Principles of Distributed Network Design

Stefan Schmid *et al.*, mainly Chen Avin (BGU, Israel)

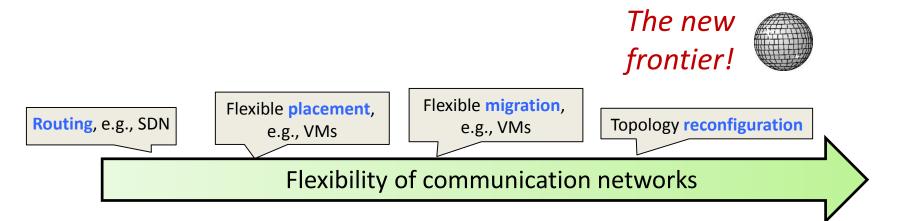


Flexible Distributed Systems: A Great Time To Be a Researcher!



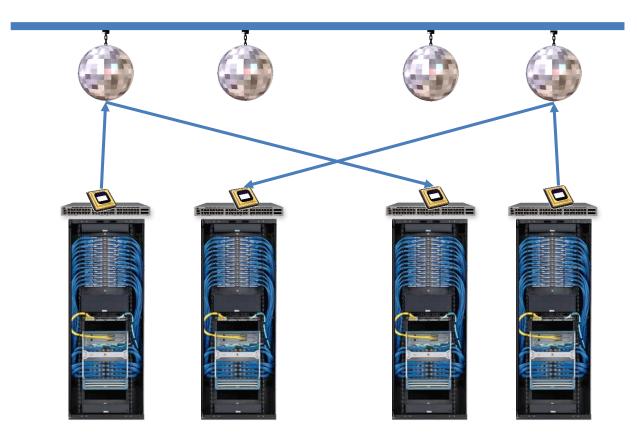
Rhone and Arve Rivers, Switzerland

> Credits: George Varghese.



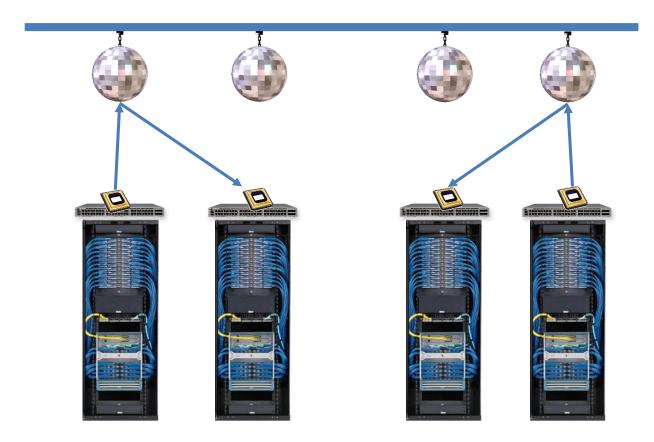
Technological Motivation

Example: Free-Space Optics (*ProjecToR*)



t=1

Example: Free-Space Optics (*ProjecToR*)

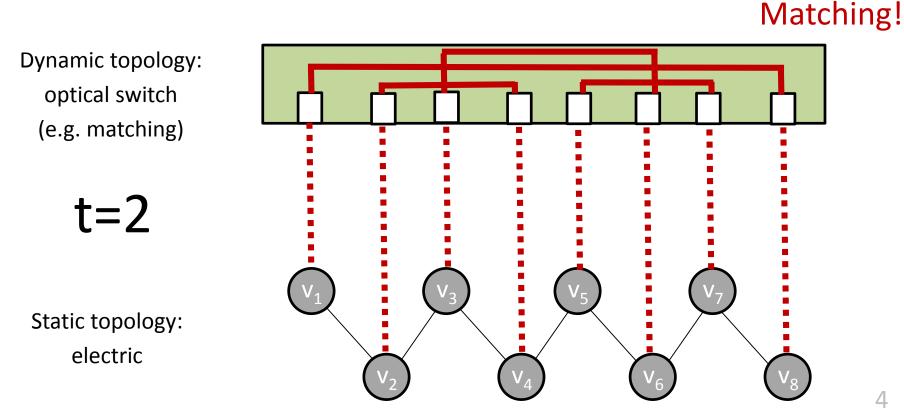


t=2

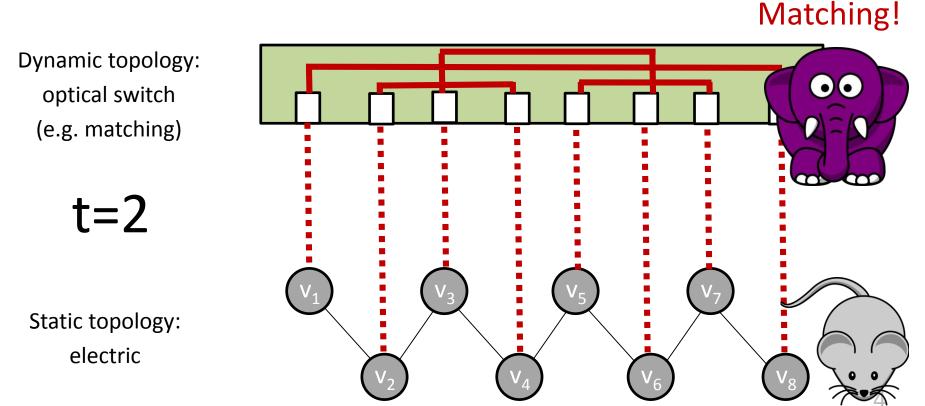
Example: Reconfigurable Optical Switches (*Helios, c-Through,* etc.) Matching!

Dynamic topology: optical switch (e.g. matching) t=1 Static topology: electric

Example: Reconfigurable Optical Switches (Helios, c-Through, etc.)



Example: Reconfigurable Optical Switches (*Helios, c-Through,* etc.)



Further Reading

Free-Space Optics

- Ghobadi et al., "Projector: Agile reconfigurable data center interconnect," SIGCOMM 2016.
- Hamedazimi et al. "Firefly: A reconfigurable wireless data center fabric using free-space optics," CCR 2014.

Optical Circuit Switches

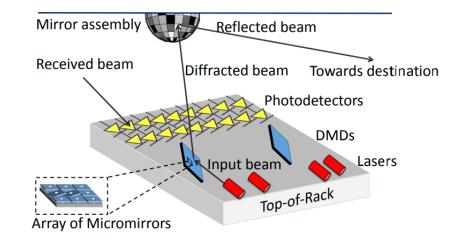
- Farrington et al. "*Helios*: a hybrid electrical/optical switch architecture for modular data centers," CCR 2010.
- Mellette et al. "*Rotornet*: A scalable, low-complexity, optical datacenter network," SIGCOMM 2017.
- Farrington et al. "Integrating microsecond circuit switching into the data center," SIGCOMM 2013.
- Liu et al. "Circuit switching under the radar with reactor.," NSDI 2014

Movable Antennas

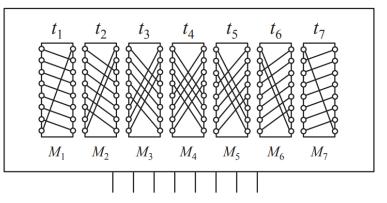
 Halperin et al. "Augmenting data center networks with multi-gigabit wireless links," SIGCOMM 2011.

60GHz Wireless Communication

- Zhou et al. "Mirror mirror on the ceiling: Flexible wireless links for data centers," CCR 2012.
- Kandula et al. "Flyways to de-congest data center networks," 2009.



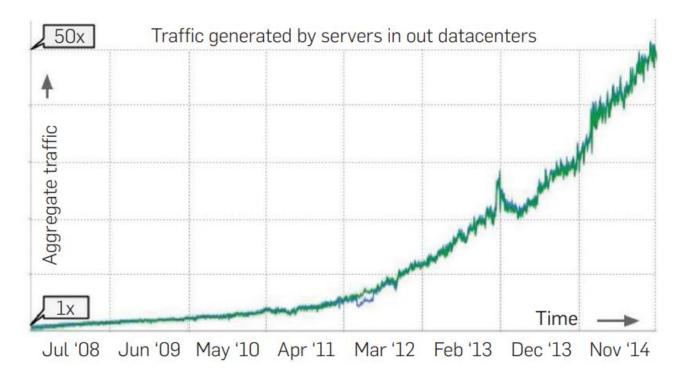
Rotor switch



Etc.!

Empirical Motivation

Data-Centric Applications: Growing Traffic...



Aggregate server traffic in Google's datacenter fleet

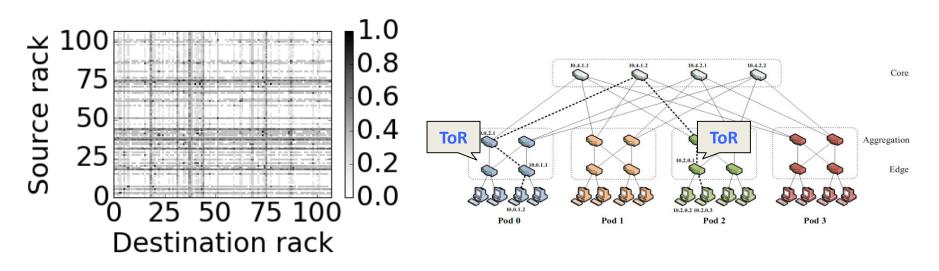
Source: Jupiter Rising.

SIGCOMM 2015.

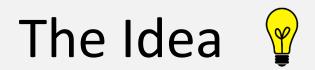
... But Much Structure!

Heatmap rack-to-rack traffic:

Clos topology and ToR switches:



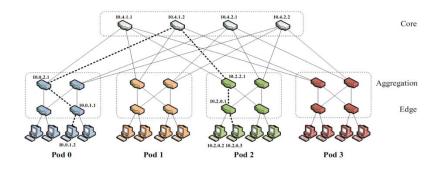
ProjecToR @ SIGCOMM 2016



Traditional Networks

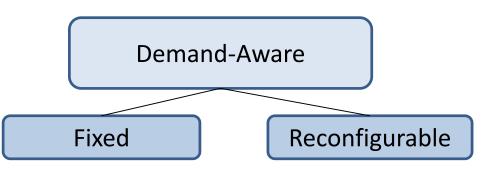


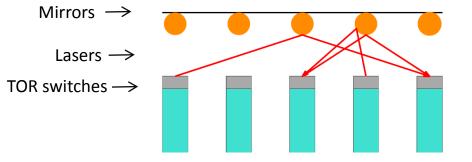
- Usually optimized for the "worstcase" (all-to-all communication)
- Example, fat-tree topologies: provide full bisection bandwidth
- Lower bounds and hard trade-offs, e.g., degree vs diameter



Demand-Aware Networks

- **DAN**: Demand-Aware Network
 - Statically optimized toward the demand
- **SAN**: Self-Adjusting Network
 - Dynamically optimized toward the (time-varying) demand





Roadmap

- Vision and Motivation
- An analogy: coding and datastructures
- Principles of Demand-Aware Network (DAN) Designs
- Principles of Self-Adjusting Network (SAN) Designs
- Principles of Decentralized Approaches



Roadmap

Vision and Motivation

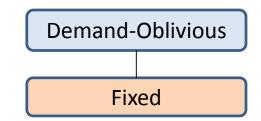


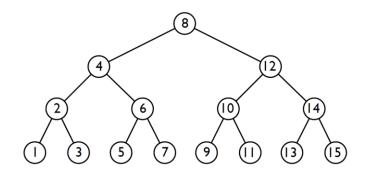
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Analogous to *Datastructures*: Oblivious...

