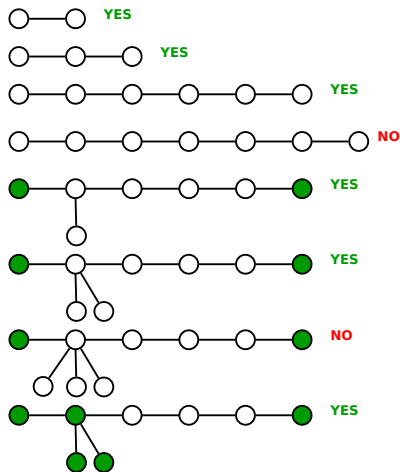
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- **Correctness:**  $H$  is connected, we explore all the possible paths
- **Cost:** each **Yes** we discover at least one more node. Each **No** we mark one node explored  $\Rightarrow$

$$\text{cost}(Tree) = \theta(n)$$

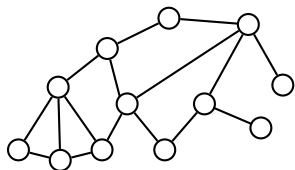
- **Optimality:** |possible trees of size  $n$ |  $\approx 2.96^n / n^{5/2}$   
([Plotkin, Rosenthal94])  
 $\Rightarrow$  at least  $\log(2.96^n / n^{5/2}) = \Omega(n)$  requests using binary answers

*Tree* is asymptotically optimal

# General graphs

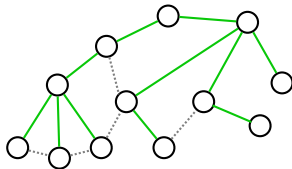
*Works for general graphs!*

- Tree provides a spanning tree on general graphs
- Algorithm sketch
  - Let  $T = \text{Tree}(H)$
  - $\forall i, j \in V(T)^2$  try  $T \cup \{(i, j)\}$



Analysis

- Complexity:  $n^2$  (we test each pair)
- Lower bound:
$$|\{H \text{ of } n \text{ nodes}\}| \geq \frac{2^{\binom{n}{2}}}{n!}$$
$$\Rightarrow \Omega(n^2) \text{ in a binary answer model}$$
$$\Rightarrow \text{asymptotically optimal}$$





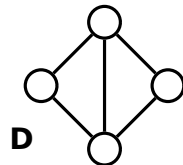
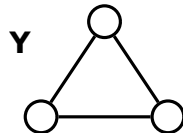
**Can we do better ?**

E.g.  $\text{cost}(\textit{Discovery}) = \theta(|E(H)|)$

# Sometimes Yes!

**Idea:** Compose « little » graph structures

- *Motifs*: minimal bi-connected subgraph that reserves a hole  $H$  subgraph
- $\Rightarrow H$  is a **tree** of such motifs!
- Approach: compose motifs.
- **However** composition is not straightforward  
 $\Rightarrow$  need to have composition rules:  
**dictionary!**
- Key idea:  $\mapsto$  on motif set is a poset

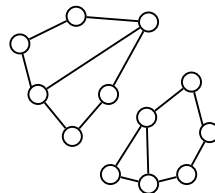
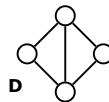


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# Evaluation

- RocketFuel topologies
- A European power distribution grid

For each topology:

- Identify tree nodes
- Identify relay nodes
- Extract motifs

Tools:

- R
- ggplot2
- R::igraph



# Results

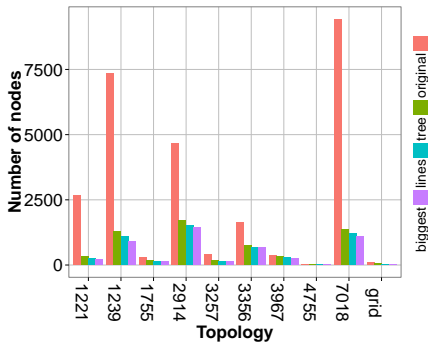


FIGURE: Composition of each topology:  
Tree, Relay and Motif nodes breakout

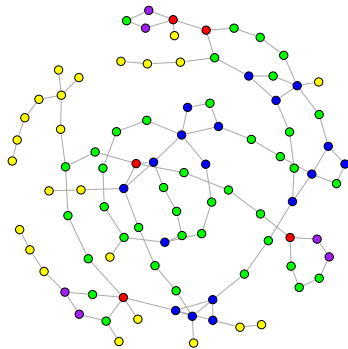
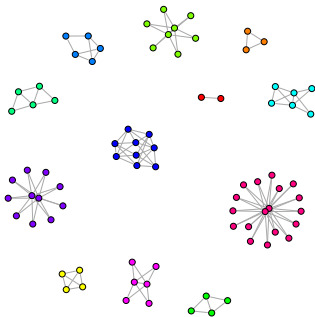
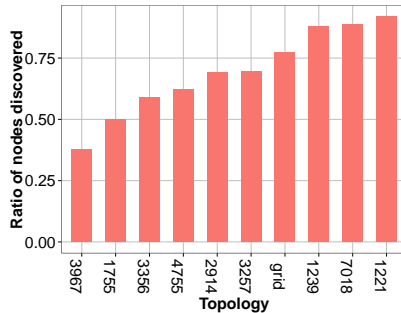


FIGURE: The « grid » topology



**FIGURE:** Common motifs found in the topologies



**FIGURE:** Ratio of the topology discoverable with the dictionary

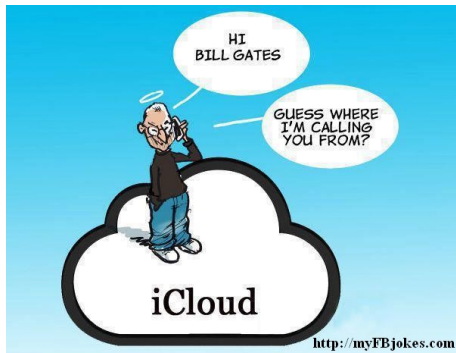
# Conclusion

Can information leak through Vnet embedding answers: **Yes !**

- General case: slow
- Small dictionary  $\Rightarrow$  fast leak !

## Directions

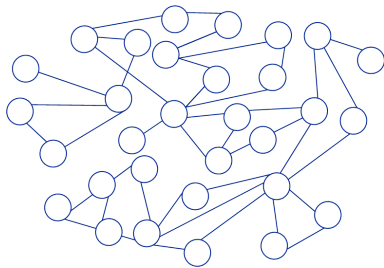
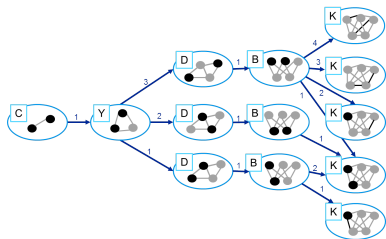
- (Outer)Planar graphs ?
- Only partial info:
  - min-cut
  - bounded stretch ?



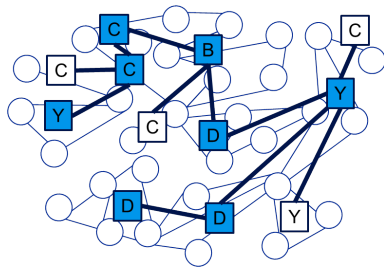
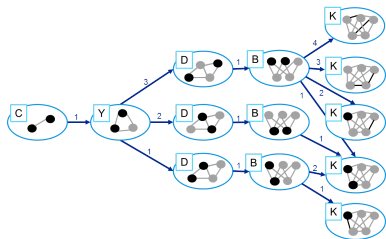
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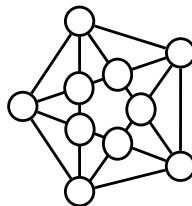
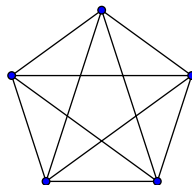
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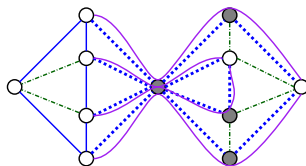
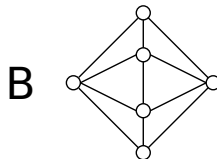
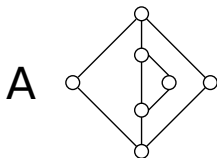
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- Minor differences



# Observations



**AA → BB**

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