- Traditional, **fixed** BSTs do not rely on any assumptions on the demand
- Optimize for the worst-case

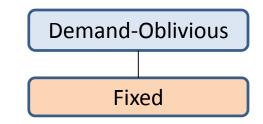


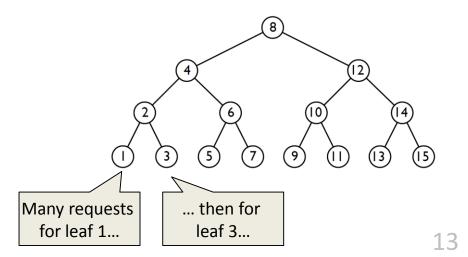


Analogous to *Datastructures*: Oblivious...

- Traditional, **fixed** BSTs do not rely on any assumptions on the demand
- Optimize for the worst-case
- Example demand:

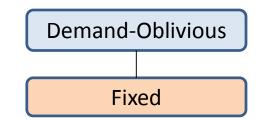
 Items stored at O(log n) from the root, uniformly and independently of their frequency

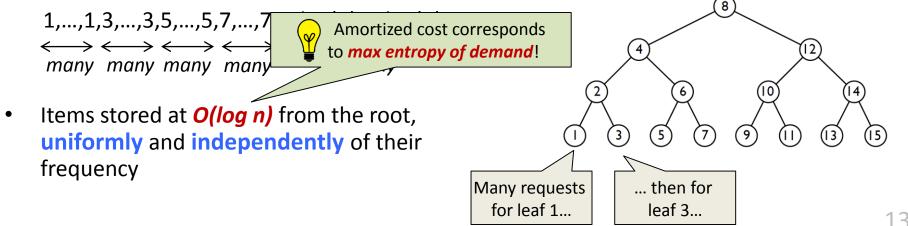




Analogous to *Datastructures*: Oblivious...

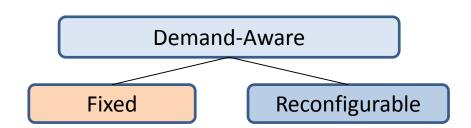
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- Example demand:





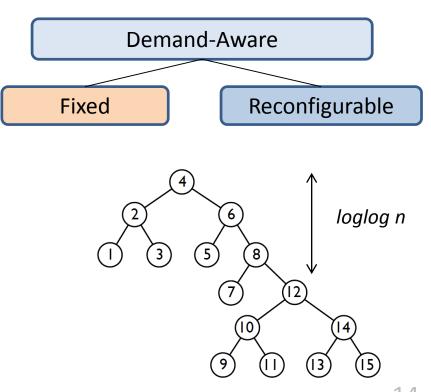
... Demand-Aware ...

- Demand-aware fixed BSTs can take advantage of *spatial locality* of the demand
- E.g.: place frequently accessed elements close to the root
- E.g., Knuth/Mehlhorn/Tarjan trees



... Demand-Aware ...

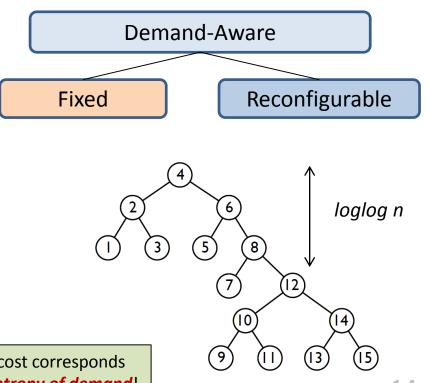
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- Recall example demand: 1,...,1,3,...,3,5,...,5,7,...,7,...,log(n),...,l og(n)
 - Amortized cost O(loglog n)



... Demand-Aware ...

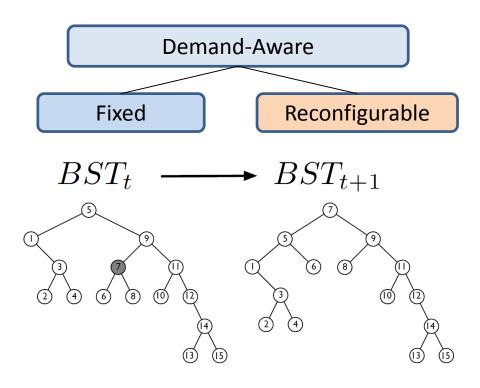
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 - Amortized cost O(loglog n)





... Self-Adjusting!

- Demand-aware reconfigurable BSTs can additionally take advantage of temporal locality
- By moving accessed element to the root: amortized cost is *constant*, i.e., O(1)
 - Recall example demand:
 1,...,1,3,...,3,5,...,5,7,...,7,...,log(n),...,log(n)
- Self-adjusting BSTs e.g., useful for implementing *caches* or garbage collection

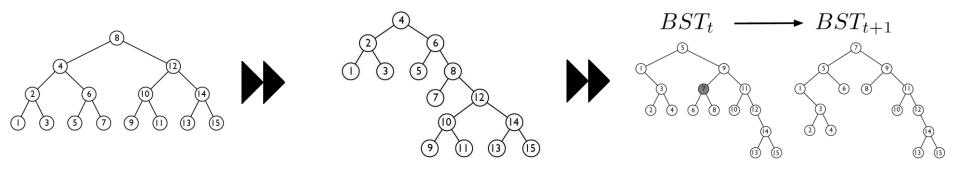


Datastructures

Oblivious

Demand-Aware

Self-Adjusting



Lookup O(log n)

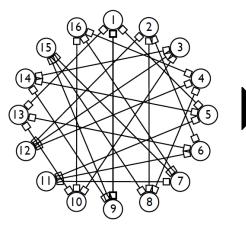
Exploit spatial locality: empirical entropy O(loglog n) Exploit temporal locality as well: O(1)

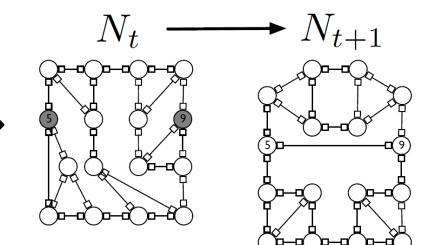
Analogously for Networks

Oblivious

DAN

SAN





Const degree (e.g., expander): route lengths *O(log n)* Exploit spatial locality: Route lengths depend on conditional entropy of demand

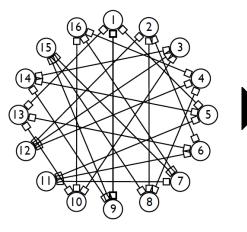
Exploit temporal locality as well

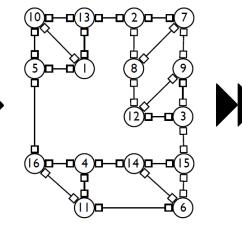
Analogously for Networks

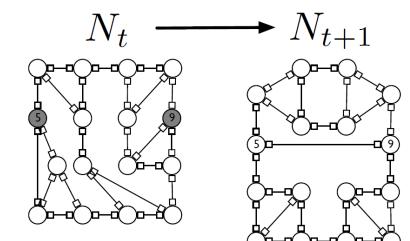
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Const degree (e.g., expander): route lengths *O(log n)* Exploit spatial locality: Route lengths depend on conditional entropy of demand

Exploit temporal locality as well

Toward Demand-Aware Networking: A Theory for Self-Adjusting Networks. **ArXiv** 2018.

How useful are DANs/SANs?

As always in computer science (e.g., also in coding, in selfadjusting datastructures, etc.): it depends! ^(C)

Roadmap

Vision and Motivation

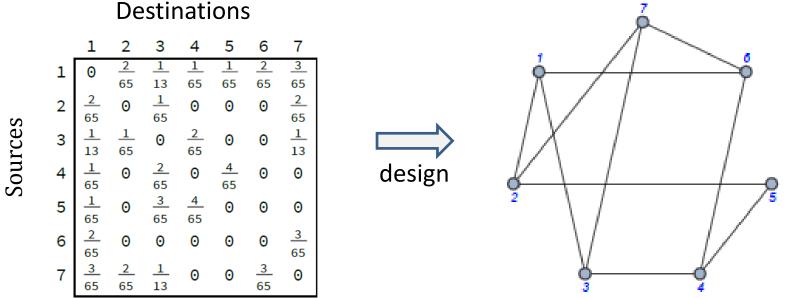


- An analogy: coding and datastructures
- Principles of Demand-Aware Network (DAN) Designs
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Input: Workload

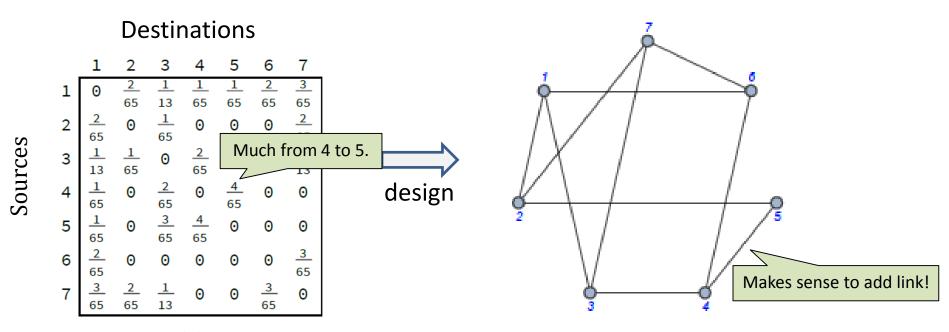
Output: DAN



Demand matrix: joint distribution

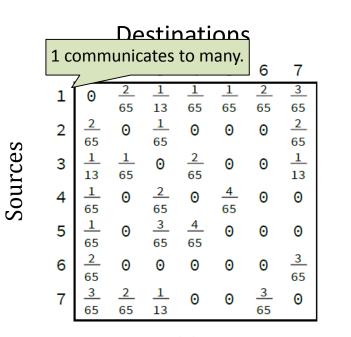
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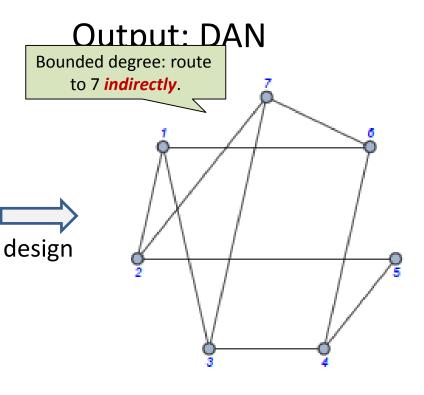
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Demand matrix: joint distribution

Input: Workload

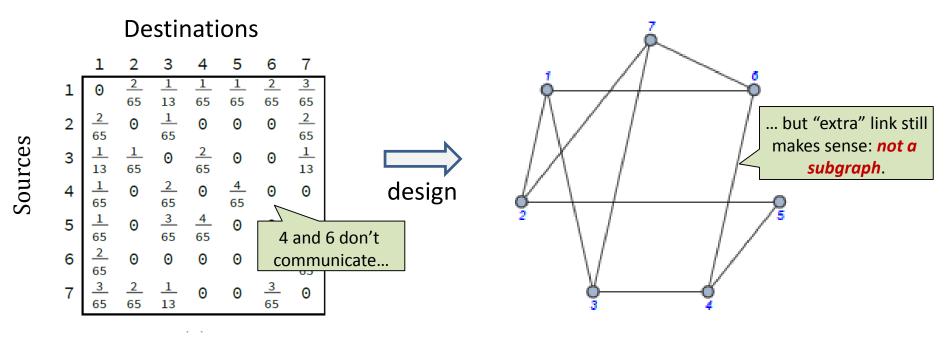




Demand matrix: joint distribution

Input: Workload

Output: DAN

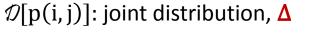


Demand matrix: joint distribution

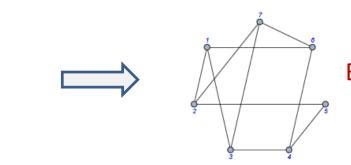
Case Study: Expected Route Length

Shorter paths: smaller bandwidth footprint, lower latency, less energy, ...

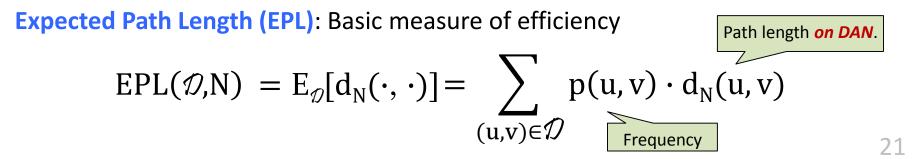
More Formally: DAN Design Problem Input: Output:



N: DAN



Bounded degree $\Delta = 3$



The Goal: Bounded Network Design (BND)

Inputs: Communication distribution D[p(i,j)]_{nxn} and a maximum degree Δ.

• **Output**: A Demand Aware Network $N \in N_{\Delta}$ s.t.

$$BND(\mathcal{D}, \Delta) = \min_{\mathbf{N} \in N_{\Delta}} EPL(\mathcal{D}, \mathbf{N})$$

Belong to some graph family: bounded-degree, but e.g. also local routability!

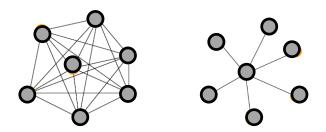
Examples

• What about BND for $\Delta = n$?

Examples

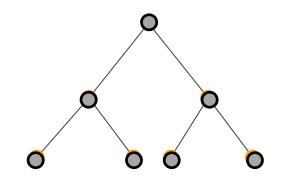
• What about BND for $\Delta = n$?

 Easy: e.g., clique and star have constant EPL but unbounded degree.

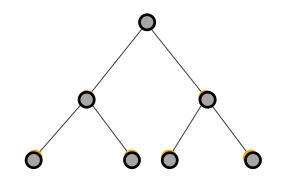


• What about $\Delta = 3$?

- What about $\Delta = 3$?
 - E.g., complete binary tree
 - $d_N(u,v) \le 2 \log n$
 - Can we do better than log n?

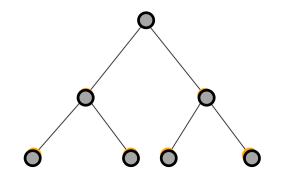


- What about $\Delta = 3$?
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• What about $\Delta = 2$?

- What about $\Delta = 3$?
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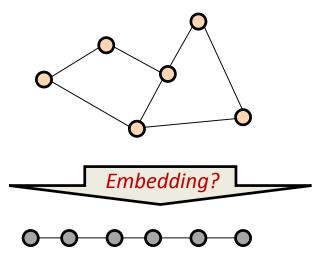


- What about $\Delta = 2$?
 - E.g., set of lines and cycles

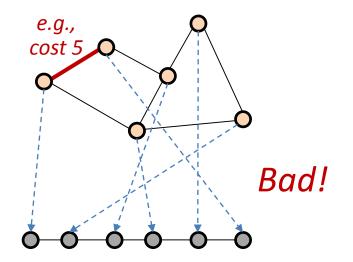


How hard is it to design a DAN?

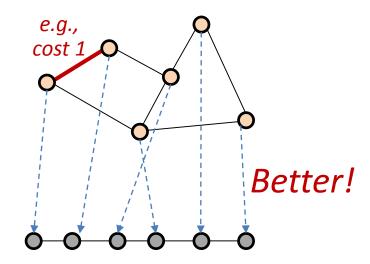
- Example Δ = 2: A Minimum Linear Arrangement (MLA) problem
 - A "Virtual Network Embedding Problem", VNEP
 - Minimize sum of lengths of virtual edges



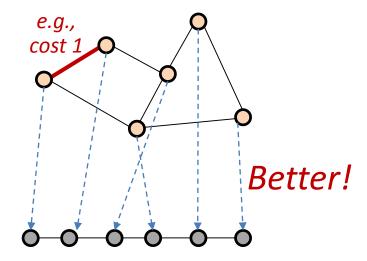
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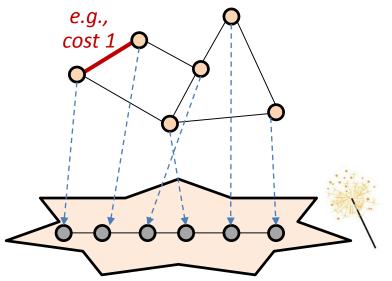


- Arrangement (M DAN design in Arrangement (M DAN design in Arrangement (M DAN design)
 A "Virtual N and so is bedding Problem"
 Minim Ard, and so is bedding Problem'
 Minim Ard, and so is bedding Problem. • Example Δ = 2: A Mipi inear
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 A "Virtual M and so is bedding Problem", engths of virtual edges • Example $\Delta = 2$: A Mipi inear
 - Jedding Problem", VNEP
- But what about > 2? Embedding problem still hard, but we have an additional degree of freedom:

Do topological flexibilities make problem easier or harder?!



A new knob for optimization!

Also Related To...:

• Sparse, distance-preserving (low-distortion) spanners

- But:
 - Spanners aim at low distortion among *all pairs*; in our case, we are only interested in the *local distortion*, 1-hop communication neighbors
 - We allow auxiliary edges (not a subgraph): similar to geometric spanners
 - We require *constant degree*

Expected Path Length in Traditional Networks?

Theorem (Traditional Networks):

Proof.

Each network with n nodes and max degree $\Delta > 2$ must have a diameter of at least log(n)/log(Δ -1)-1.

In k steps, reach at most $1 + \sum \Delta(\Delta - 1)^i$

1 Δ $\Delta(\Delta-1)$

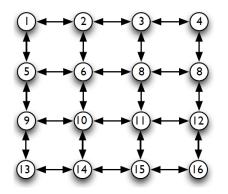
Corollary: Constant-degree graphs have at least logarithmic diameter.

Example: Clos, Bcube, Xpander.

Can DANs do better?

Yes, constant-degree DANs can!

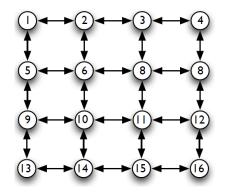
• Example 1: demand



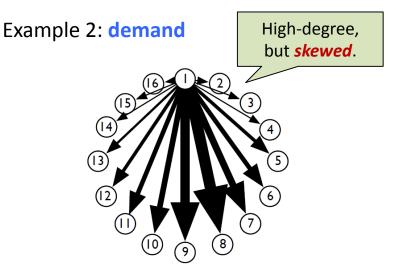
- Oblivious design diameter O(log n) (e.g., Δ-ary tree)
- But constant-degree DAN can serve it at cost O(1).

Yes, constant-degree DANs can!

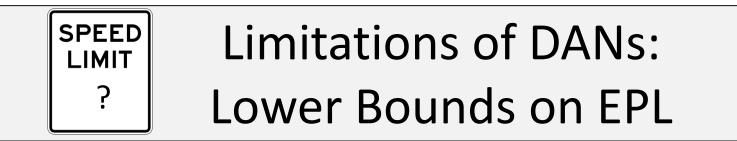
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- Oblivious design: diameter O(log n) (e.g., Δ-ary tree)
- But constant-degree DAN can serve it at cost O(1) (e.g., Huffman tree for node 1)





Lower Bound Idea: Leverage Coding or Datastructure!

Destinations

		1	2	3	4	5	6	7	
	1	Θ	<u>2</u> 65	$\frac{1}{13}$	$\frac{1}{65}$	$\frac{1}{65}$	<u>2</u> 65	<u>3</u> 65	
Sources	2	<u>2</u> 65	Θ	<u>1</u> 65	0	Θ	0	2 65 <u>1</u> 13	
	3	$\frac{2}{65}$ $\frac{1}{13}$ 1	$\frac{1}{65}$	Θ	<u>2</u> 65	Θ	0	<u>1</u> 13	
	4	<u>1</u> 65	Θ	<u>2</u> 65	0	<u>4</u> 65	0	0	
	5	65 <u>1</u> 65 <u>2</u> 65 <u>3</u>	Θ	<u>3</u> 65	<u>4</u> 65	Θ	0	0	
	6	<u>2</u> 65	Θ	Θ	Θ	Θ	Θ	<u>3</u> 65	
	7	<u>3</u> 65	<u>2</u> 65	$\frac{1}{13}$	0	0	<u>3</u> 65	0	
									1

- Consider *(source) node* 1: best Δ-ary tree we can build for this source is Huffman tree for its destinations [0,1/65,1/13,1/65,1/65,2/65,3/65]
 - resp. Knuth/Mehlhorn/Tarjan tree if search property required
- How good can this tree be?

Lower Bound Idea: Leverage Coding or Datastructure!

Destinations

		1	2	3	4	5	6	7	
Sources	1	0	<u>2</u> 65	$\frac{1}{13}$	$\frac{1}{65}$	$\frac{1}{65}$	<u>2</u> 65	<u>3</u> 65	
	2	<u>2</u> 65	0	<u>1</u> 65	0	0	0	2 65 <u>1</u> 13	
	3	$\frac{2}{65}$ $\frac{1}{13}$ $\frac{1}{65}$	<u>1</u> 65	Θ	<u>2</u> 65	0	0	<u>1</u> 13	
	4		0	2 65 3	Θ	<u>4</u> 65	0	0	
	5	1 65 2 65 3	Θ	<u>3</u> 65	<u>4</u> 65	Θ	0	0	
	6	<u>2</u> 65	Θ	0	0	0	0	<u>3</u> 65	
	7	<u>3</u> 65	<u>2</u> 65	<u>1</u> 13	0	0	<u>3</u> 65	0	

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 [0,1/65,1/13,1/65,1/65,2/65,3/65]
 - resp. Knuth/Mehlhorn/Tarjan tree if search property required
- How good can this tree be?



Entropy lower bound known on EPL known for binary trees, e.g. *Mehlhorn* 1975 for BST

Lower Bound Idea: Leverage Coding or Datastructure!

Destinations

		1	2	3	4	5	6	7	
	1	Θ	<u>2</u> 65	$\frac{1}{13}$	$\frac{1}{65}$	$\frac{1}{65}$	<u>2</u> 65	<u>3</u> 65	
S	2	<u>2</u> 65	0	<u>1</u> 65	0	0	0	2 65 <u>1</u> 13	
Sources	3	$\frac{2}{65}$ $\frac{1}{13}$ $\frac{1}{65}$	<u>1</u> 65	Θ	<u>2</u> 65	0	Θ	$\frac{1}{13}$	
Sou	4	<u>1</u> 65	0	2 65 3	Θ	<u>4</u> 65	Θ	0	
	5	1 65 2 65 3	0	<u>3</u> 65	<u>4</u> 65	Θ	Θ	0	
	6	<u>2</u> 65	0	Θ	0	Θ	Θ	<u>3</u> 65	
	7	<u>3</u> 65	<u>2</u> 65	<u>1</u> 13	0	0	<u>3</u> 65	0	
		65	65	13			65		

- Consider (source) node 1: best Δ-ary tree we can build for this source is Huffman tree for its destinations [0,1/65,1/13,1/6] An optimal ego-tree
 - resp. Knuth/Me property requir
- for this source!
- How good can this tree be?



Entropy lower bound known on EPL known for binary trees, e.g. *Mehlhorn* 1975 for BST

Entropy lower bound for Binary Search Trees (BST):

Let H(p) be the entropy of the frequency distribution p = (p1, p2, ..., pn). Let T be an optimal binary search tree built for the above frequency distribution. Then $EPL(p, T) \ge H(p)/log(3)$.

Corollary: Can generalize it easily to other degrees Δ .

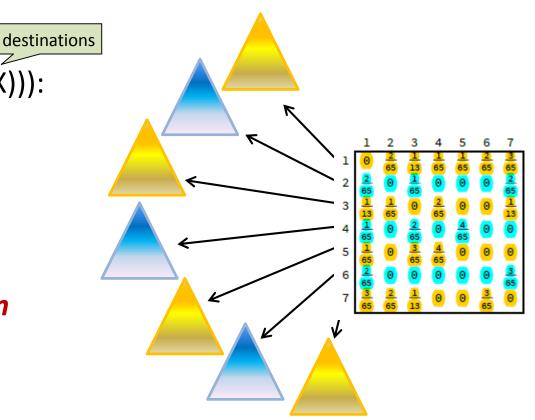
An Entropy Lower Bound (Sources)

• **Proof idea** (EPL= $\Omega(H_{\Delta}(Y|X))$):

sources

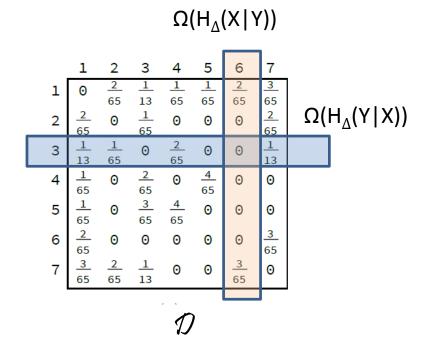
 Consider *union* of all egotrees

 Violates *degree restriction* but valid lower bound

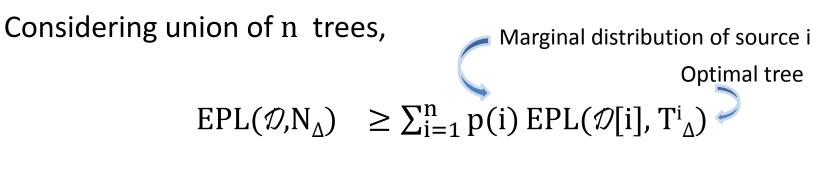


Lower Bound: Sources + Destinations

Do this in **both dimensions**: EPL $\geq \Omega(\max\{H_{\Delta}(Y|X), H_{\Delta}(X|Y)\})$



Lower Bound: Summary



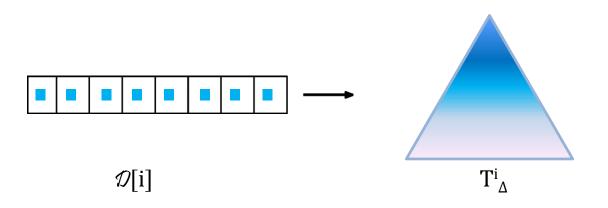
 $\geq \sum_{i=1}^{n} p(i) (H_{\Delta}(Y | X=i))$

 $= \Omega(H_{\Delta}(Y | X))$

Can DANs Reach The Entropy Speed Limit? Upper Bounds on EPL

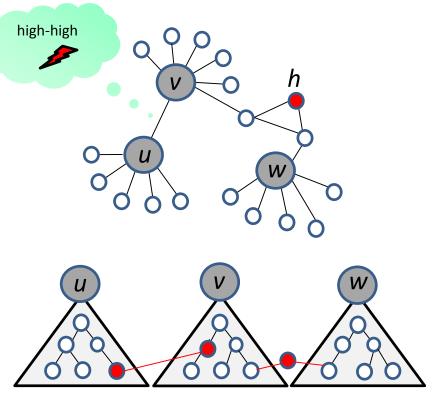


Ego-Trees Revisited



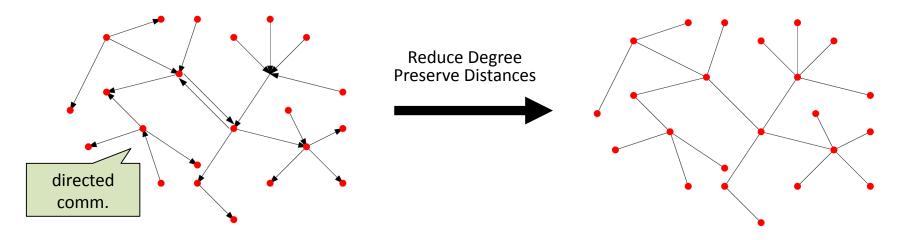
(Tight) Upper Bounds: Algorithm Idea

- Idea: construct per-node optimal tree
 - BST (e.g., Mehlhorn)
 - Huffman tree
 - Splay tree (!)
- Take union of trees but reduce degree
 - E.g., in *sparse distribution*: leverage helper nodes between two "large" (i.e., high-degree) nodes



How to Reduce Degree? Example: Tree Distributions

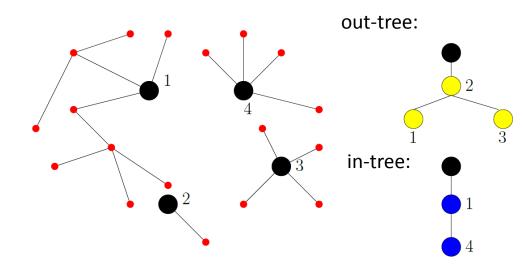
Theorem: Let \mathcal{D} be such that $G_{\mathcal{D}}$ is a tree (ignoring the edge direction). It is possible to generate a DAN with maximum degree 8, such that, $EPL(\mathcal{D}, N) \leq O(H(Y|X) + H(X|Y))$.



Tree Distributions

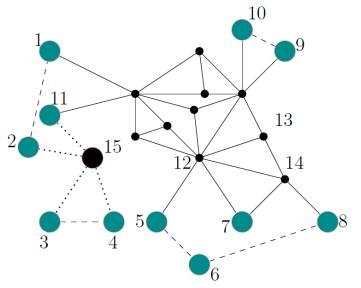
Proof idea:

- Make tree rooted and directed: gives parent-child relationship
- Arrange the outgoing edges (to children) of each node in a binary (Huffman) tree
- Repeat for the incoming edges: make another another binary (Huffman) tree with incoming edges from children
- Analysis
 - Can *appear in at most 4 trees*: in&out own tree and in&out tree of parent (parent-child helps to avoid many "children trees")
 - **Degree** at most 6
 - Huffman trees maintain *distortion*: proportional to *conditional entropy*



Generalize to Arbitrary Sparse Distributions

Demand graph:

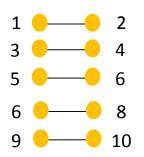


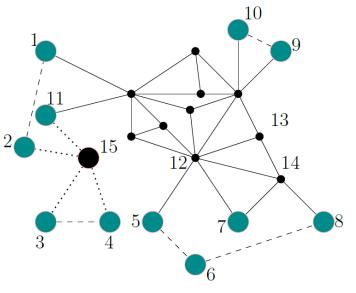
Demand

Sparse Distributions: Construction

Demand graph:

Low-low edges: remove from guest, add to DAN





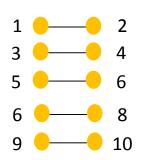
DAN

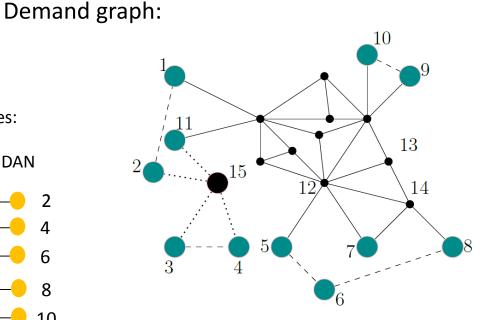
Demand

Sparse Distributions: Construction

High degree nodes with low degree neighbors: need binarization

Low-low edges: remove from guest, add to DAN

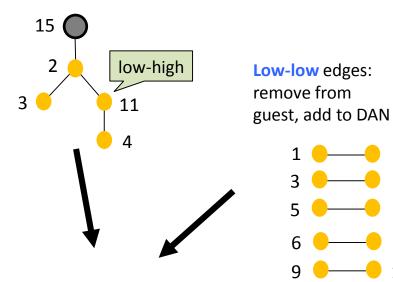




DAN

Sparse Distributions: Construction

High degree nodes with low degree neighbors: need binarization



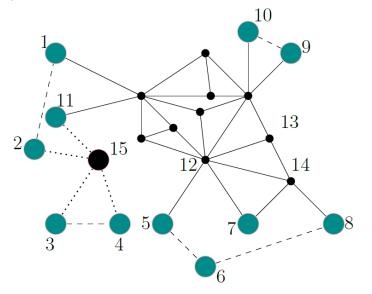
Remove from guest, add to DAN!

Demand graph:

6

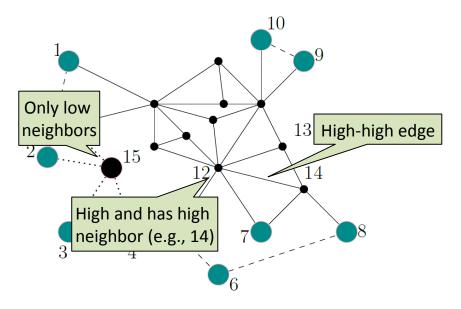
8

10



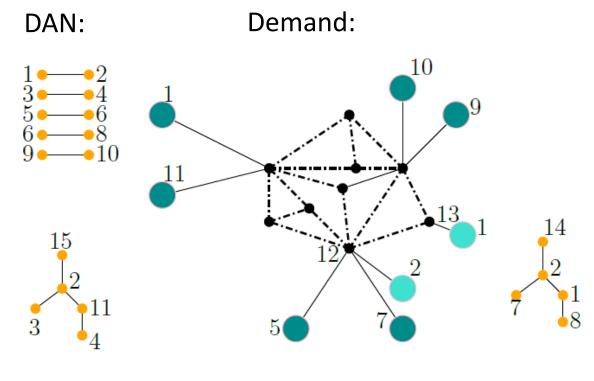
Sparse Distributions: Construction

- Find low degree nodes
 - Half of the nodes of lowest degree: "below twice average degree"
- Find high degree nodes having only low degree neighbors (e.g., 15 but not 12):
 - Create optimal binary tree with low degree neighbors
- Put the low-low edges and the binary tree into DAN and remove from demand
- Mark high-high edges
 - Put (any) low degree nodes in between (e.g., 1 or 2):
 one is enough so distanced increased by +1
- Now high degree nodes have only low degree neighbors: make tree again



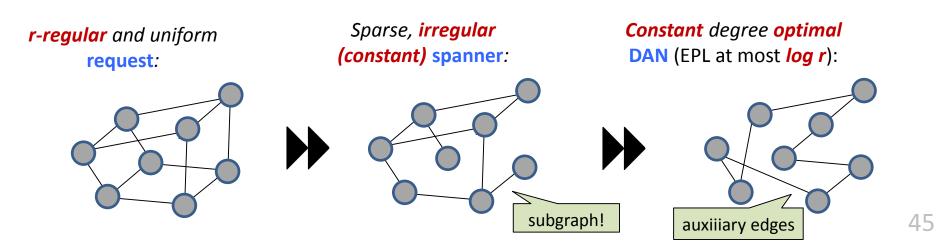
Example Illustrated

- Find low degree nodes
- Mark low-low edges
- Find high degree nodes with only low degree neighbors (e.g., 15)
- Make **binary tree** for them
- Add low degree node (e.g., 1 and 2) between high-high edge (e.g., 12-14, e.g., 14 has two high-degree neighbors 12 and 13)
- Now high nodes have only low neighbors as well, so make tree again (at 12-14)

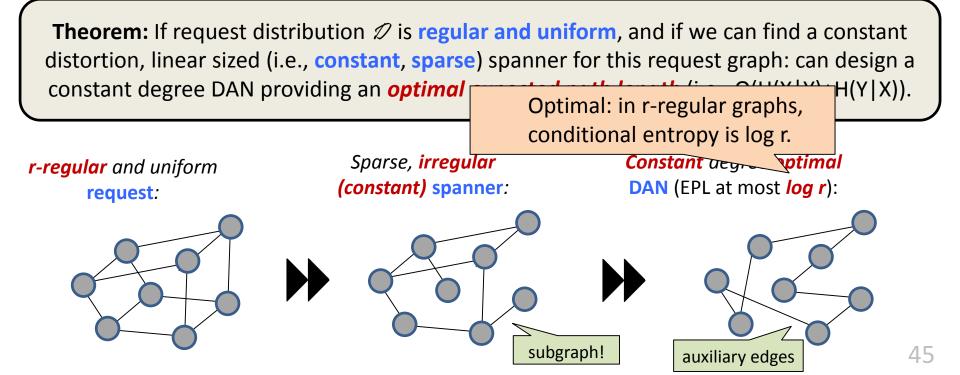


Regular and Uniform Distribution: Leveraging The Connection to Spanners

Theorem: If request distribution \mathscr{D} is **regular and uniform**, and if we can find a constant distortion, linear sized (i.e., **constant**, **sparse**) spanner for this request graph: can design a constant degree DAN providing an **optimal expected path length** (i.e., O(H(X|Y)+H(Y|X))).

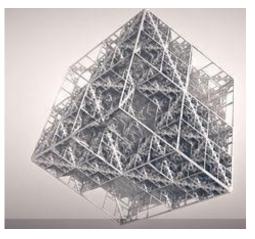


Regular and Uniform Distribution: Leveraging The Connection to Spanners



Reduction from Spanner

- Proof technique: degree-reduction again, this time *from sparse spanner* (before: from sparse demand graph)
- Consequences: optimal DAN designs for
 - Hypercubes (with n log n edges) Has sparse 3-spanner.
 - Chordal graphs Has sparse O(1)-spanner.
 - Trivial: graphs with polynomial degree (dense graphs)



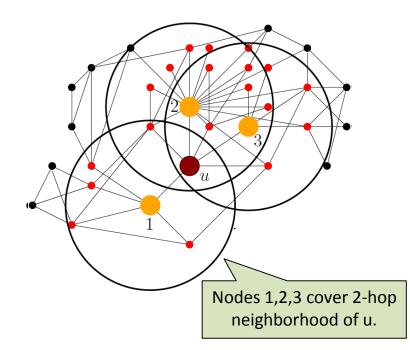
A dense graph

Another Example: Demands of Locally-Bounded Doubling Dimension

- LDD: G_𝖉 has a Locally-bounded Doubling Dimension (LDD) iff all 2hop neighbors are covered by 1-hop neighbors of just λ nodes
 - Note: care only about 2-neighborhood

We only consider 2 hops!

- Formally, $B(u, 2) \subseteq \bigcup_{i=1}^{\lambda} B(v_i, 1)$
- Challenge: can be of *high degree*!



DAN for Locally-Bounded Doubling Dimension

Lemma: There exists a sparse 9-(subgraph)spanner for LDD.

This *implies optimal DAN*: still focus on regular and uniform!

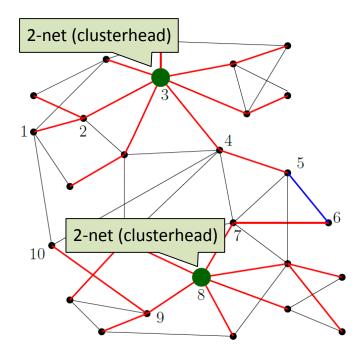
Def. (ϵ -net): A subset V' of V is a ϵ -net for a graph G = (V, E) if

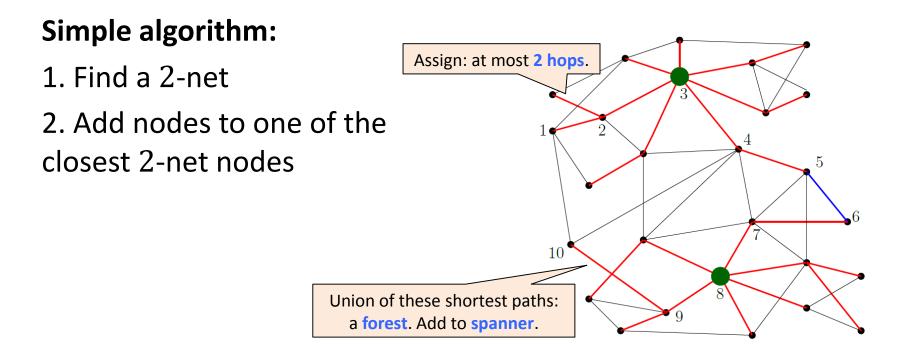
- V' sufficiently "independent": for every $u, v \in V$, $d_G(u, v) > \varepsilon$
- "dominating" V: for each $w \in V$, \exists at least one $u \in V$ ' such that, $d_G(u,w) \leq \epsilon$

Simple algorithm:

1. Find a 2-net

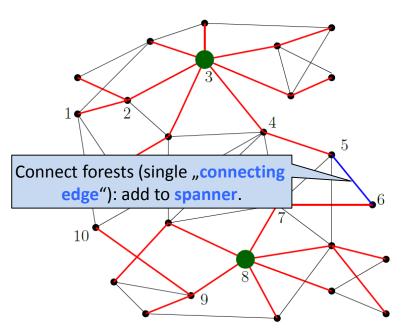
Easy: Select nodes into 2-net one-by-one in decreasing (remaining) degrees, remove 2-neighborhood. Iterate.





Simple algorithm:

- 1. Find a 2-net
- 2. Add nodes to one of the closest 2-net nodes
- 3. Join two clusters if there are edges in between





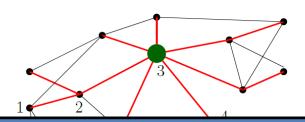
Distortion 9: Detour via clusterheads: u,ch(u),x,y,ch(v),v

2. Add nodes to one of the

closest 2-net node

3. Join two clusters edges in between

Sparse: Spanner only includes forest (sparse) plus
"connecting edges": but since in a locally doubling
dimension graph the number of cluster heads at
distance 5 is bounded, only a small number of
neighboring clusters will communicate.



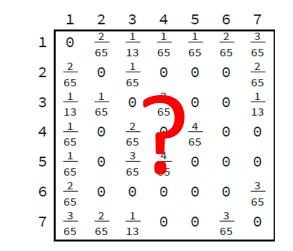
Further Reading

Demand-Aware Network Designs of Bounded Degree Chen Avin, Kaushik Mondal, and Stefan Schmid. 31st International Symposium on Distributed Computing (**DISC**), Vienna, Austria, October 2017.

So how useful are entropy-proportional DANs?

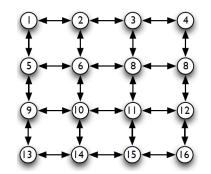
It depends...

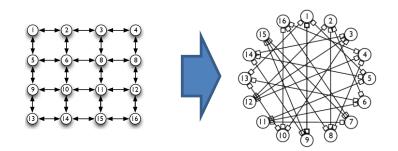
- Demand-oblivious network: no information about matrix: maximum uncertainty (entropy), so EPL = entropy = Ω(log n)...
 - ... even if the demand matrix has a very low actual entropy
- Actual entropy depends on *spatial locality* of communication



Example 1: 2-dim Grid

Low **spatial locality**: conditional entropy *less than two* (i.e., O(1))

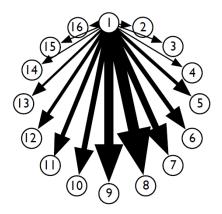


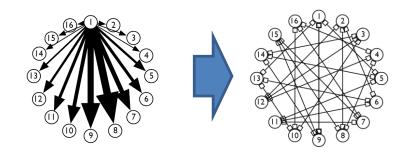


But **embedding** a 2-dim grid demand graph on a const-degree expander would result in $\Omega(\log n)$ path lengths

Example 2: Weighted Star

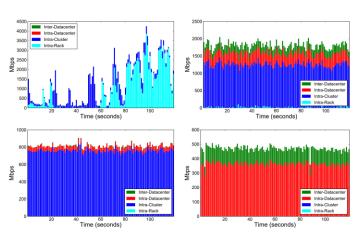
Low **spatial locality**: conditional entropy can be **very small** if skew is large





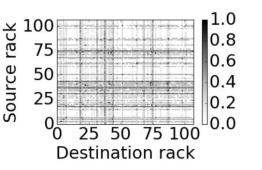
But **embedding** a weighted star demand graph on a const-degree expander would result in $\Omega(\log n)$ path lengths

Many Empirical Studies Confirm Spatial Locality



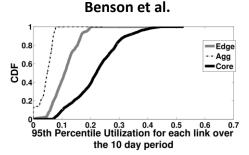
Facebook

Inside the Social Network's (Datacenter) Network @ SIGCOMM 2015



Microsoft

ProjecToR @ SIGCOMM 2016



Understanding Data Center Traffic Characteristics @ WREN 2009

Roadmap

Vision and Motivation

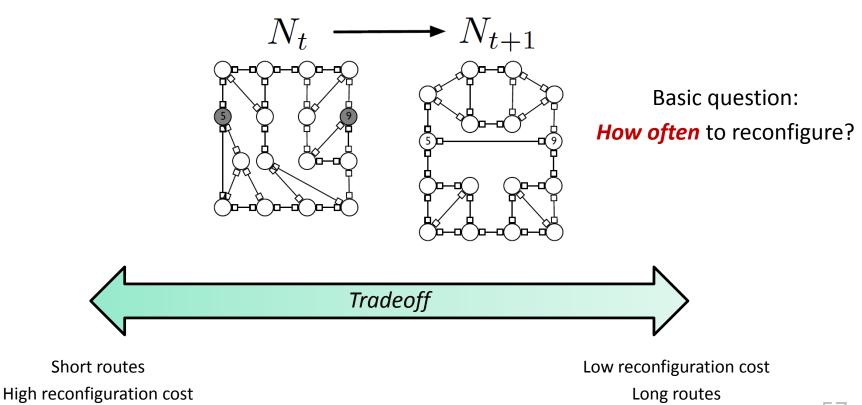


- An analogy: coding and datastructures
- Principles of Demand-Aware Network (DAN) Designs
- Principles of Self-Adjusting Network (SAN) Designs
- Principles of Decentralized Approaches

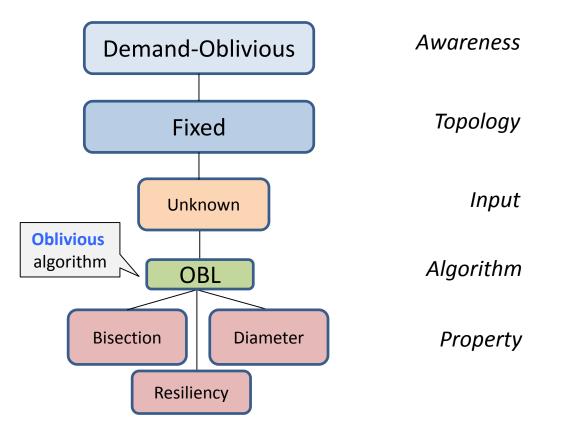


What Are the Objectives and Metrics for SANs?

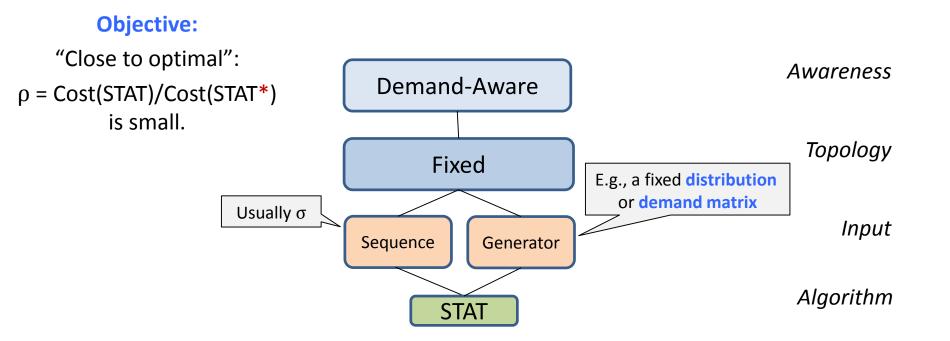
Model: A Cost-Benefit Tradeoff

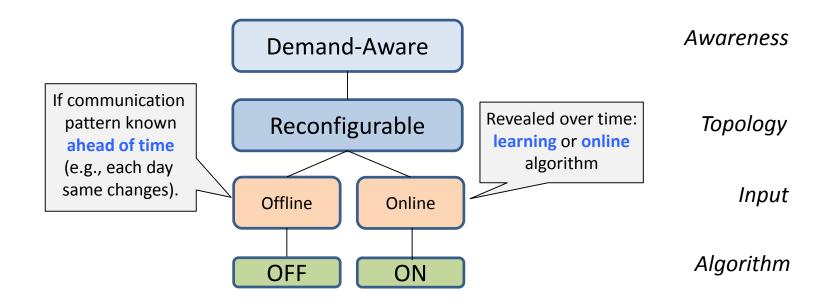


A Taxonomy: Traditional Networks



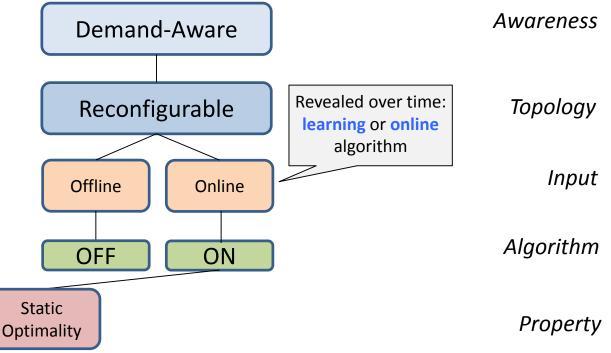
A Taxonomy: Static DANs

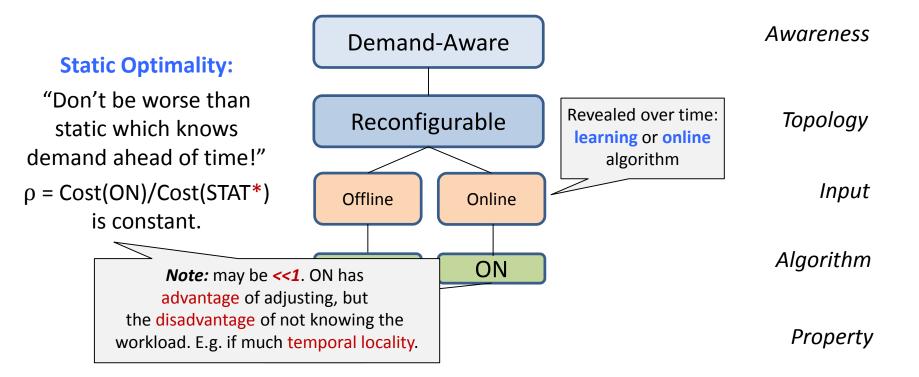




Static Optimality:

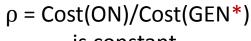
"Don't be worse than static which knows demand ahead of time!" ρ = Cost(ON)/Cost(STAT*) is constant.





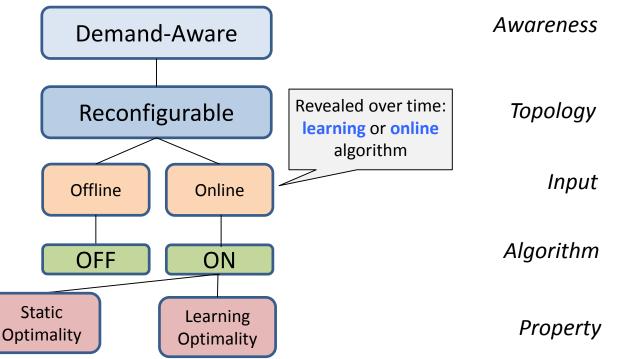
Learning Optimality:

"Don't be worse than a dynamic algorithm which knows the (fixed) generator!"



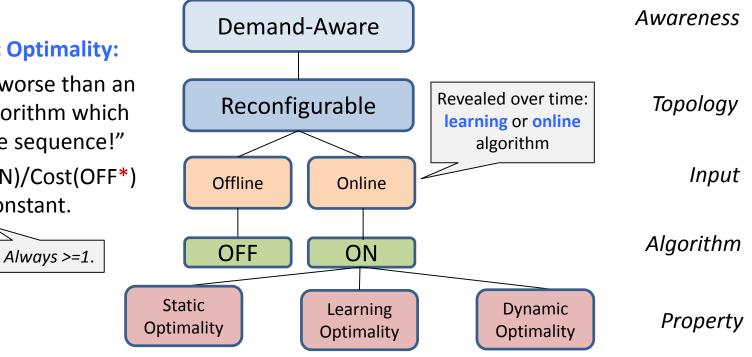
is constant.

Always >=1.



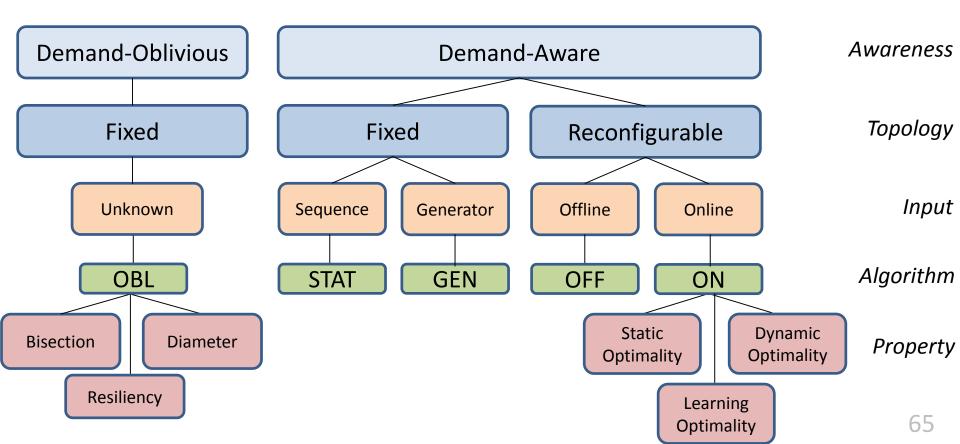
Dynamic Optimality:

"Don't be worse than an offline algorithm which knows the sequence!" $\rho = Cost(ON)/Cost(OFF^*)$ is constant.



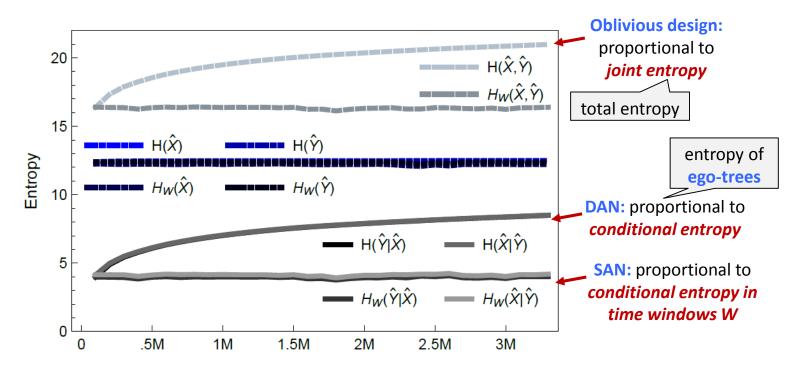
Taxonomy

Toward Demand-Aware Networking: A Theory for Self-Adjusting Networks. **ArXiv** 2018.



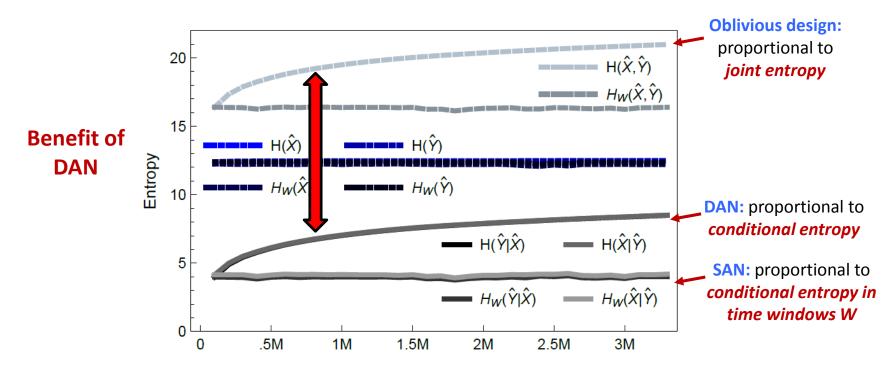
When are SANs better than DANs?

If There is Much Temporal Locality



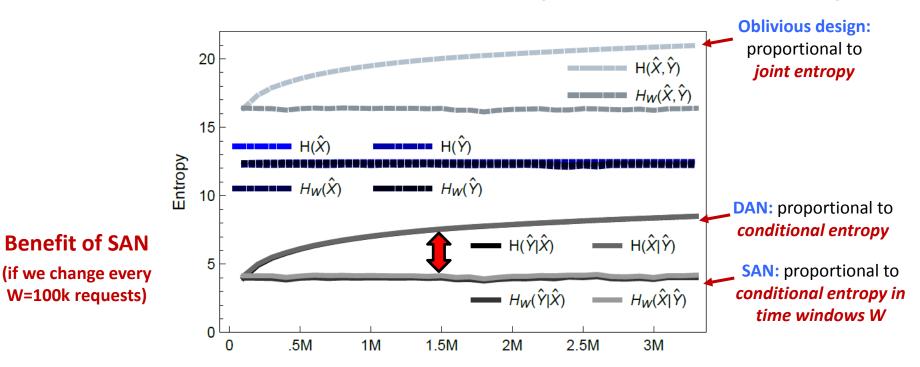
Entropy measures in Facebook's workload (3 million requests)

If There is Much Temporal Locality



Entropy measures in Facebook's workload (3 million requests)

If There is Much Temporal Locality



Entropy measures in Facebook's workload (3 million requests)

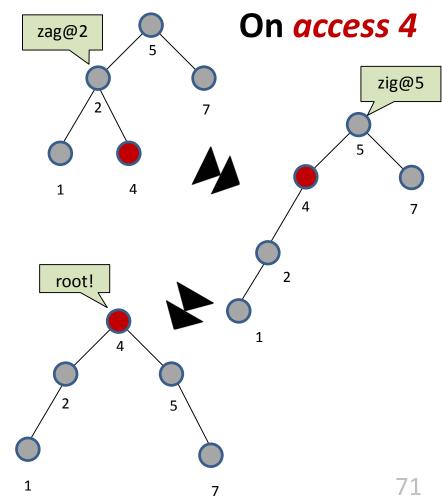
How to Design SANs?



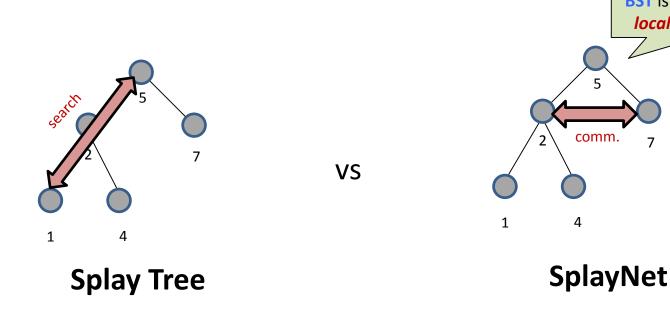
Inspiration from self-adjusting datastructures again!

The Classic Self-Adjusting Datastructure: Splay Tree

- A Binary Search Tree (BST)
- Inspired by "move-to-front": move to root!
- Self-adjustment: zig, zigzig, zigzag
 - Maintains search property
- Many nice properties
 - Static optimality, working set, (static,dynamic) fingers, ...



A Simple Idea: Generalize Splay Tree To SplayNet





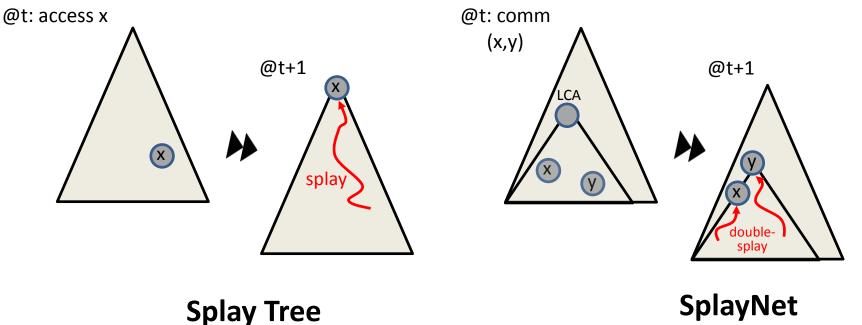
7

4

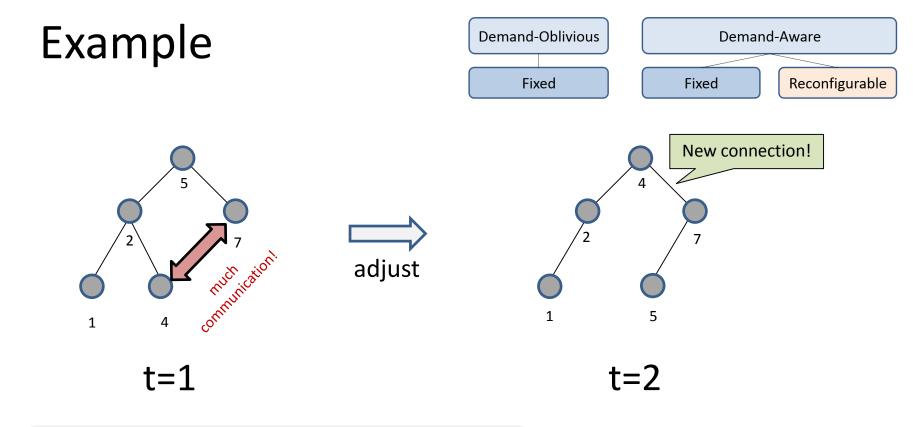
A Simple Idea: Generalize Splay Tree To SplayNet



SplayNet: A Simple Idea



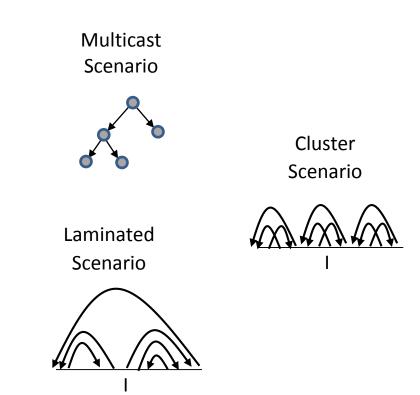
SplayNet



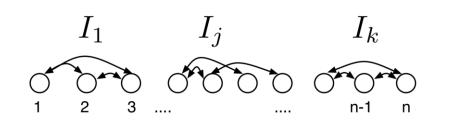
Challenges: How to minimize reconfigurations? How to keep network locally routable?

Properties of SplayNets

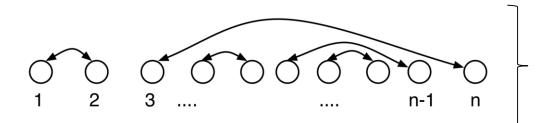
- Statically optimal if demand comes from a product distribution
 - Product distribution: entropy equals conditional entropy, i.e., H(X)+H(Y)=H(X|Y)+H(X|Y)
- Converges to optimal static topology in
 - Multicast scenario: requests come from a BST as well
 - Cluster scenario: communication only within interval
 - Laminated scenario : communication is "noncrossing matching"



More Specifically



Cluster scenario: SplayNet will converge to state where path between cluster nodes only includes cluster nodes



Non-crossing matching scenario: SplayNet will converge to state where all communication pairs are adjacent

Remark: Fast Static SplayNet

Decouple cost to ouside:

distance to root of T₁ only

Theorem: Optimal static SplayNet can be computed in polynomial-time (dynamic programming)

- Unlike unordered tree?
- 1. Define: flow out of interval I

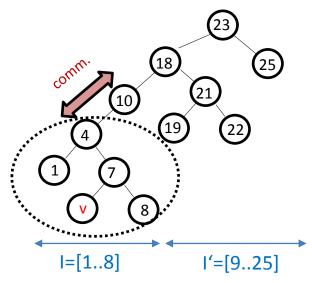
 $W_{I}(v)=\sum_{u \in I'} w(u, v) + w(v, u)$

2. Cost of a given tree T_1 on I:

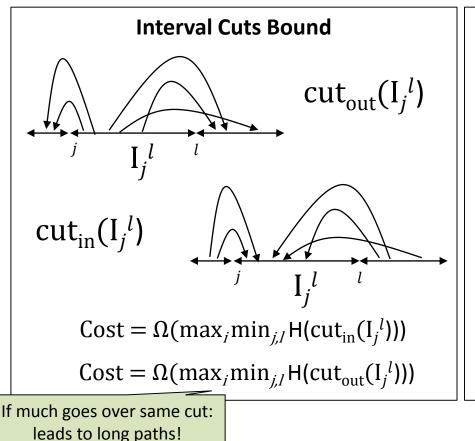
Cost(T_I, W_I)=[$\sum_{u,v \in I} (d(u,v) + 1)w(u,v)$] + $D_I * W_I$ (D_I distances of nodes in I from root of T_I)

3. Dynamic program over intervals

Choose optimal root and add dist to root



Remark: Improved Lower Bounds



Edge Expansion Bound

- Let cut W(S) be weight of edges in cut (S,S') for a given S
- Define a distribution w_s (u) according to the weights to all possible nodes v:

$$w_S(u) = \sum_{\substack{(u,v) \in E(S,\bar{S})\\ u \in S}} w(u,v) / W(S)$$

 Define entropy of cut and src(S),dst(S) distributions accordingly: :

 $\varphi_H(S) = W(S) \left(H(\operatorname{src}(S)) + H(\operatorname{dst}(S)) \right)$

• Conductance entropy is lower bound:

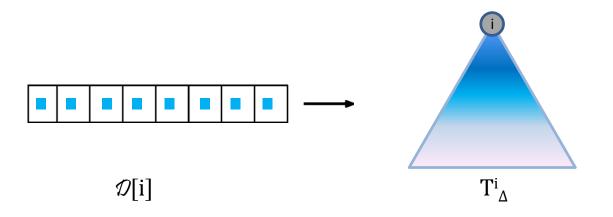
 $\Omega(\phi_H(\mathcal{R}(\sigma)))$

For SplayNets: stronger lower bounds than conditional entropy.

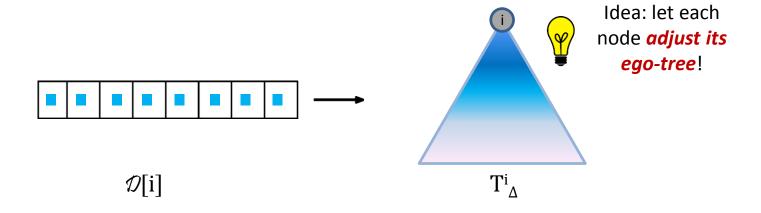
Further Reading

SplayNet: Towards Locally Self-Adjusting Networks Stefan Schmid, Chen Avin, Christian Scheideler, Michael Borokhovich, Bernhard Haeupler, and Zvi Lotker. IEEE/ACM Transactions on Networking (**TON**), Volume 24, Issue 3, 2016.

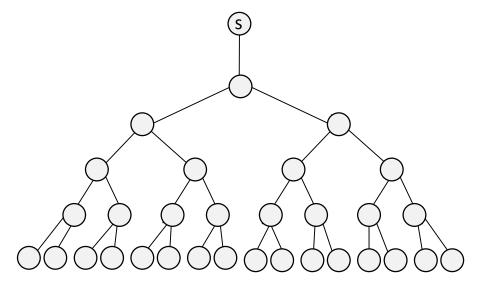
Better Idea: Back to Ego-Trees!



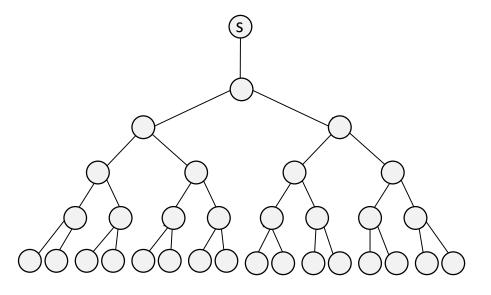
Better Idea: Back to Ego-Trees!



- **Push-down tree:** a self-adjusting complete tree
- Dynamically optimal
- Not ordered: requires a map



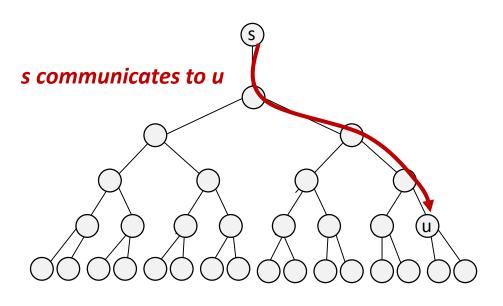
- Push-down tree: a self-adjusting complete tree
- Dynamically optimal
- Not ordered: requires a map



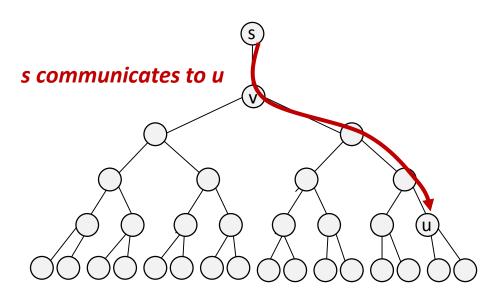
A useful dynamic property: Most-Recently Used (MRU)!

Similar to Working Set Property: more recent communication Partners closer to source.

- **Push-down tree:** a self-adjusting complete tree
- Dynamically optimal
- Not ordered: requires a map



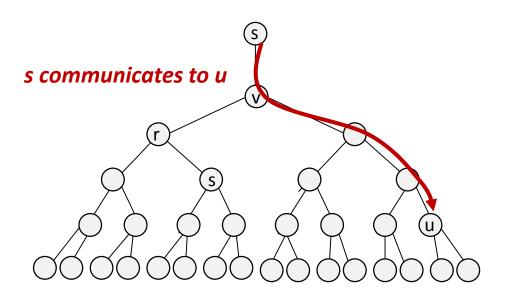
- **Push-down tree:** a self-adjusting complete tree
- Dynamically optimal
- Not ordered: requires a map





Strict MRU requires: move u to root! But how? Cannot swap with v: v no longer MRU!

- Push-down tree: a self-adjusting complete tree
- Dynamically optimal
- Not ordered: requires a map



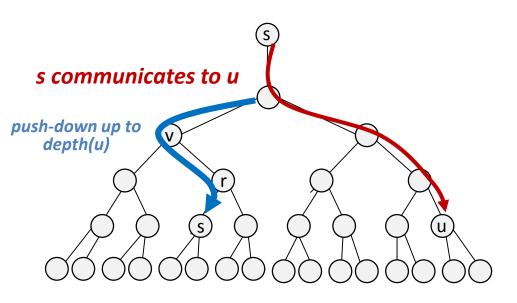


Strict MRU requires: move u to root! But how? Cannot swap with v: v no longer MRU!



Idea: Push v down, in a balanced manner, up to depth(u): left-right-left-right ("rotate-push")

- Push-down tree: a self-adjusting complete tree
- Dynamically optimal
- Not ordered: requires a map



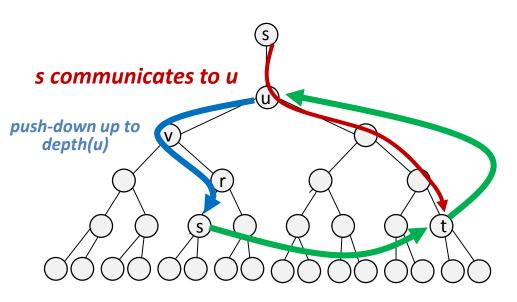


Strict MRU requires: move u to root! But how? Cannot swap with v: v no longer MRU!



Idea: Push v down, in a balanced manner, up to depth(u): left-right-left-right ("rotate-push")

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- Not ordered: requires a map

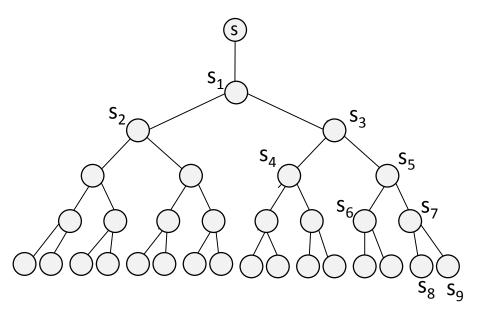




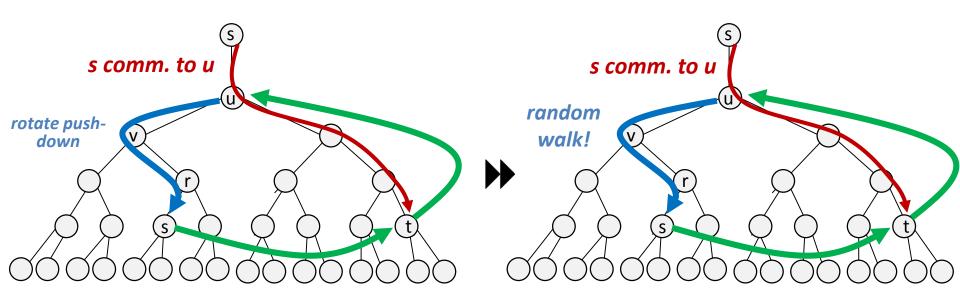
Then: promote u to available root, and t to u: at original depth!

Remarks

- Unfortunately, alternating push-down does *not maintain MRU* (working set) property
- Tree can *degrade*, e.g.: sequence of requests from level 4,1,2,1,3,1,4,1



Solution: Random Walk



At least maintains approximate working set / MRU!

Further Reading

Push-Down Trees: Optimal Self-Adjusting Complete Trees Chen Avin, Kaushik Mondal, and Stefan Schmid. **ArXiv** Technical Report, July 2018.

Roadmap

Vision and Motivation

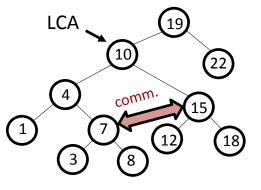


- An analogy: coding and datastructures
- Principles of Demand-Aware Network (DAN) Designs
- Principles of Self-Adjusting Network (SAN) Designs
- Principles of Decentralized Approaches



A "Simple" Decentralized Solution: Distributed SplayNet (*DiSplayNet*)

- SplayNet attractive: ordered BST supports local routing
 - Nodes *maintain three ranges*: interval of left subtree, right subtree, upward
- If communicate (frequently): double-splay toward LCA
- Challenge: concurrency!
 - Access Lemma of splay trees no longer works: *potential function* does not *"telescope"* anymore: a concurrently rising node may push down another rising node again



SplayNet

DiSplayNet: Challenges

- DiSplayNet: Rotations (zig,zigzig,zigzag) are *concurrent*
- To avoid conflict: distributed computation of independent clusters

• Still challenging:

	1	2	3	4	5	6	7	8	 i – 6	i – 5	i – 4	i – 3	i – 2	i – 1	i
σ_1	1	~	1	~	-	-	-	-	 -	-	-	-	-	-	-
σ_2	-	X	X	X	✓	✓	✓	-	 -	-	-	-	-	-	-
σ_{m-1}	-	-	-	-	-	-	-	-	 ✓	 Image: A set of the set of the	-	-	-	-	-
σ_m	-	-	-	-	-	-	-	-	 X	X	1	1	1	1	-

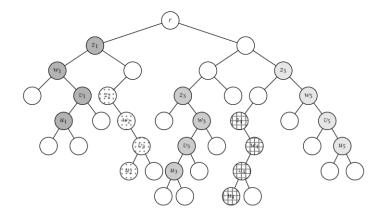
Sequential SplayNet: requests *one after another*

i + 3 i + 4i + 51 1 1 1 1 1 X х Х 1 х х X X X

DiSplayNet: Analysis more challenging: potential function sum no longer **telescopic**. One request can "push-down" another.

DiSplayNet: Challenges

- DiSplayNet: Rotations (zig,zigzig,zigzag) are *concurrent*
- To avoid conflict: distributed computation of independent clusters



• Still challenging:

Telescopic: max potential drop



Sequential SplayNet: requests one after another

i + 3 i + 4i + 51 1 1 1 1 1 1 1 1 1 X X X Х Х 1 х X X X X X X

DiSplayNet: Analysis more challenging: potential function sum no longer **telescopic**. One request can "push-down" another.

Further Reading

Brief Announcement: Distributed SplayNets Bruna Peres, Olga Goussevskaia, Stefan Schmid, and Chen Avin. 31st International Symposium on Distributed Computing (**DISC**), Vienna, Austria, October 2017.

Roadmap

Vision and Motivation

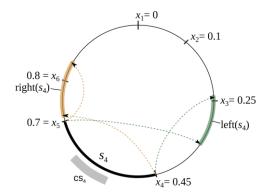


- An analogy: coding and datastructures
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- Principles of Decentralized Approaches



Many Open Questions

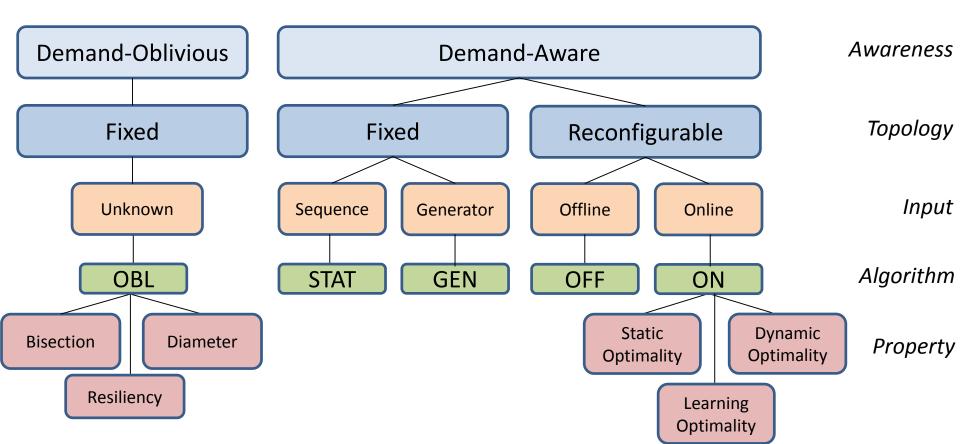
- E.g., robust demand-aware networks?
 - First idea: rDAN, based on continuous-discrete approach and Shannon-Fano-Elias coding
- Serving dense communication patterns
- Distributed version



rDAN: Toward Robust Demand-Aware Network Designs. Chen Avin, Alexandr Hercules, Andreas Loukas, and Stefan Schmid. Information Processing Letters (IPL), Elsevier, 2018.

Uncharted Landscape!

Toward Demand-Aware Networking: A Theory for Self-Adjusting Networks. **ArXiv** 2018.



Conclusion

- Networked systems become reconfigurable
- First techniques emerging (e.g., ego-trees)
- How much it helps depends on spatial and temporal locality
- Entropy seems to be a useful metric

Thank you! Question?

Chen Avin and Stefan Schmid. ArXiv Technical Report, July 2018. Demand-Aware Network Designs of Bounded Degree Chen Avin, Kaushik Mondal, and Stefan Schmid. 31st International Symposium on Distributed Computing (DISC), Vienna, Austria, October 2017. Push-Down Trees: Optimal Self-Adjusting Complete Trees Chen Avin, Kaushik Mondal, and Stefan Schmid. ArXiv Technical Report, July 2018. **Online Balanced Repartitioning** Chen Avin, Andreas Loukas, Maciej Pacut, and Stefan Schmid. 30th International Symposium on Distributed Computing (DISC), Paris, France, September 2016. rDAN: Toward Robust Demand-Aware Network Designs Chen Avin, Alexandr Hercules, Andreas Loukas, and Stefan Schmid. Information Processing Letters (IPL), Elsevier, 2018. SplayNet: Towards Locally Self-Adjusting Networks Stefan Schmid, Chen Avin, Christian Scheideler, Michael Borokhovich, Bernhard Haeupler, and Zvi Lotker. IEEE/ACM Transactions on Networking (TON), Volume 24, Issue 3, 2016. Early version: IEEE IPDPS 2013. Characterizing the Algorithmic Complexity of Reconfigurable Data Center Architectures Klaus-Tycho Foerster, Monia Ghobadi, and Stefan Schmid. ACM/IEEE Symposium on Architectures for Networking and Communications Systems (ANCS), Ithaca, New York, USA, July 2018. Charting the Complexity Landscape of Virtual Network Embeddings Matthias Rost and Stefan Schmid. IFIP Networking, Zurich, Switzerland, May 2018. Chapter 72: Overlay Networks for Peer-to-Peer Networks Andrea Richa, Christian Scheideler, and Stefan Schmid. Handbook on Approximation Algorithms and Metaheuristics (AAM), 2nd Edition, 2017.

Toward Demand-Aware Networking: A Theory for Self-Adjusting Networks